ZCA 110 Calculus Test 3.Venue: DPD; Date: Friday, 11 am- 12pm9 Dec 2016Name:Matrix No:Q1.Given that u(x) is a differentiable function, explain how the following integration rule is

derived. [Hint: You may have to start from the differentiation of u^n]

$$\int u^n \, \mathrm{du} = \frac{1}{n+1} \, u^{n+1} + C; \ n \neq -1.$$

Q2.Given $f(x) = \frac{\sin x + x \cos x}{\exp(x) + \exp(-x)}$, evaluate $\int_{-\pi}^{\pi} f(x) dx$.

Q3. Find the length of the curve parametrised by $x = 2t^2 + 1$, $y = 2t^3$, $0 \le t \le 1$.

Q4. Explain how the following differential result is derived: $\frac{d}{dx}e^{x}=e^{x}$.

Q5. Prove $\frac{e^{x_2}}{e^{x_1}} = e^{x_2} \cdot e^{-x_1}$, for all real numbers x_1 and x_2 .