

Special Assignment ZCE 111

First Part: Planckian locus

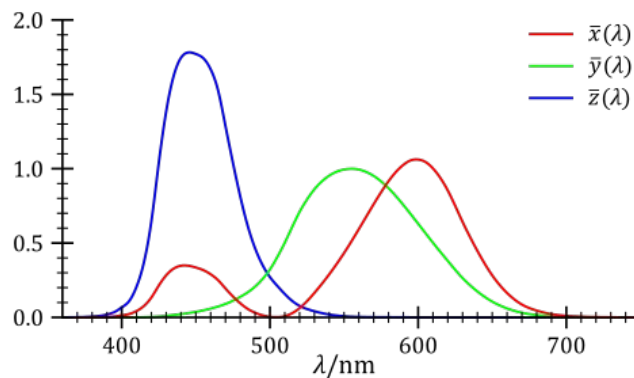
Read Planckian locus on https://en.wikipedia.org/wiki/Planckian_locus

In the **CIE XYZ color space**, the three coordinates defining an electromagnetic spectrum are given by X_T, Y_T, Z_T :

$$X_T = \int \bar{x}(\lambda) M(\lambda, T) d\lambda, Y_T = \int \bar{y}(\lambda) M(\lambda, T) d\lambda, Z_T = \int \bar{z}(\lambda) M(\lambda, T) d\lambda,$$

where $M(\lambda, T)$ is the **spectral radiant exitance** of the light being viewed, and $\bar{x}(\lambda), \bar{y}(\lambda), \bar{z}(\lambda)$ are the **color matching functions** of the CIE **standard colorimetric observer**, shown in the diagram illustration 1, and λ is the wavelength.

Illustration



The Planckian locus is determined by substituting into the above equations the black body spectral radiant exitance, which is given by **Planck's law**:

$$M(\lambda, T) = \frac{c_1}{\lambda^5} \frac{1}{\exp\left(\frac{c_2}{\lambda T}\right) - 1}$$

where:

$c_1 = 2\pi hc^2$ is the **first radiation constant**

$c_2 = hc/k$ is the **second radiation constant**

and

M is the black body spectral radiant exitance (power per unit area per unit wavelength: watt per square meter per meter (W/m³))

T is the **temperature** of the black body

h is **Planck's constant**

c is the **speed of light**

k is **Boltzmann's constant**

This will give the Planckian locus in CIE XYZ color space. If these coordinates are X_T, Y_T, Z_T where T is the temperature, then the CIE chromaticity coordinates will be

$$x_T = \frac{X_T}{X_T + Y_T + Z_T}$$

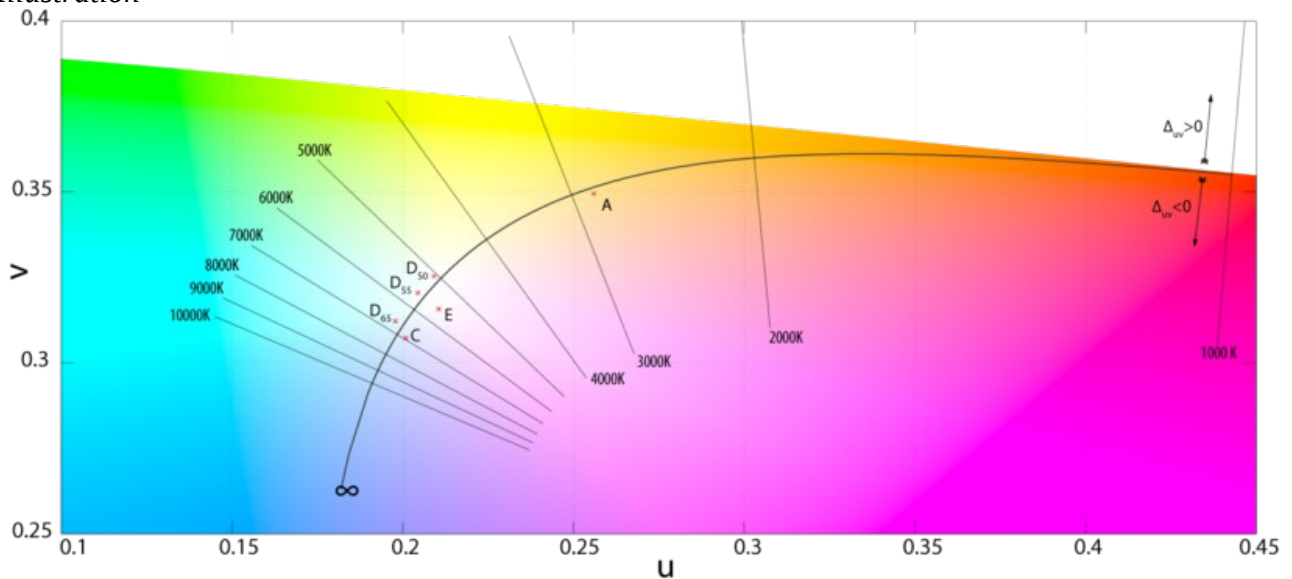
$$y_T = \frac{Y_T}{X_T + Y_T + Z_T}$$

A pair of chromaticity coordinates (x,y) can be expressed in MacAdam's chromaticity scale (u, v) as

$$u = \frac{4x}{-2x + 12y + 3}, \quad v = \frac{6y}{-2x + 12y + 3}$$

A Planckian locus can be mapped out in the (u,v) chromaticity space, see Illustration 2.

Illustration



Task No.1 to perform: Given the CIE color matching functions data, write a code to automatically generate the Planckian locus in (u,v) space as shown in Illustration 2. The numerical data file for the color matching functions $\bar{x}(\lambda), \bar{y}(\lambda), \bar{z}(\lambda)$ can be downloaded from http://comsics.usm.my/tlyoon/teaching/ZCE111_1516SEM2/data/StdObsFuncs.xls (as an Excel file).

Second Part: Correlated Color temperature (CCT)

Read CCT on https://en.wikipedia.org/wiki/Color_temperature

The tristimulus values (X,Y,Z) for a colour with a spectral power distribution $S(\lambda)$ are given in terms of:

$$X = \int S(\lambda) \bar{x}(\lambda) d\lambda, Y = \int S(\lambda) \bar{y}(\lambda) d\lambda, Z = \int S(\lambda) \bar{z}(\lambda) d\lambda,$$

where λ is the wavelength of the equivalent monochromatic light (measured in nanometers). In practice, $S(\lambda)$ is a spectrum measured experimentally, e.g., that emitted from a LED light bulb.

Task No. 2 to perform: Download the numerical data of a spectrum $S(\lambda)$ from http://comsics.usm.my/tlyoon/teaching/ZCE111_1516SEM2/data/spectral_power_distribution.dat. Note that the numerical data for $S(\lambda)$ is expressed in SI unit (in particular the wavelength values (in the first column) is in unit of meter).

Modify your code from **Task No. 1** to obtain the chromaticity coordinates for the spectrum $S(\lambda)$. Call it $C_s(u_s, v_s)$.

Answer: $(u_s, v_s) = (0.210696, 0.321492)$

Task No. 3 to perform: Extend your code to do the following: Identify a point on the Planckian locus $P_N(u_N, v_N)$ at which the normal line at that point passes through $C_s(u_s, v_s)$. Identify the temperature corresponds to the Planckian locus point $P_N(u_N, v_N)$. This temperature is the CCT of the spectrum $S(\lambda)$.

Answer:

$P_N(u_N, v_N) = (0.212529, 0.323398)$

5259.3 K

Task No. 4 to perform: Output a diagram displaying (i) the Planckian curve, (ii) the point $C_s(u_s, v_s)$, (iii) $P_N(u_N, v_N)$, (iii) the normal line that passes through both $C_s(u_s, v_s)$ and $P_N(u_N, v_N)$, see the sample output below.

Note:

1. Make sure that your code must output explicitly (a) the values of the CCT for $S(\lambda)$, (b) the $C_s(u_s, v_s)$ dot, (c) the $P_N(u_N, v_N)$ dot, (d) the Planckian locus and (e) the normal line.
2. Your code should be fully automatic and should produce all the required output at a press of a button without any manual intervention (except the act of pressing the shift+enter burron keys).

Illustration

(a) CCT = ?? K

