ZCT 104 (Class A)

MODERN PHYSICS

ACADEMIC SESSION 2007/08 (SECOND SEMESTER)

LECTURE NOTES, TUOTRIAL PROBLEM SET And PAST YEAR QUESTIONS

> By Yoon Tiem Leong School Of Physics USM, Penang

ZCT 104 Modern Physics (Class A)

General information

This is a Kursus Teras offered by school of physics only in semester II. The course ZCT 104 is split into two separate classes, i.e. ZCT 104 (Class A and Class B). The two classes are to be handled concurrently and independently by two different lecturers, namely Yoon Tiem Leong for ZCT 104 (Class A) and Dr. Ng Sha Shiong for ZCT 104 (Class B). The coursework assessment and final exam will be the same for both classes. In general, both classes will be using different sets of lecture notes and tutorial questions (though same overlap may be possible).

Generally ZCT 104 is taken by most first year students in the school of physics. This course serves the purpose to prepare the basic foundation for any science students (particularly physics students) who would need this very important basic mathematics in their future undertaking of any discipline of study. The course will be conducted in English. However, students can answer in either Bahasa or English in the final exam.

Since this is a 3 units course, as a rough guide, students have to spend about 3 hours for revision per week for this course. In other words, if you spend about 3 hours per week to practice the exercises it would be suffice to pass the course. Of course, if a student wants to score excellently he/she is required to walk an extra mile by spending more time than suggested for practicing the exercises

Lecturer for class A: <u>Yoon Tiem Leong</u>, School of Physics, USM, Room 115, Tel:04-6533674; e-mail: <u>tlyoon@usm.my</u>.

Course Meeting Times

Lectures: Two lectures per week + 1 tutorial class per week

- 1) Monday, E 48A, 12.00-1.00 pm (lecture)
- 2) Wednesday, DKH, 9.00-9.50am (lecture)
- 3) Friday, SK1, 4.00-4.50 pm (tutorial) .

This course is intended to cover some of the standard concepts in modern physics since 1900. It includes special theory of relativity, wave-particle duality of light and material particles, introductory quantum theory of atoms and introductory quantum mechanics. The course aims to lay the foundational concepts for students who would take up papers on quantum mechanics at a higher level.

Course Duration

This course is offered in the second semester for science students in USM -- a 14-week term at USM that runs from 17 Dec 2007 until end of March 2007.

Course Prerequisites

Since ZCT 104 is conducted in English, students must prepare to take the challenge to deal with language barrier (if relevant). Despite requiring no formal prerequisites (prasyarat kursus), students are assumed to be familiar with elementary calculus, differential equations, and Newtonian mechanics. Most importantly, students are expected to exercise independence throughout the learning process. This course demands ones to think critically to comprehend some rather counter intuitive physics ideas.

Consultation hours

There is no specific timeslots allocated for consultation with the lecturer as he of dedicated willingness to offer consultation and advice to students who wish to engage discussion with him. The principle of the lecturer is that: as long as the students are showing enthusiasm to learn, he will be willing to offer his time for discussion. However, in order to avoid inconvenience students are advised to call up (ext 3674) or email him (tlyoon@usm.my) before rushing into his office. His door is always open to anyone who is keen to explore physics.

Textbooks

The following textbooks are required or strongly recommended. There exist many good textbooks on the topics of modern physics. I have decided to select the following as my main reference texts. Lecture materials are written based on them. It is strongly advised that students should not be contented with the lecture material supplied by the lecturer alone. They should make reference to these suggested texts and do the reading on a consistent manner. You gonna prepare to think in an intellectual manner in order to comprehend the essential concepts I wish to convey in this course. To people who are expecting to make only mechanical memorisation and pass with flying colour, please be prepared for disappointment.

Main Text:

1. Concepts of Modern Physics, 6th ed., by Arthur Beiser, McGraw-Hill.

- 2. Modern Physics, 2nd ed., by Kenneth Krane, John. Wiley & Sons.
- 3. Modern Physics, 3rd ed., by Serway, Moses and Moyer, Thomson 2005.
- 4. Understanding Physics, by Karen Cummings et. al., John Wiley and Sons,

2004 (used for special theory of relativity only).

Others references:

Advanced texts for hard-core physics enthusiasts:

- Introduction to special relativity, by Robert Resnick, John Wiley & sons (readable and well explained, suggested for enthusiasts).
- Quantum Physics of Atoms, Molecules, Solids, Nuclei, and Particles by Robert Eisberg, Robert Resnick, John Wiley & Sons; 2nd edition

Suggestion for the pleasure of understanding (not totally useful for exam but precious for intellectual pursuit)

- Relativity: The Special and the General Theory. Dover Publications (2001). A classic book by the creator himself, Einstein, for a clear explanation that everyone can understand. Minimum equations.
- The Feynman Lecture on Physics Volume III, by Richard Feynman, Addison Wesley Longman (June, 1970). (Read how Feynman expounds excellently on the basics of quantum mechanics.)

Tutorial Classes

The 50 min time slot on Friday is reserved for tutorial discussion. During the tutorial session the class will still meet in the lecture hall and no separate 'tutorial classes' will be arranged. The lecturer in charged (Yoon) will conduct the tutorial class himself.

A total of 5 problem sets will be prepared for you. Problem sets are an integral part of this course. It simply isn't enough to learn physics unless you sit down and work through the problems and concepts on your own. Formally there will be some assigned tutors to provide guidance and counseling to the students on the subject. However, it is recognized that students also learn a great deal from talking to and working with each other. Therefore I encourage each student to make his/her own attempt on every problem. Discussion among yourselves shall definitely help a lot in understanding the course content more thoroughly. Our typical Malaysian students are used to spoon-feeding. As a matter of fact I am strongly disapproved of such unhealthy attitude. To encourage proactive and independent learning attitude (and to deprive your privilege to be a copy-cat and a bagger of spoon-

feedings), NO solution sheets shall be provided to you. We will only discuss the solutions on-the-spot during the tutorial meetings.

Please note the following: You shall pass up some selected tutorial answers to your tutor for grading each week (worth 5 marks). Deadline will be specified, and late submission will not be accepted. In order to promote discipline, rejection of late submission will be enforced strictly. Solutions and most updated coursework grades will be accessible in the ZCT 104 website.

Assessment (Exam and coursework)

Grading will be weighted: Coursework will contribute 30 marks, while final exam 70 marks, totaling (30 + 70 = 100) marks. Please be noted that the coursework assessment and final exam will be the same for both classes.

Coursework assessment (total 30 marks):

(1) 2 common tests to be conducted on some selected Saturday mornings. These will be the common tests sat by both of the ZCT 104 A and B classes (10 + 10 = 20 marks).

(2) Each week students shall submit some selected tutorial solutions for grading (5 marks).

(3) Online assignment will be assigned once every week or so. This will be a descriptive type of assignment posed on the course webpage. Students have to submit a 300 words writing online before the deadline (5 marks).

Final Exam (70 marks)

The final exam questions will appear in dual language: English + Malay. This will be a 3-hour exam covering almost everything from the lecture material will be conducted at the end of the semester. The format of the exam is yet to be finalized. Once it is been decided the format will be announced on the course webpage.

Course Materials

Hard copy of lecture notes plus problem sets will be available for sale to students. If you like to view the simulation and colour pages not available in the hard copy version, <u>powerpoint lecture notes</u> are also downloadable on the ZCT 104 (Class A) webpage. Past year questions plus their solutions (tests, final exam and KSCP papers) and problem set are also available.

Other Information

The performance of past year ZCT 104 classes (their exam and coursework grade distribution), as well as the lecturer's comment on these performances, can be accessed via internet. Check this out from the course webpages of the respective academic sessions via www2.fizik.usm.my/tlyoon/teaching/

POWERPOINT LECTURE NOTES SESSI 2007/08 SEMESTER II

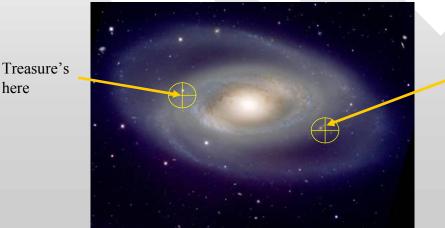
Special theory of Relativity

Notes based on **Understanding Physics** by Karen Cummings et al., John Wiley & Sons



An open-chapter question

- Let say you have found a map revealing a huge galactic treasure at the opposite edge of the Galaxy 200 ly away.
- Is there any chance for you to travel such a distance from Earth • and arrive at the treasure site by traveling on a rocket within your lifetime of say, 60 years, given the constraint that the rocket cannot possibly travel faster than the light speed?



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CHAPTER 2

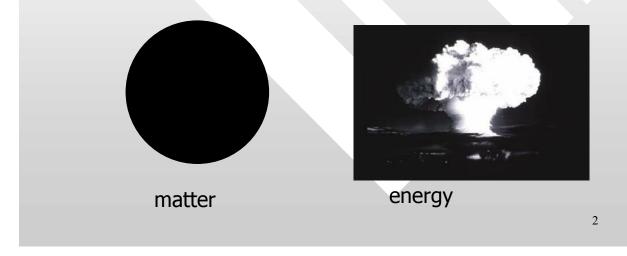
PROPERTIES OF WAVES AND MATTERBLACK BODY RADIATION

Matter, energy and interactions

• One can think that our universe is like a stage existing in the form of space-time as a background

1

• All existence in our universe is in the form of either matter or energy (Recall that matter and energy are `equivalent' as per the equation $E = mc^2$)



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Interactions

- Matter and energy exist in various forms, but they constantly transform from one to another according to the law of physics
- we call the process of transformation from one form of energy/matter to another energy/matter as 'interactions'
- Physics attempts to elucidate the interactions between them
- But before we can study the basic physics of the matter-energy interactions, we must first have some general idea to differentiate between the two different modes of physical existence: matter and wave
- This is the main purpose of this lecture

Matter (particles)

3

4

 m_0

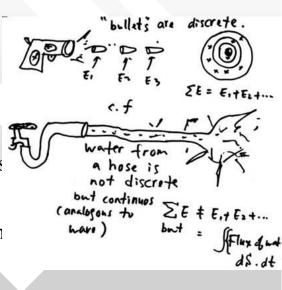
- Consider a particles with mass:
- you should know the following facts since kindergarten.
- A particle is discrete, or in another words, corpuscular, in nature.
- a particle can be localized completely, has mass and electric charge that can be determined with infinite precision (at least in principle)
- So is its momentum
- These are all implicitly assumed in Newtonian mechanics
- This is to be contrasted with energy exists in the forms of wave which is not corpuscular in nature (discuss later)

Energy in particle is corpuscular (discrete) i.e. not spread out all over the place like a continuum The energy carried by a particle is

given by

$$E^2 = m_0^2 c^4 + p^2 c^2$$

- The energy of a particles is concentrated within the boundary of a particle (e,g. in the bullet)
- Hence we say "energy of a particle is corpuscular"
- This is in contrast to the energy carried by the water from the host, in which the energy is distributed spread all over the space in a continuous manner



Example of particles

- Example of `particles': bullet, billiard ball, you and me, stars, sands, etc...
- Atoms, electrons, molecules (or are they?)

What is not a `particle'?

• Waves - electromagnetic radiation (light is a form of electromagnetic radiation), mechanical waves and matter waves is classically thought to not have attributes of particles as mentioned

Analogy

- Imagine energy is like water
- A cup containing water is like a particle that carries some energy within it
- Water is contained within the cup as in energy is contained in a particle.
- The water is not to be found outside the cup because they are all retained inside it. Energy of a particle is corpuscular in the similar sense that they are all inside the carrier which size is a finite volume.
- In contrast, water that is not contained by any container will spill all over the place (such as water in the great ocean). This is the case of the energy carried by wave where energy is not concentrated within a finite volume but is spread throughout the space

Wave

- Three kinds of wave in Nature: mechanical, electromagnetical and matter waves
- The simplest type of wave is strictly sinusoidal and is characterised by a `sharp' frequency ν (= 1/T, T = the period of the wave), wavelength λ and its travelling speed c

$$\lambda \qquad y = A\cos(kx - \omega t)$$

$$C = \lambda v; k = \frac{2\pi}{2}$$
A `pure' (or `plain') wave which has

λ

Quantities that characterise a pure

sharp' wavelength and frequency

 $y = A\cos\left(kx - \omega t\right)$

10

wave

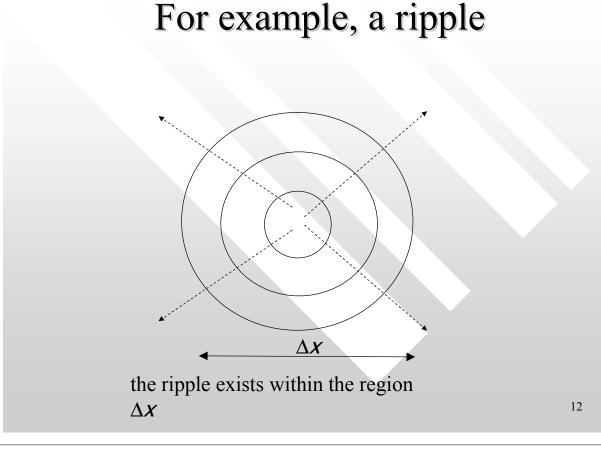
- The quantities that quantify a pure (or called a plane) wave:
 λ, wave length, equivalent to k = 2π/λ, the wave number
 ν=1/T, frequency, equivalent angular frequency,
 ω = 2πν
- c speed of wave, related to the above quantities via

•
$$c = \lambda v = \omega / k$$

 $C = \lambda v$:

- For the case of a particle we can locate its location and momentum precisely
- But how do we 'locate' a wave?
- Wave spreads out in a region of space and is not located in any specific point in space like the case of a particle
- To be more precise we says that a plain wave exists within some region in space, Δx
- For a particle, Δx is just the 'size' of its dimension, e.g. Δx for an apple is 5 cm, located exactly in the middle of a square table, x = 0.5 m from the edges. In principle, we can determine the position of x to infinity
- But for a wave, Δx could be infinity

In fact, for the 'pure' (or 'plain') wave which has 'sharp' wavelength and frequency mentioned in previous slide, the Δx is infinity



A pure wave has $\Delta x \rightarrow$ infinity

- If we know the wavelength and frequency of a pure wave with infinite precision (= the statement that the wave number and frequency are 'sharp'), one can shows that :
- The wave cannot be confined to any restricted region of space but must have an infinite extension along the direction in which it is propagates
- In other words, the wave is 'everywhere' when its wavelength is 'sharp'
- This is what it means by the mathematical statement that " Δx is infinity"

More quantitatively, $\Delta x \Delta \lambda \ge \lambda^2$

• This is the uncertainty relationships for classical waves

 $\Delta\lambda$ is the uncertainty in the wavelength.

- When the wavelength `sharp' (that we knows its value precisely), this would mean $\Delta \lambda = 0$.
- In other words, $\Delta \lambda \rightarrow$ infinity means we are totally ignorant of what the value of the wavelength of the wave is.

 Δx is the uncertainty in the location of the wave (or equivalently, the region where the wave exists)

• $\Delta x = 0$ means that we know exactly where the wave is located, whereas $\Delta x \rightarrow infinity$ means the wave is spread to all the region and we cannot tell where is it's `location'

 $\Delta \lambda \Delta x \ge \lambda^2$ means the more we knows about x, the less we knows about λ as Δx is inversely proportional to $\Delta \lambda$

Other equivalent form

• $\Delta x \Delta \lambda \ge \lambda^2$ can also be expressed in an equivalence form

$\Delta t \Delta \nu \ge 1$

via the relationship $c = v\lambda$ and $\Delta x = c\Delta t$

- Where Δt is the time required to measure the frequency of the wave
- The more we know about the value of the frequency of the wave, the longer the time taken to measure it
- If u want to know exactly the precise value of the frequency, the required time is $\Delta t = infinity$
- We will encounter more of this when we study the Heisenberg uncertainty relation in quantum physics

- The classical wave uncertain relationship $\Delta x \Delta \lambda \ge \lambda^2$
 - can also be expressed in an equivalence form $\Delta t \Delta \nu \geq 1$

via the relationship $c = v\lambda$ and $\Delta x = c\Delta t$

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Wave can be made more ``localised"

- We have already shown that the 1-D plain wave is infinite in extent and can't be properly localised (because for this wave, $\Delta x \rightarrow infinity$)
- However, we can construct a relatively localised wave (i.e., with smaller Δx) by :
- adding up two plain waves of slightly different wavelengths (or equivalently, frequencies)
- Consider the `beat phenomena'

Constructing wave groups • Two pure waves with slight difference in frequency and wave number $\Delta \omega = \omega_1 - \omega_2$, $\Delta k = k_1 - k_2$, are superimposed $y_1 = A\cos(k_1 x - \omega_1 t); \quad y_2 = A\cos(k_2 x - \omega_2 t)$ 180° out Individual waves of phase In phase Envelop wave and phase wave The resultant wave is a 'wave group' comprise of an 'envelop' (or the group wave) and a phase waves $y = y_1 + y_2$ $=2A\cos\frac{1}{2}(\{k_{2}-k_{1}\}x-\{\omega_{2}-\omega_{1}\}t)\cdot\cos\left\{\left(\frac{k_{2}+k_{1}}{2}\right)x-\left(\frac{\omega_{2}+\omega_{1}}{2}\right)t\right\}$ Broad High-frequency wave $2A\cos\left(\frac{\Delta k}{\Omega}x\right)$ $\cos\left(\frac{k_1 + k_2}{2}\right)x$ 20 Av

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- As a comparison to a plain waves, a group wave is more 'localised' (due to the existence of the wave envelop. In comparison, a plain wave has no `envelop' but only `phase wave')
- It comprises of the slow envelop wave

$$2A\cos\frac{1}{2}(\{k_{2}-k_{1}\}x-\{\omega_{2}-\omega_{1}\}t)=2A\cos\frac{1}{2}(\Delta kx-\Delta \omega t)$$

that moves at group velocity $v_g = \Delta \omega / \Delta k$

♦ and the phase waves (individual waves oscillating inside the envelop) $(k_2 + k_1) (\omega_2 + \omega_1)$

$$\left\{\left(\frac{\kappa_{2}+\kappa_{1}}{2}\right)x-\left(\frac{\omega_{2}+\omega_{1}}{2}\right)t\right\}=\cos\left\{k_{p}x-\omega_{p}t\right\}$$

moving at phase velocity $v_p = \omega_p / k_p$

In general, $v_g = \Delta \omega / \Delta k \ll v_p = (\omega_1 + \omega_2) / (k_1 + k_2)$ because ω_2 $\approx \omega_1, k_1 \approx k_2$

$$y = y_1 + y_2 = \left\{ 2A\cos\frac{1}{2}(\Delta kx - \Delta \omega t) \right\} \cdot \cos\left\{k_p x - \omega_p t\right\}$$

'envelop' (group waves). Sometimes it's called 'modulation' Phase waves

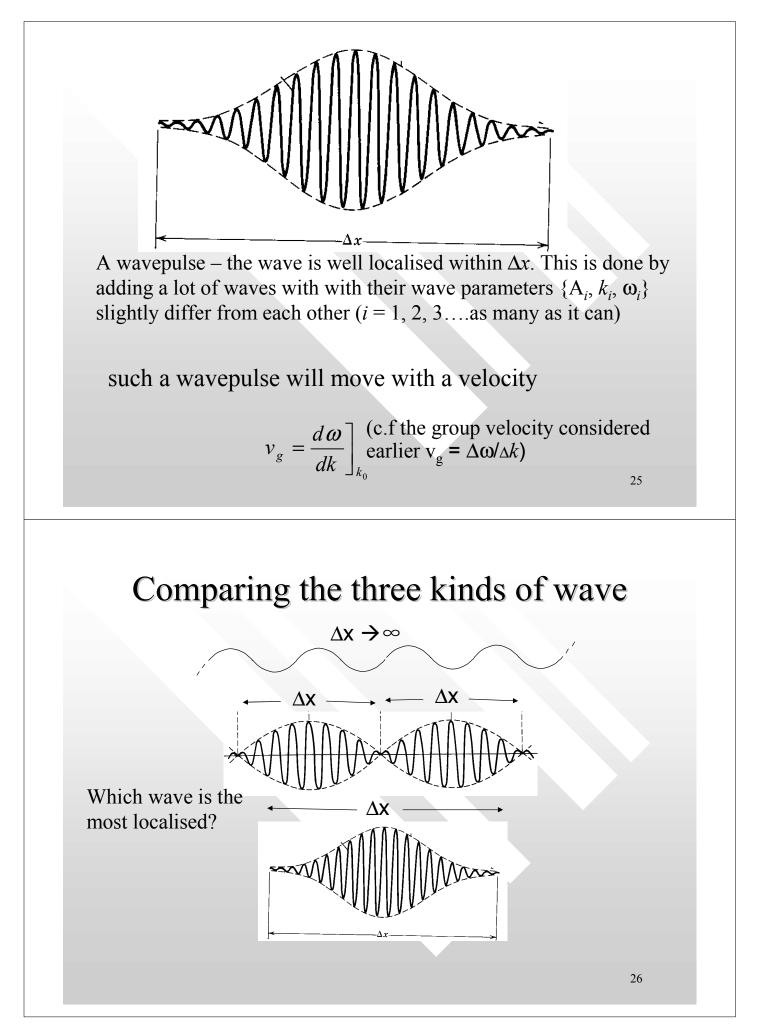
Energy is carried at the speed of the group wave

- The energy carried by the group wave is concentrated in regions in which the amplitude of the envelope is large
- The speed with which the waves' energy is transported through the medium is the speed with which the envelope advances, not the phase wave
- In this sense, the envelop wave is of more 'physical' relevance in comparison to the individual phase waves (as far as energy transportation is concerned)

Wave pulse – an even more `localised' wave 23

- In the previous example, we add up only two slightly different wave to form a train of wave group
- An even more `localised' group wave what we call a "wavepulse "can be constructed by adding more sine waves of different numbers k_i and possibly different amplitudes so that they interfere constructively over a small region Δx and outside this region they interfere destructively so that the resultant field approach zero
- Mathematically,

$$w_{\text{wave pulse}} = \sum_{i} A_{i} \cos \left(k_{i} x - \omega_{i} t \right)$$



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Why are waves and particles so important in physics?

- Waves and particles are important in physics because they represent the only modes of energy transport (interaction) between two points.
- E.g we signal another person with a thrown rock (a particle), a shout (sound waves), a gesture (light waves), a telephone call (electric waves in conductors), or a radio message (electromagnetic waves in space).

Interactions take place between

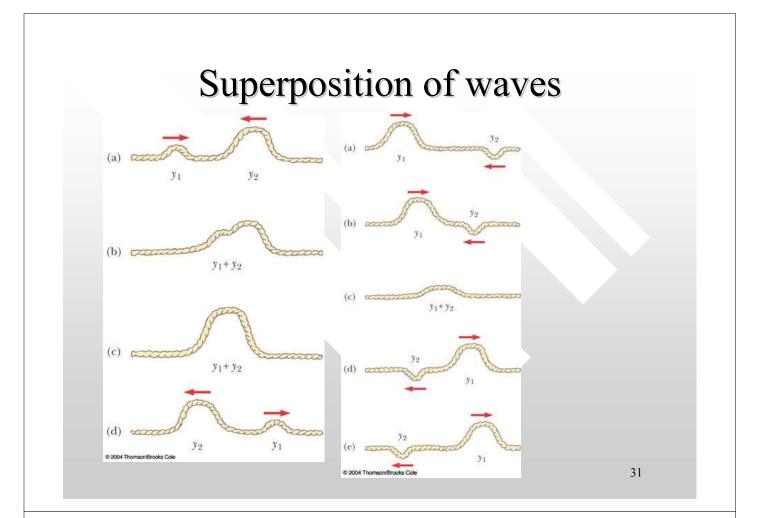
(i) particles and particles (e.g. in particle-particle collision, a girl bangs into a guy) or

(ii) waves and particle, in which a particle gives up all or part of its energy to generate a wave, or when all or part of the energy carried by a wave is absorbed/dissipated by a nearby particle (e.g. a wood chip dropped into water, or an electric charge under acceleration, generates EM wave)

Oscillating electron gives off energy This is an example where particle is interacting with wave; energy transform from the electron's K.E. to the energy propagating in the form of EM wave wave

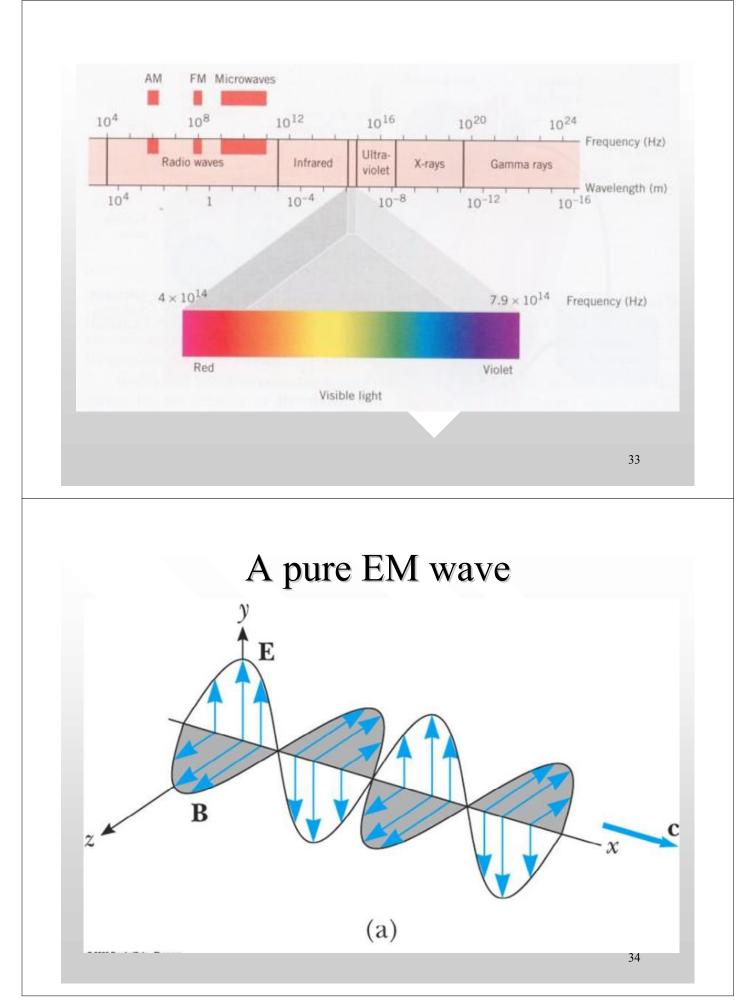
Waves superimpose, not collide

- In contrast, two waves do not interact in the manner as particle-particle or particle-wave do
- Wave and wave simply "**superimpose**": they pass through each other essentially unchanged, and their respective effects at every point in space simply add together according to the principle of superposition to form a resultant at that point -- a sharp contrast with that of two small, impenetrable particles



A pure EM wave

- According to Maxwell theory, light is a form of energy that propagates in the form of electromagnetic wave
- In Maxwell theory light is synonym to electromagnetic radiation is synonym to electromagnetic wave
- Other forms of EM radiation include heat in the form of infra red radiation, visible light, gamma rays, radio waves, microwaves, x-rays



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Heinrich Hertz (1857-1894), German, Established experimentally that light is EM wave



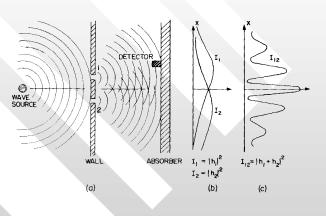
Interference experiment with water

waves

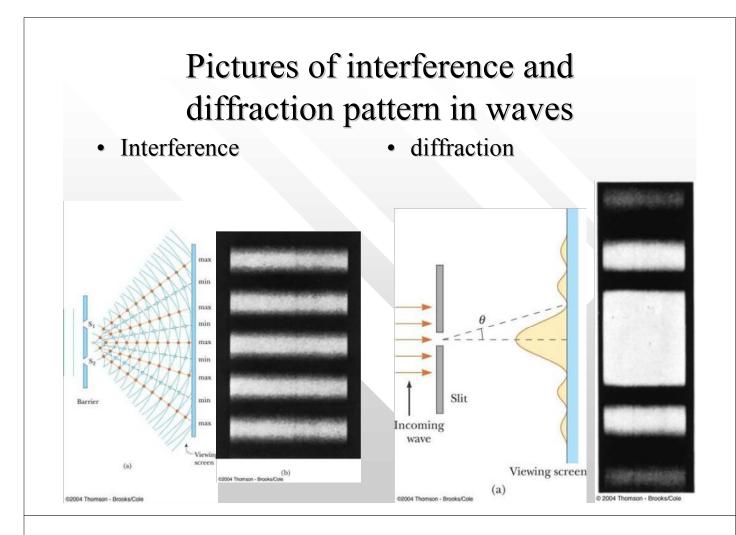
- If hole 1 (2) is block, intensity distribution of (I₁) I₂ is observed
- However, if both holes are opened, the intensity of I_{12} is such that $I_{12} \neq I_1 + I_2$
- Due to the wave nature, the intensities do not simply add
- In addition, and interference term exist,

$$I_{12} = I_1 + I_2 + 2\cos\delta(I_1 + I_2)$$

"waves interfere"



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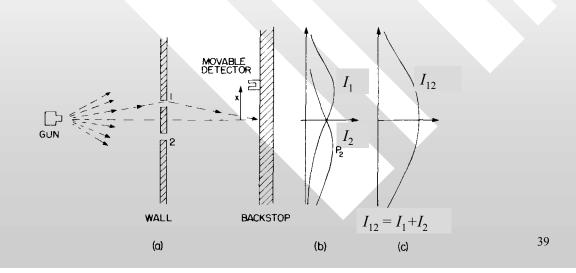


Since light display interference and diffraction pattern, it is wave

- Furthermore, Maxwell theory tell us what kind of wave light is
- It is electromagnetic wave
- (In other words it is not mechanical wave)

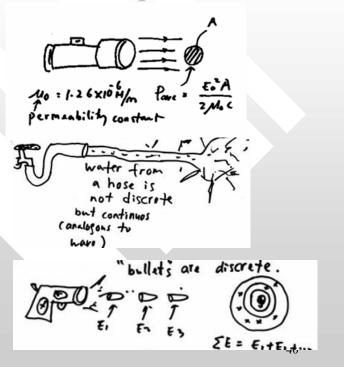
Interference experiment with bullets (particles)

- I_2 , I_1 are distribution of intensity of bullet detected with either one hole covered. I_{12} the distribution of bullets detected when both holes opened
- Experimentally, $I_{12} = I_1 + I_2$ (the individual intensity simply adds when both holes opened)
- Bullets always arrive in identical lump (corpuscular) and display no interference



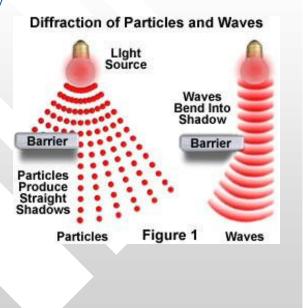
EM radiation transports energy in flux, not in bundles of particles

- The way how wave carries energy is described in terms of 'energy flux', in unit of energy per unit area per unit time
- Think of the continuous energy transported by a stream of water in a hose This is in contrast to a stream of 'bullet' from a machine gun where the energy transported by such a steam is discrete in nature



Essentially,

- Particles and wave are disparately distinct phenomena and are fundamentally different in their physical behaviour
- Free particles only travel in straight line and they don't bend when passing by a corner
- However, for light, it does
- Light, according to Maxwell's EM theory, is EM wave
- It display wave phenomena such as diffraction and interference that is not possible for particles
- Energy of the EM wave is transported in terms of energy flux



BLACK BODY RADIATION

- Object that is HOT (anything > 0 K is considered "hot") emits EM radiation
- For example, an incandescent lamp is red HOT because it emits a lot of EM wave, especially in the IR region



Attempt to understand the origin of radiation from hot bodies from classical theories

- In the early years, around 1888 1900, light is understood to be EM radiation
- Since hot body radiate EM radiation, hence physicists at that time naturally attempted to understand the origin of hot body in terms of classical EM theory and thermodynamics (which has been well established at that time)

- All hot object radiate EM wave of all wavelengths
- However, the energy intensities of the wavelengths differ continuously from wavelength to wavelength (or equivalently, frequency)
- Hence the term: the spectral distribution of energy as a function of wavelength

Spectral distribution of energy in radiation depends only on temperature The distribution of intensity of the emitted radiation from a hot body at a given wavelength depends on the temperature ackbody radiation 80-7000 K 70 6000 K 30 10 4000 K 3000 K 0 400 1000 1200 1400 200 1600 600 800 45 vavelength (nm)

Radiance

- In the measurement of the distribution of intensity of the emitted radiation from a hot body, one measures d*I* where d*I* is the intensity of EM radiation emitted between λ and λ +dλ about a particular wavelength λ.
- Intensity = power per unit area, in unit if Watt per m^2 .
- **Radiance** $R(\lambda, T)$ is defined as per $dI = R(\lambda, T) d\lambda$
- *R*(λ, *T*) is the power radiated per unit area (*intensity*) per unit wavelength interval at a given wavelength λ and a given temperature *T*.
- It's unit could be in Watt per meter square per m or
- W per meter square per nm.

Total radiated power per unit area

• The total power radiated per unit area (intensity) of the BB is given by the integral

$$I(T) = \int_{0}^{\infty} R(\lambda, T) \,\mathrm{d}\lambda$$

• For a blackbody with a total area of *A*, its total power emitted at temperature *T* is

$$P(T) = AI(T)$$

• Note: The SI unit for *P* is Watt, SI unit for *I* is Watt per meter square; for *A*, the SI unit is meter square

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Introducing idealised black body

- In reality the spectral distribution of intensity of radiation of a given body could depend on the type of the surface which may differ in absorption and radiation efficiency (i.e. frequency-dependent)
- This renders the study of the origin of radiation by hot bodies case-dependent (which means no good because the conclusions made based on one body cannot be applicable to other bodies that have different surface absorption characteristics)
- E.g. At the same temperature, the spectral distribution by the exhaust pipe from a Proton GEN2 and a Toyota Altis is different

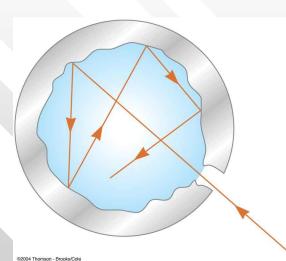
Emmissivity, e

- As a strategy to overcome this non-generality, we introduce an idealised black body which, by definition, absorbs all radiation incident upon it, regardless of frequency
- Such idealised body is universal and allows one to disregard the precise nature of whatever is radiating, since all BB behave identically
- All real surfaces could be approximate to the behavior of a black body via a parameter EMMISSIVITY *e* (*e*=1 means ideally approximated, *e* << 1 means poorly approximated)



Blackbody Approximation

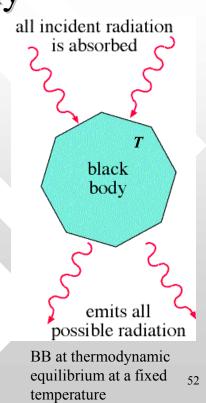
- A good approximation of a black body is a small hole leading to the inside of a hollow object
- The HOLE acts as a perfect absorber
- The Black Body is the HOLE



- Any radiation striking the HOLE enters the cavity, trapped by reflection until is absorbed by the inner walls
- The walls are constantly absorbin and emitting energy at thermal EI/
- The nature of the radiation leaving the cavity through the hole depends only on the temperature of the cavity and not the detail of the surfaces nor frequency of the radiation

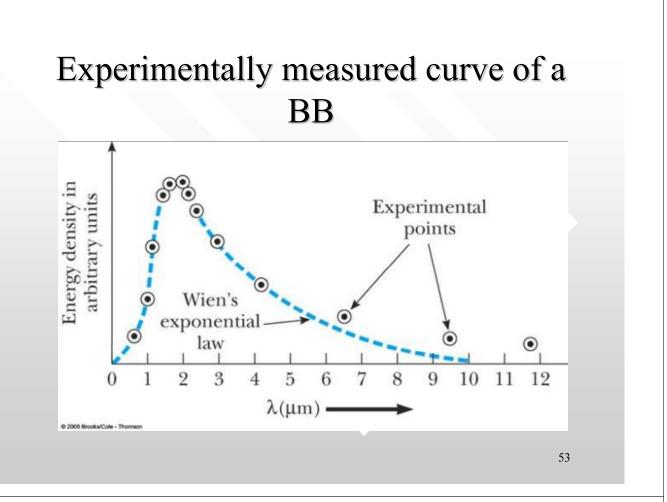
Essentially

- A black body in thermal EB absorbs and emits radiation at the same rate
- The HOLE effectively behave like a Black Body because it effectively absorbs all radiation fall upon it
- And at the same time, it also emits all the absorbed radiations at the same rate as the radiations are absorbed
- The measured spectral distribution of black bodies is universal and depends only on temperature.
- In other words: THE SPECTRAL DISTRIBUTION OF EMISSION DEPENDS SOLELY ON THE TEMPERATURE AND NOT OTHER DETAILS.



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Stefan's Law

- $P = \sigma A e T^4$
 - *P* total power output of a BB
 - A total surface area of a BB
 - σ Stefan-Boltzmann constant $\sigma = 5.670 \times 10^{-8} \text{ W} / \text{m}^2 \cdot \text{K}^4$
- Stefan's law can be written in terms of intensity
 - $I = P/A = \sigma T^4$
 - For a blackbody, where e = 1

Wien's Displacement Law

- $\lambda_{\text{max}}T = 2.898 \text{ x } 10^{-3} \text{ m} \text{K}$
 - λ_{\max} is the wavelength at which the curve peaks
 - *T* is the absolute temperature
- The wavelength at which the intensity peaks, λ_{max} , is inversely proportional to the absolute temperature
 - As the temperature increases, the peak wavelength λ_{\max} is "displaced" to shorter wavelengths.

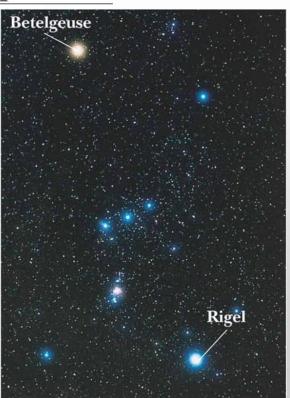
Example

This figure shows two stars in the constellation Orion. Betelgeuse appears to glow red, while Rigel looks blue in color. Which star has a higher surface temperature?

- (a) Betelgeuse
- (b) Rigel

(c) They both have the same surface temperature.

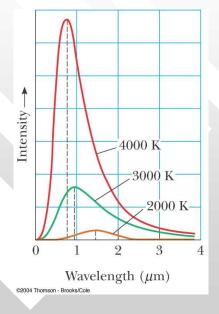
(d) Impossible to determine.



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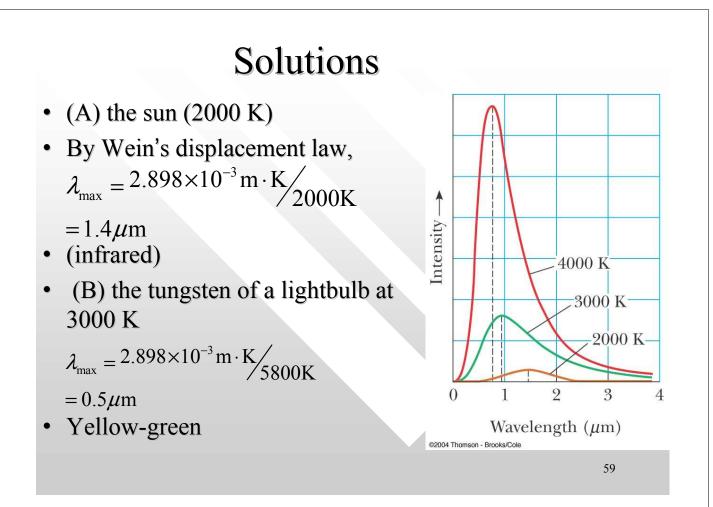
Intensity of Blackbody Radiation, Summary

- The intensity increases with increasing temperature
- The amount of radiation emitted increases with increasing temperature
 - The area under the curve
- The peak wavelength decreases with increasing temperature



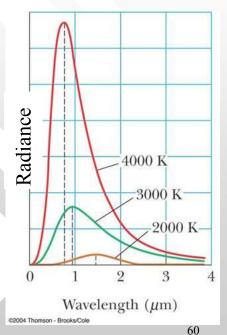
Example

- Find the peak wavelength of the blackbody radiation emitted by
- (A) the Sun (2000 K)
- (B) the tungsten of a light bulb at 3000 K



Why does the spectral distribution of black bodies have the shape as measured?

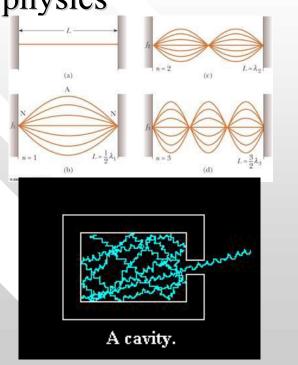
- Lord Rayleigh and James Jeans at 1890's try to theoretically derive the distribution based on statistical mechanics (some kind of generalised thermodynamics) and classical Maxwell theory
- (Details omitted, u will learn this when u study statistical mechanics later)



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RJ's model of BB radiation with classical EM theory and statistical physics

- Consider a cavity at temperature *T* whose walls are considered as perfect reflectors
- The cavity supports many modes of oscillation of the EM field caused by accelerated charges in the cavity walls, resulting in the emission of EM waves at all wavelength
- These EM waves inside the cavity are the BB radiation
- They are considered to be a series of standing EM wave set up within the cavity



Number density of EM standing wave modes in the cavity

The number of independent standing waves G(v)dv in the frequency interval between v and v+dv per unit volume in the cavity is (by applying statistical mechanics)

$$G(v)dv = \frac{8\pi v^2 dv}{c^3}$$

• The next step is to find the average energy per standing wave

The average energy per standing wave, $\langle \mathcal{E} \rangle$

- Theorem of equipartition of energy (a mainstay theorem from statistical mechanics) says that the average energy per standing wave is
- $\langle \mathcal{E} \rangle = kT$

 $k = 1.38 \times 10^{-23}$ J/K, Boltzmann constant

- In classical physics, (e) can take any value CONTINOUSLY and there is not reason to limit it to take only discrete values
- (this is because the temperature T is continuous and not discrete, hence e must also be continuous)₆₃

Energy density in the BB cavity

- Energy density of the radiation inside the BB cavity in the frequency interval between v and v + dv, u(v,T)dv
- = the total energy per unit volume in the cavity in the frequency interval between v and v + dv
- = the number of independent standing waves in the frequency interval between v and v + dv per unit volume, G(v)dv, × the average energy per standing wave.

$$\Rightarrow u(v,T)dv = G(v)dv \times \langle \mathcal{E} \rangle = \frac{8\pi v^2 kTdv}{c^3}$$

Energy density in terms of radiance

• The energy density in the cavity in the frequency interval between v and v + dv can be easily expressed in terms of wavelength, $\lambda \text{ via } c = v\lambda$

$$u(v,T) = \frac{8\pi v^2 kT dv}{c^3} \rightarrow u(\lambda,T) = \frac{8\pi kT}{\lambda^4} d\lambda$$

In experiment we measure the BB in terms of radiance *R*(λ,*T*) which is related to the energy density via a factor of *c*/4:

•
$$R(\lambda,T) = (c/4)u(\lambda,T) = \frac{2\pi ckT}{\lambda^4}$$

Rayleigh-Jeans Law

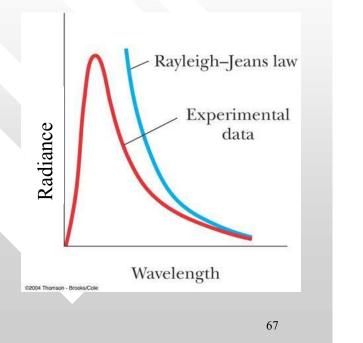
• Rayleigh-Jeans law for the radiance (based on classical physics):

$$R(\lambda,T)=\frac{2\pi ckT}{\lambda^4}$$

• At long wavelengths, the law matched experimental results fairly well

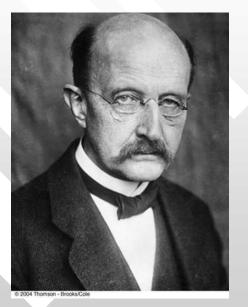
Rayleigh-Jeans Law, cont.

- At short wavelengths, there was a major disagreement between the Rayleigh-Jeans law and experiment
- This mismatch became known as the *ultraviolet catastrophe*
 - You would have infinite energy as the wavelength approaches zero



Max Planck

- Introduced the concept of "quantum of action"
- In 1918 he was awarded the Nobel Prize for the discovery of the quantized nature of energy



Planck's Theory of Blackbody Radiation

- In 1900 Planck developed a theory of blackbody radiation that leads to an equation for the intensity of the radiation
- This equation is in complete agreement with experimental observations

Planck's Wavelength Distribution Function

• Planck generated a theoretical expression for the wavelength distribution (radiance)

$$R(\lambda,T) = \frac{2\pi hc^2}{\lambda^5 \left(e^{hc/\lambda kT} - 1\right)}$$

- $h = 6.626 \text{ x } 10^{-34} \text{ J} \cdot \text{s}$
- *h* is a fundamental constant of nature

Planck's Wavelength Distribution Function, cont.

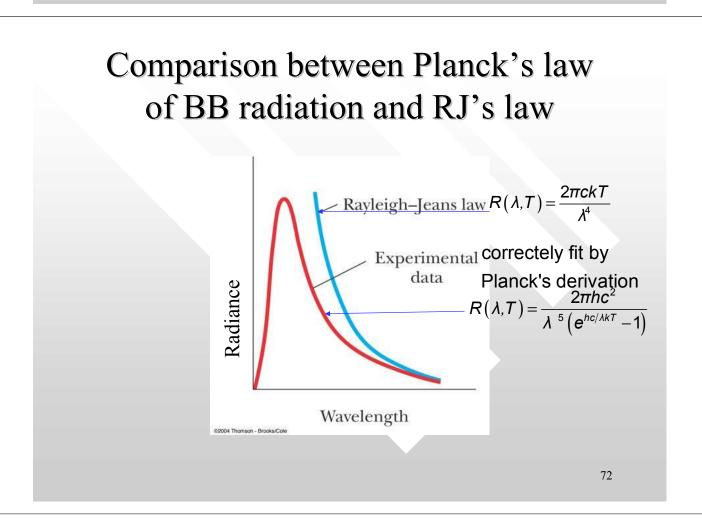
- At long wavelengths, Planck's equation reduces to the Rayleigh-Jeans expression
- This can be shown by expanding the exponential term $b_{2} = 1 (b_{2})^{2}$

$$e^{hc/\lambda kT} = 1 + \frac{hc}{\lambda kT} + \frac{1}{2!} \left(\frac{hc}{\lambda kT}\right)^2 + \dots \approx 1 + \frac{hc}{\lambda kT}$$

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in the long wavelength limit $hc \ll \lambda kT$

- At short wavelengths, it predicts an exponential decrease in intensity with decreasing wavelength
 - This is in agreement with experimental results



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How Planck modeled the BB

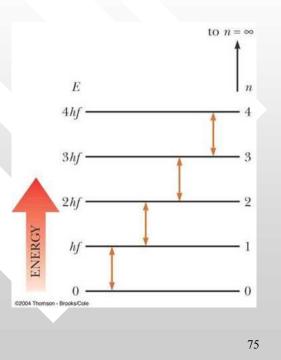
- He assumed the cavity radiation came from atomic oscillations in the cavity walls
- Planck made two assumptions about the nature of the oscillators in the cavity walls

Planck's Assumption, 1

- The energy of an oscillator can have only certain discrete values E_n
 - $E_n = nhf$
 - *n* is a positive integer called the quantum number
 - *h* is Planck's constant = 6.63×10^{-34} Js
 - *f* is the frequency of oscillation
 - This says the energy is **quantized**
 - Each discrete energy value corresponds to a different **quantum state**
 - This is in stark contrast to the case of RJ derivation according to classical theories, in which the energies of oscillators in the cavity must assume a continuous distribution

Energy-Level Diagram of the Planck Oscillator

- An energy-level diagram of the oscillators showing the quantized energy levels and allowed transitions
- Energy is on the vertical axis
- Horizontal lines represent the allowed energy levels of the oscillators
- The double-headed arrows indicate allowed transitions



Oscillator in Planck's theory is quantised in energies (taking only discrete values)

- The energy of an oscillator can have only certain *discrete* values $E_n = nhf$
- The average energy per standing wave in the Planck oscillator is

 $\langle \varepsilon \rangle = \frac{hf}{e^{hf/kT} - 1}$ (instead of $\langle \varepsilon \rangle = kT$ in classical theories)

Planck's Assumption, 2

- The oscillators emit or absorb energy when making a transition from one quantum state to another
 - The entire energy difference between the initial and final states in the transition is emitted or absorbed as a single quantum of radiation
 - An oscillator emits or absorbs energy only when it changes quantum states

Pictorial representation of oscillator transition between states

A quantum of energy *hf* is absorbed or emitted during transition between states

Transition between states

Allowed states of the oscillators

Example: quantised oscillator vs classical oscillator

- A 2.0 kg block is attached to a massless spring that has a force constant *k*=25 N/m. The spring is stretched 0.40 m from its EB position and released.
- (A) Find the total energy of the system and the frequency of oscillation according to classical mechanics.

Solution

- In classical mechanics, $E = \frac{1}{2}kA^2 = \dots 2.0 \text{ J}$
- The frequency of oscillation is

$$f = \frac{1}{2\pi} \sqrt{\frac{k}{m}} = ... = 0.56 \text{ Hz}$$

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(B)

- (B) Assuming that the energy is quantised, find the quantum number *n* for the system oscillating with this amplitude
- Solution: This is a quantum analysis of the oscillator
- $E_n = nhf = n \ (6.63 \text{ x } 10^{-34} \text{ Js})(0.56 \text{ Hz}) = 2.0 \text{ J}$
- $\Rightarrow n = 5.4 \ge 10^{33}$!!! A very large quantum number, typical for macroscopin system

- The previous example illustrated the fact that the quantum of action, *h*, is so tiny that, from macroscopic point of view, the quantisation of the energy level is so tiny that it is almost undetectable.
- Effectively, the energy level of a macroscopic system such as the energy of a harmonic oscillator form a 'continuum' despite it is granular at the quantum scale

"magnified" view of the energy continuum shows discrete energy levels



allowed energies in quantised system – discrete (such as energy levels in an atom, energies carried by a photon)

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allowed energies in classical system – continuous (such as an harmonic oscillator, energy carried by a wave; total mechanical energy of an orbiting planet, etc.)

 $\varepsilon = 0$

- To summarise Classical BB presents a "ultraviolet catastrophe"
- The spectral energy distribution of electromagnetic radiation in a black body CANNOT be explained in terms of classical Maxwell EM theory, in which the average energy in the cavity assumes continuous values of $\langle \varepsilon \rangle = kT$ (this is the result of the wave nature of radiation)
- To solve the BB catastrophe one has to assume that the energy of individual radiation oscillator in the cavity of a BB is quantised as per $E_n = nhf$
- This picture is in conflict with classical physics because in classical physics energy is in principle a continuous variable that can take any value between $0 \rightarrow \infty$
- One is then lead to the revolutionary concept that

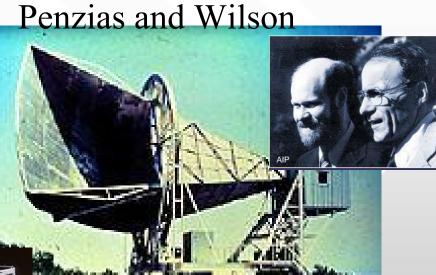
ENERGY OF AN OSCILLATOR IS QUANTISED 84

Cosmic microwave background (CMBR) as perfect black body radiation

1965, cosmic microwave background was first detected by



Nobel Prize 1976



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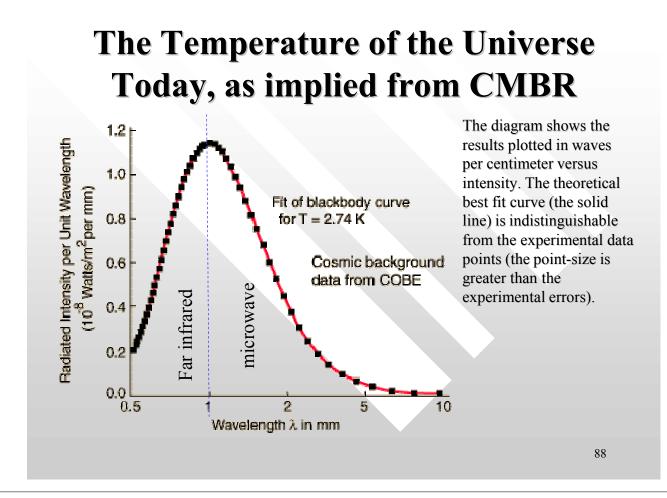


Pigeon Trap Used Penzias and Wilson thought the static their radio antenna was picking up might be due to droppings from pigeons roosting in the antenna horn. They captured the pigeons with this trap and cleaned out the horn, but the static persisted.

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CMBR – the most perfect Black Body

- Measurements of the cosmic microwave background radiation allow us to determine the temperature of the universe today.
- The brightness of the relic radiation is measured as a function of the radio frequency. To an excellent approximation it is described by a thermal of blackbody distribution with a temperature of T=2.735 degrees above absolute zero.
- This is a dramatic and direct confirmation of one of the predictions of the Hot Big Bang model.
- The COBE satellite measured the spectrum of the cosmic microwave background in 1990, showing remarkable agreement between theory and experiment.

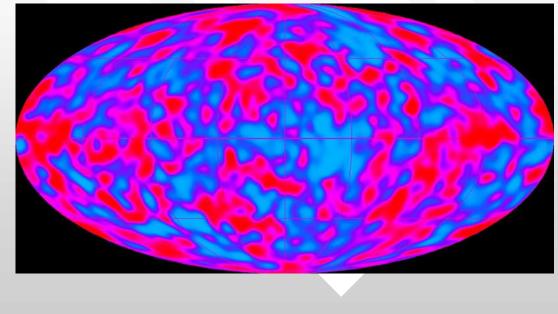


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COBE

- The Cosmic Background Explorer satellite was launched twenty five years after the discovery of the microwave background radiation in 1964.
- In spectacular fashion in 1992, the COBE team announces that they had discovered `ripples at the edge of the universe', that is, the first sign of primordial fluctuations at 100,000 years after the Big Bang.
- These are the imprint of the seeds of galaxy formation.

"Faces of God"



- The "faces of God": a map of temperature variations on the full sky picture that COBE obtained.
- They are at the level of only one part in one hundred thousand.
- Viewed in reverse the Universe is highly uniform in every direction lending strong support for the <u>cosmological principle.</u>

The Nobel Prize in Physics 2006

"for their discovery of the blackbody form and anisotropy of the cosmic microwave background radiation"

John C. Mather

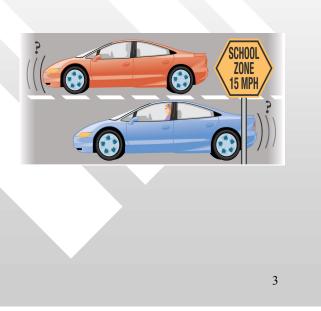




George F. Smoot

Relative motions at ordinary speed

- Relative motion in ordinary life is commonplace
- E.g. the relative motions of two cars (material objects) along a road
- When you observe another car from within your car, can you tell whether you are at rest or in motion if the other car is seen to be "moving?"



Relative motion of wave

- Another example: wave motion
- Speed of wave measured by Observer 1 on wave 2 depends on the speed of wave 1 wrp (with respect) to the shore: $\vec{v} = \vec{v} - \vec{v}$

$$\vec{v}_{1} = \vec{v}_{1} \hat{x}; \qquad \vec{v}_{2} = -\vec{v}_{2} \hat{x}$$

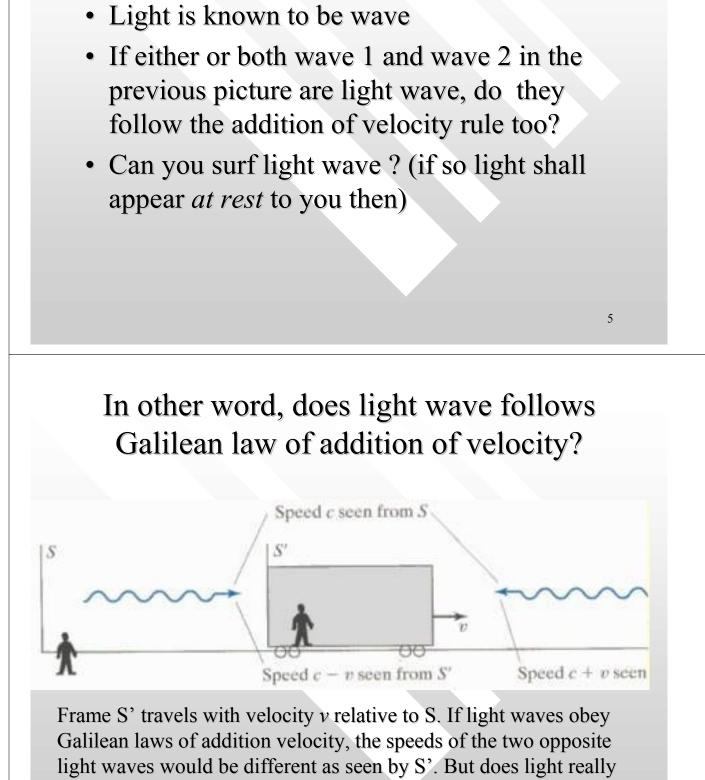
$$\vec{v}_{1} = \vec{v}_{1} \hat{x}; \qquad \vec{v}_{2} = -\vec{v}_{2} \hat{x}$$

$$\vec{v}_{1,2} = \vec{v}_{1} - \vec{v}_{2} = v_{1} \hat{x} - (-v_{2} \hat{x}) = (v_{1} + v_{2}) \hat{x};$$

$$\vec{v}_{2,1} = \vec{v}_{2} - \vec{v}_{1} = (-v_{2} \hat{x}) - (v_{1} \hat{x}) = -(v_{1} + v_{2}) \hat{x} \qquad 4$$

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Query: can we surf light waves?

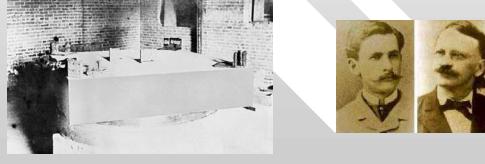


6

obey Galilean law of addition of velocity?

The negative result of Michelson-Morley experiment on Ether

- In the pre-relativity era, light is thought to be propagating in a medium called ether -
- an direct analogy to mechanical wave propagating in elastic medium such as sound wave in air
- If exist, ether could render measurable effect in the apparent speed of light in various direction
- However Michelson-Morley experiment only find negative result on such effect
- A great puzzlement to the contemporary physicist: what does light wave move relative to?



How could we know whether we are at rest or moving?

- Can we cover the windows of our car and carry out experiments inside to tell whether we are at rest or in motion?
- NO



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In a "covered" reference frame, we can't tell whether we are moving or at rest

• Without referring to an external reference object (such as a STOP sign or a lamp post), whatever experiments we conduct in a constantly moving frame of reference (such as a car at rest or a car at constant speed) could not tell us the state of our motion (whether the reference frame is at rest or is moving at constant velocity)

《尚書經.考靈曜》

- 「地恒動不止,而人不知,譬如人在大 舟中,閉牖而坐,舟行而不覺也。」
- "The Earth is at constant state of motion yet men are unaware of it, as in a simile: if one sits in a boat with its windows closed, he would not aware if the boat is moving" in "Shangshu jing", 200 B.C

Physical laws must be invariant in any reference frame

- Such an inability to deduce the state of motion is a consequence of a more general principle:
- There must be no any difference in the physical laws in any reference frame with constant velocity
- (which would otherwise enable one to differentiate the state of motion from experiment conducted in these reference frame)
- Note that a reference frame at rest is a special case of reference frame moving at constant velocity (v = 0 = constant)

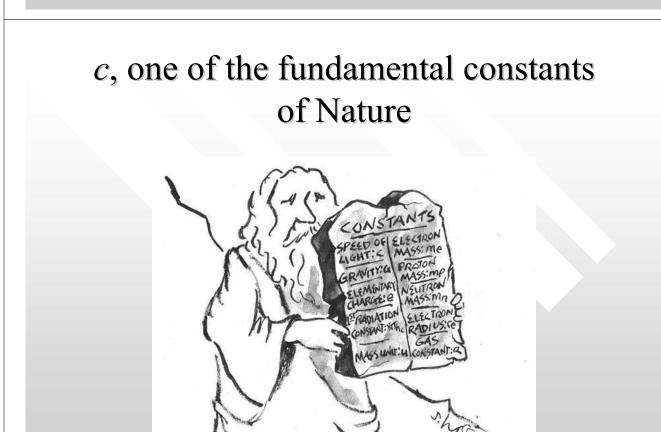
The Principle of Relativity

• All the laws of Physics are the same in every reference frame

Einstein's Puzzler about running fast while holding a mirror



- Says Principle of Relativity: Each fundamental constants must have the same numerical value when measured in any reference frame (c, h, e, m_e, etc)
- (Otherwise the laws of physics would predict inconsistent experimental results in different frame of reference which must not be according to the Principle)
- Light always moves past you with the same speed *c*, no matter how fast you run
- Hence: you will not observe light waves to slow down as you move faster 13



Constancy of the speed of light

Figure 1-2

Two observers in relative motion. O is at rest and O' moves toward O at constant speed u. O and O' agree on the speed of light coming from the source carried by O'.



Observer O'



Observer O

Reading Exercise (RE) 38-2

- While standing beside a railroad track, we are startled by a boxcar traveling past us at half the speed of light. A passenger (shown in the figure) standing at the front of the boxcar fires a laser pulse toward the rear of the boxcar. The pulse is absorbed at the back of the box car. While standing beside the track we measure the speed of the pulse through the open side door.
- (a) Is our measured value of the speed of the pulse greater than, equal to, or less than its speed measured by the rider?
- (b) Is our measurement of the distance between emission and absorption of the light pulse great than, equal to, or less than the distance between emission and absorption measured by the rider?
- (c) What conclusion can you draw about the relation between the times of flight of the light pulse as measured in the two reference frames?



Touchstone Example 38-1: **Communication storm!**

A sunspot emits a tremendous burst of particles that travels toward the Earth. An astronomer on the Earth sees the emission through a solar telescope and issues a warning. The astronomer knows that when the particle pulse arrives it will wreak havoc with broadcast radio transmission. Communications systems require ten minutes to switch from over-the-air broadcast to underground cable transmission. What is the maximum speed of the particle pulse emitted by the Sun such that the switch can occur in time, between warning and arrival of the pulse? Take the sun to be 500 light-seconds distant from the Earth.

Solution

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It takes 500 seconds for the warning light flash to travel the distance of 500 light-seconds between the Sun and the Earth and enter the astronomer's telescope. If the particle pulse moves at half the speed of light, it will take twice as long as light to reach the Earth. If the pulse moves at one-quarter the speed of light, it will take four times as long to make the trip. We generalize this by saying that if the pulse moves with speed v/c, it will take time to make the trip given by the expression:

$$\Delta t_{\rm pulse} = 500 \, {\rm s}/\left(v_{\rm pulse}/c\right)$$

How long a warning time does the Earth astronomer have between arrival of the light flash carrying information about the pulse the arrival of the pulse itself? It takes 500 seconds for the light to arrive. Therefore the warning time is the difference between pulse transit time and the transit time of light:

- $\Delta t_{\text{warning}} = \Delta t_{\text{pulse}} 500 \text{ s.}$ But we know that the minimum possible warning time is 10 min = 600 s.
- Therefore we have
- $600 \text{ s} = 500 \text{ s} / (v_{\text{pulse}}/c) 500 \text{ s},$
- which gives the maximum value for v_{puls} if there is to he sufficient time for warning:

$$_{\rm uls} = 0.455 \ c.$$
 (Answer)

Observation reveals that pulses of particles emitted from the sun travel much slower than this maximum value. So we would have much longer warning 18 time than calculated here.

Relating Events is science

- Science: trying to relate one event to another event
- E.g. how the radiation is related to occurrence of cancer; how lightning is related to electrical activities in the atmosphere etc.
- Since observation of events can be made from different frames of reference (e.g. from an stationary observatory or from a constantly moving train), we must also need to know how to predict events observed in one reference frame will look to an observer in another frame

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Some examples

- How is the time interval measured between two events observed in one frame related to the time interval measured in another frame for the same two events?
- How is the velocity of a moving object measured by a stationary observer and that by a moving observer related?

Defining events

• So, before one can work out the relations between two events, one must first precisely define what an event is

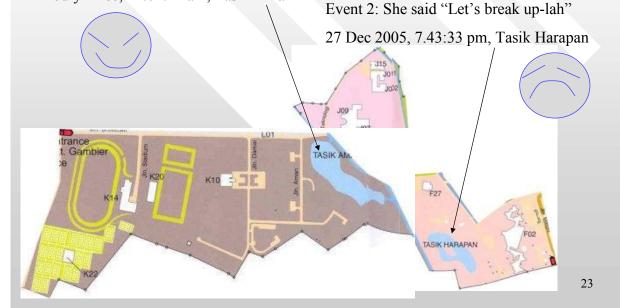
Locating Events

- An event is an occurrence that happens at a unique place and time
- Example: a collision, and explosion, emission of a light flash
- An event must be sufficiently localised in space and time
- e.g. your birthday: you are born in the General Hospital PP at year 1986 1st April 12.00 am)

Example of two real-life events

Event 1: She said "I love you"

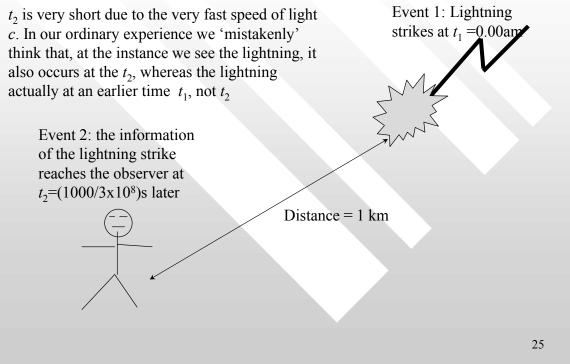
July 1Dec, 12.01:12 am, Tasik Aman



Subtle effect to locate an event: delay due to finiteness of light speed

- In our (erroneous) "common sense" information are assumed to reach us instantaneously as though it is an immediate action through a distance without any delay
- In fact, since light takes finite time to travel, locating events is not always as simple it might seems at first

An illustrative example of delay while measuring an event far away



Reading Exercise 38-4

- When the pulse of protons passes through detector A (next to us), we start our clock from the time t = 0 microseconds. The light flash from detector B (at distance L=30 m away) arrives back at detector A at a time t = 0.225 microsecond later.
- (a) At what time did the pulse arrive at detector B?
- (b) Use the result from part (a) to find the speed at which the proton pulse moved, as a fraction of the speed of light.

Answer

- The time taken for light pulse to travel from B to A is $L/c = 10^{-7}$ s =0.1 μ s
- Therefore the proton pulse arrived detector B $0.225 - 0.1 \ \mu s = 0.125 \ \mu s$ after it passed us at detector A.
- (b) The protons left detector A at t =0 and, according to part (a), arrived at detector B at t = 0.125 μs. Therefore its speed from A to B is L/0.125 μs = ...=0.8c

Redefining Simultaneity

- Hence to locate an event accurately we must take into account the factor of such time delay
- An intelligent observer is an observer who, in an attempt to register the time and spatial location of an event far away, takes into account the effect of the delay factor
- (In our ordinary daily life we are more of an unintelligent observer)
- For an intelligent observer, he have to redefine the notion of "simultaneity" (example 38-2)

Example 38-2: Simultaneity of the Two Towers

Frodo is an intelligent observer standing next to Tower A, which emits a flash of light every 10 s. 100 km distant from him is the tower B, stationary with respect to him, that also emits a light flash every 10 s. Frodo wants to know whether or not each flash is emitted from remote tower B simultaneous with (at the same time as) the flash from Frodo's own Tower A. Explain how to do this with out leaving Frodo position next to Tower A. Be specific and use numerical values.



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Solution

- Frodo is an intelligent observer, which means that he know how to take into account the speed of light in determining the time of a remote event, in this case the time of emission of a flash by the distant Tower B. He measures the time lapse between emission of a flash by his Tower A and his reception of flash from Tower B.
- If this time lapse is just that required for light move from Tower B to Tower A, then the two emissions occur the same time.
- The two Towers are 100 km apart. Call this distance *L*. Then the time *t* for a light flash to move from B to A is
- $t = L/c = 10^5 \text{ m/3} \times 10^8 \text{ m/s} = 0.333 \text{ ms.}$ (ANS)
- If this is the time Frodo records between the flash nearby Tower A and reception of the flash from distant tower then he is justified in saying that the two Towers emit flashes simultaneously in his frame.

One same event can be considered in any frame of reference

- One same event, in principle, can be measured by many separate observers in different (inertial) frames of reference (reference frames that are moving at a constant velocity with respect to each other)
- Example: On the table of a moving train, a cracked pot is dripping water
- The rate of the dripping water can be measured by (1) Ali, who is also in the train, or by (2) Baba who is an observer standing on the ground. Furthermore, you too can imagine (3) ET is also performing the same measurement on the dripping water from Planet Mars. (4) By Darth Veda from Dead Star.³¹

No 'superior' (or preferred) frame

- In other words, any event can be considered in infinitely many different frames of references.
- No particular reference frame is 'superior' than any other
- In the previous example, Ali's frame is in no way superior than Baba's frame, nor ET's frame, despite the fact that the water pot is stationary with respect to Ali.

Transformation laws

- Measurements done by any observers from all frame of reference are equally valid, and are all equivalent.
- Transformation laws such as Lorentz transformation can be used to relate the measurements done in one frame to another.
- In other words, once you know the values of a measurement in one frame, you can calculate the equivalent values as would be measured in other frames.
- In practice, the choice of frame to analyse any event is a matter of convenience.

Example 1

- In the previous example, obviously, the pot is stationary with respect to Ali, but is moving with respect to Baba.
- Ali, who is in the frame of the moving train, measures that the water is dripping at a rate of, say, r_A .
- Baba, who is on the ground, also measures the rate of dripping water, say $r_{\rm B}$.
- Both of the rates measured by Ali and that measured by Baba have equal status you can't say any one of the measurements is 'superior' than the other
- One can use Lorentz transformation to relate r_A with r_B . In reality, we would find that $r_B = r_A / \gamma$ where
- $1/\gamma^2 = 1 (v/c)^2$, with v the speed of the train with respect to ground, and c the speed of light in vacuum.
- Note: $r_{\rm B}$ is not equal to $r_{\rm A}$ (would this contradict your expectation?)

Against conventional wisdom?

- According to SR, r_A and r_B are different in general.
- This should come as a surprise as your *conventional wisdom* (as according to Newtonian view point) may tell you that both r_A and r_B should be equal in their numerical value.
- However, as you will see later, such an assumption is false in the light of SR since the rate of time flow in two frames in relative motion are different
- Both rates, r_A and r_B , despite being different, are correct in their own right.

Example 2

- Consider a stone is thrown into the air making a projectile motion.
- If the trajectory of the stone is considered in the frame of Earth (the so-called Lab frame, in which the ground is made as a stationary reference), the trajectory of the stone is a parabolic curve.
- The trajectory of the stone can also be analysed in a moving frame traveling at velocity v_x along the same horizontal direction as the stone. In this frame (the so-called rocket frame), the trajectory of the stone is not a parabolic curve but a vertical line.

View from different frames In the Rocket frame, • In the Lab frame, the • the pilot sees the observer on the projectile to follow a ground sees a vertically straight line parabolic trajectory downwards rajectory 37

Transformation law for the coordinates In rocket frame

In Lab frame

•
$$y = -(gt^2)/2 + H$$

•
$$y' = -(gt^2)/2$$

38

•
$$x'=0$$

• $x = v_x t$ • Transformation law relating the coordinates of projectile in both frames is

•
$$y' = y - H$$
, $x' = x - v_x t$

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Time dilation as direct consequence of constancy of light speed

- According to the Principle of Relativity, the speed of light is invariant (i.e. it has the same value) in every reference frame (constancy of light speed)
- A direct consequence of the constancy of the speed of light is time stretching
- Also called time dilation
- Time between two events can have different values as measured in lab frame and rocket frames in relative motion
- "Moving clock runs slow"

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Experimental verification of time stretching with pions

- Pion's half life $t_{\frac{1}{2}}$ is 18 ns.
- Meaning: If N_0 of them is at rest in the beginning, after 18 ns, $N_0/2$ will decay
- Hence, by measuring the number of pion as a function of time allows us to deduce its half life
- Consider now N_0 of them travel at roughly the speed of light *c*, the distance these pions travel after $t_{\frac{1}{2}}=18$ ns would be $ct_{\frac{1}{2}}\approx5.4$ m.
- Hence, if we measure the number of these pions at a distance 5.4 m away, we expect that $N_0/2$ of them will survive
- However, experimentally, the number survived at 5.4m is much greater than expected
- The flying poins travel tens of meters before half of them decay
- How do you explain this? the half life of these pions seems to have been stretched to a larger value!
- Conclusion: in our lab frame the time for half of the pions to decay is much greater than it is in the rest frame of the pions!

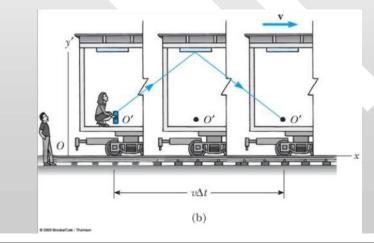
RE 38-5

- Suppose that a beam of pions moves so fast that at 25 meters from the target in the laboratory frame exactly half of the original number remain undecayed. As an experimenter, you want to put more distance between the target and your detectors. You are satisfied to have one-eighth of the initial number of pions remaining when they reach your detectors. How far can you place your detectors from the target?
- ANS: 75 m

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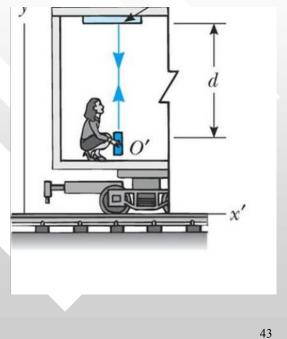
- A Gedanken Experiment Since light speed c is invariant (i.e. the same in all frames), it is suitable to be used as a clock to measure time and space
- Use light and mirror as clock light clock
- A mirror is fixed to a moving vehicle, and a light pulse leaves O' at rest in the vehicle. O' is the rocket frame.
- Relative to a lab frame observer on Earth, the mirror and O' move with a speed v.



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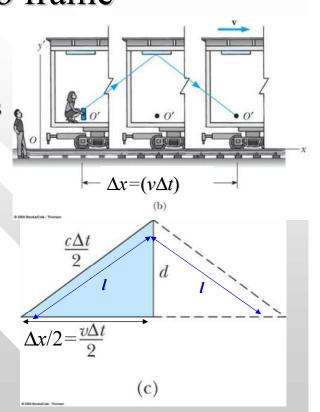
In the rocket frame

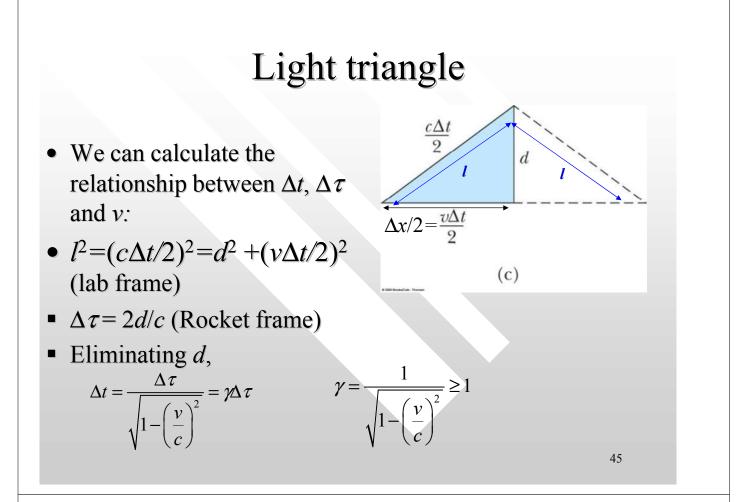
- The light pulse is observed to be moving in the vertical direction only
- The distance the light pulse traversed is 2*d*
- The total time travel by the light pulse to the top, get reflected and then return to the source is $\Delta \tau = 2d/c$



In the lab frame

- However, O in the lab frame observes a different path taken by the light pulse – it's a triangle instead of a vertical straight line
- The total light path is longer = 2*l*
- $l^2 = (c\Delta t/2)^2$ = $d^2 + (\Delta x/2)^2$ = $d^2 + (v\Delta t/2)^2$





Time dilation equation

• Time dilation equation $\Delta t = \frac{\Delta \tau}{\sqrt{1 - \left(\frac{v}{2}\right)^2}} = \gamma \Delta \tau$

- Gives the value of time $\Delta \tau$ between two events occur at time Δt apart in some reference frame
- Lorentz factor $\gamma = \frac{1}{\sqrt{1 \left(\frac{v}{r}\right)^2}} \ge 1$
- Note that as $v \ll c, \gamma \approx 1$; as $v \rightarrow c, \gamma \rightarrow \infty$
- Appears frequently in SR as a measure of relativistic effect: $\gamma \approx 1$ means little SR effect; $\gamma >>$ 1 is the ultra-relativistic regime where SR is most pronounce

RE 38-6

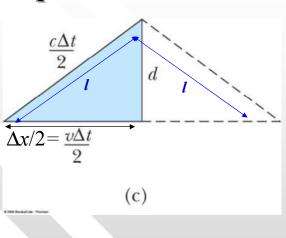
• A set of clocks is assembled in a stationary boxcar. They include a quartz wristwatch, a balance wheel alarm clock, a pendulum grandfather clock, a cesium atomic clock, fruit flies with average individual lifetimes of 2.3 days. A clock based on radioactive decay of nuclei, and a clock timed by marbles rolling down a track. The clocks are adjusted to run at the same rate as one another. The boxcar is then gently accelerated along a smooth horizontal track to a final velocity of 300 km/hr. At this constant final speed, which clocks will run at a different rate from the others as measured in that moving boxcar?

The Metric Equation

- From the light triangle in lab frame and the vertical light pulse in the rocket frame:
- $l^2 = (c\Delta t/2)^2 = d^2 + (\Delta x/2)^2;$
- $d = c\Delta \tau/2$

 $\Rightarrow (c\Delta t/2)^2 = (c\Delta \tau/2)^2 + (\Delta x/2)^2$

• Putting the terms that refer to the lab frame are on the right: $(c\Delta \tau)^2 = (c\Delta t)^2 - (\Delta x)^2$



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"the invariant space-time interval"

- We call the RHS, $s^2 \equiv (c\Delta t)^2 \cdot (\Delta x)^2$ "invariant space-time interval squared" (or sometimes simply "the space-time interval")
- In words, the space-time interval reads:
- $s^2 = (c \times \text{time interval between two events as observed in the frame})^2$ (distance interval between the two events as observed in the frame)^2
- We can always calculate the space-time intervals for any pairs of events
- The interval squared s^2 is said to be an *invariant* because it has the same value as calculated by all observers (take the simile of the mass-to-high² ratio)
- Obviously, in the light-clock gadanken experiment, the space-time interval of the two light pulse events $s^2 \equiv (c\Delta t)^2 (\Delta x)^2 = (c\Delta \tau)^2$ is positive because $(c\Delta \tau)^2 > 0$
- The space-time interval for such two events being positive is deeply related to the fact that such pair of events are causally related
- The space-time interval of such event pairs is said to be '*time-like*' (because the time component in the interval is larger in magnitude than the spatial component)
- Not all pairs of events has a positive space-time interval
- Pairs of events with a negative value of space-time interval is said to be $_{49}$ "space-like", and these pairs of event cannot be related via any causal relation

RE 38-8

- Points on the surfaces of the Earth and the Moon that face each other are separated by a distance of 3.76×10^8 m.
- (a) How long does it take light to travel between these points?
- A firecraker explodes at each of these two points; the time between these explosion is one second.
- (b) What is the invariant space-time interval for these two events?
- Is it possible that one of these explosions caused the other explosion?

Solution

(a) Time taken is t = L / c = 3.76×10⁸ m/ 3×10⁸ m/s = 1.25 s
(b) s²= (ct)² - L² = (3×10⁸ m/s × 1.25 s)² -(3.76×10⁸ m)² = -7.51 m² (space-like interval)
(c) It is known that the two events are separated by only 1 s.

(c) It is known that the two events are separated by only 1 s.
 Since it takes 1.25 s for light to travel between these point, it is impossible that one explosion is caused by the other, given that no information can travel fast than the speed of light.
 Alternatively, from (b), these events are separated by a space-

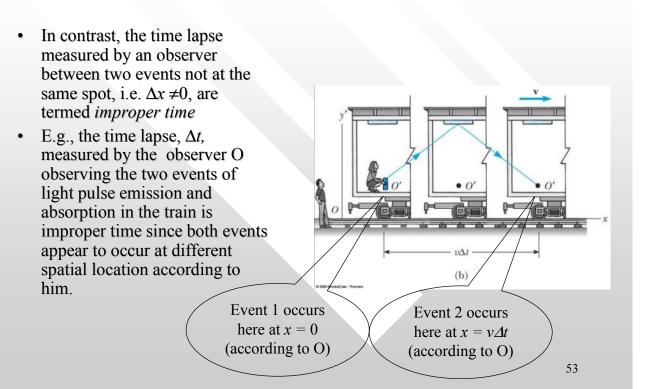
like space-time interval. Hence it is impossible that the two explosions have any causal relation

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Proper time

- Imagine you are in the rocket frame, O', observing two events taking place at the same spot, separated by a time interval Δτ (such as the emission of the light pulse from source (EV1), and re-absorption of it by the source again, (EV2))
- Since both events are measured on the same spot, they appeared at rest wrp to you
- The time lapse Δτ between the events measured on the clock at rest is called the proper time or wristwatch time (one's own time)

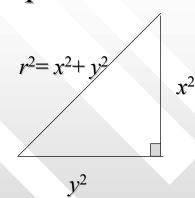
Improper time



Space and time are combined by the metric equation: Space-time

 $s^2 \equiv (c\Delta t)^2 - (\Delta x)^2 =$ invariant= $(\Delta \tau)^2$

- The metric equation says $(c\Delta t)^2 - (\Delta x)^2 = \text{invariant}$ $= (c\Delta \tau)^2 \text{ in all frames}$
- It combines space and time in a single expression on the RHS!!
- Meaning: Time and space are interwoven in a fabric of space-time, and is not independent from each other anymore (we used to think so in Newton's absolute space and absolute time system)



The space-time invariant is the 1+1 dimension Minkowsky space-time

analogous to the 3-D Pythagoras theorem with the hypotenuse $r^{2}=x^{2}+y^{2}$. However, in the Minkowsky space-time metric, the space and time components differ by an relative minus sign 54

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*s*² relates two different measures of time between the *same* two

events

 $s^2 \equiv (c\Delta t)^2 - (\Delta x)^2 = \text{invariant} = (c\Delta \tau)^2$

- (1) the time recorded on clocks in the reference frame in which the events occur at different places (improper time, Δt), and
- (2) the wristwatch time read on the clock carried by a traveler who records the two events as occurring a the same place (proper time, Δτ)
- In different frames, Δt and Δx measured for the same two events will yield different values in general. However, the interval squared, $(c\Delta t)^2 \cdot (\Delta x)^2$ will always give the same value, see example that ensues

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Example of calculation of spacetime interval squared

- In the light-clock gedanken experiment: For O', he observes the proper time interval of the two light pulse events to be $\Delta \tau$. For him, $\Delta x' = 0$ since these events occur at the same place
- Hence, for O',
- s² = (c×time interval observed in the frame)² (distance interval observed in the frame)²

•
$$= (c\Delta \tau)^2 - (\Delta x')^2 = (c\Delta \tau)^2$$

• For O, the time-like interval for the two events is $s^2 = (c\Delta t)^2 - (\Delta x)^2 = (c\gamma\Delta \tau)^2 - (v\Delta t)^2 = (c\gamma\Delta \tau)^2 - (v\gamma\Delta \tau)^2 = \gamma^2 (c^2 - v^2)\Delta \tau^2 = c^2\Delta \tau^2 = s'^2$

What happens at high and low speed

$$\Delta t = \gamma \Delta \tau, \quad \gamma = \frac{1}{\sqrt{1 - \left(\frac{v}{c}\right)^2}} \ge 1$$

- At low speed, $v \ll c$, $\gamma \approx 1$, and $\Delta \tau \approx \Delta t$, not much different, and we can't feel their difference in practice
- However, at high speed, proper time interval $(\Delta \tau)$ becomes much <u>SMALLER</u> than improper time interval (Δt) in comparison, i.e. $\Delta \tau = \Delta t/\gamma \ll \Delta t$
- Imagine this: to an observer on the Earth frame, the person in a rocket frame traveling near the light speed appears to be in a 'slow motion' mode. This is because, according to the Earth observer, the rate of time flow in the rocket frame appear to be slower as compared to the Earth's frame rate of time flow.
- A journey that takes, say, 10 years to complete, according to a traveler on board (this is his proper time), looks like as if they take 10γ yr according to Earth observers.

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Space travel with time-dilation

- A spaceship traveling at speed v = 0.995c is sent to planet 100 light-year away from Earth
- How long will it takes, according to a Earth's observer?
- $\Delta t = 100 \text{ ly}/0.995c = 100.05 \text{ yr}$
- But, due to time-dilation effect, according to the traveler on board, the time taken is only

 $\Delta \tau = \Delta t / \gamma = \Delta t \sqrt{(1-0.995^2)} = 9.992$ yr, not 100.05 yr as the Earthlings think

• So it is still possible to travel a very far distance within one's lifetime ($\Delta \tau \approx 50$ yr) as long as γ (or equivalently, v) is large enough

Nature's Speed Limit

- Imagine one in the lab measures the speed of a rocket v to be larger than c. $\sqrt{(v)^2}$
- As a consequence, according to $\Delta \tau = \Delta t \sqrt{1 \left(\frac{v}{c}\right)^2}$
- The proper time interval measurement $\Delta \tau$ in the rocket frame would be proportional to an imaginary number, $i = \sqrt{(-1)}$
- This is unphysical (and impossible) as no real time can be proportional to an imaginary number
- Conclusion: no object can be accelerated to a speed greater than the speed of light in vacuum, *c*
- Or more generally, no information can propagate faster than the light speed in vacuum, *c*
- Such limit is the consequence required by the logical consistency of SR

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Time dilation in ancient legend

- 天上方一日,人间已十年
- One day in the heaven, ten years in the human plane

RE 38-7

- Find the rocket speed v at which the time $\Delta \tau$ between ticks on the rocket is recorded by the lab clock as $\Delta t = 1.01 \Delta \tau$
- Ans: $\gamma = 1.01$, i.e. $(\nu/c)^2 = 1 1/\gamma^2 = ...$
- Solve for v in terms of $c: v = \dots$

Satellite Clock Runs Slow?

- An Earth satellite in circular orbit just above the atmosphere circles the Earth once every T = 90 min. Take the radius of this orbit to be r = 6500 kilometers from the center of the Earth. How long a time will elapse before the reading on the satellite clock and the reading on a clock on the Earth's surface differ by one microsecond?
- For purposes of this approximate analysis, assume that the Earth does not rotate and ignore gravitational effects due the difference in altitude between the two clocks (gravitational effects described by general relativity).

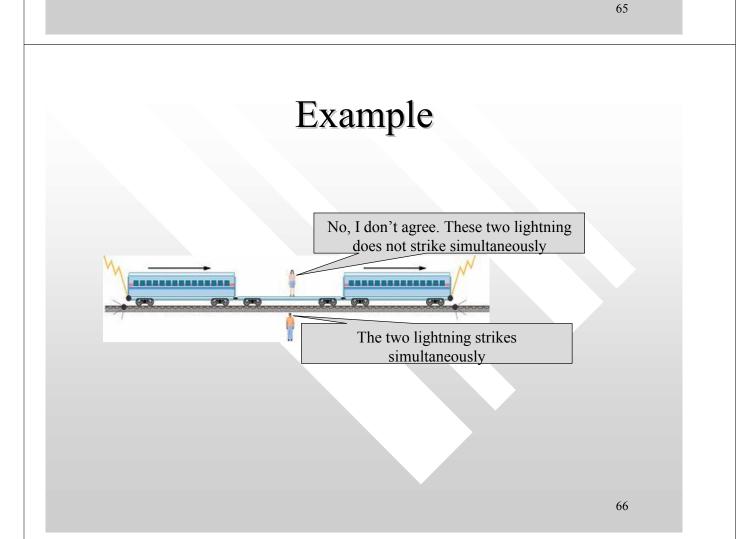
Solution

- First we need to know the speed of the satellite in orbit. From the radius of the orbit we compute the circumference and divide by the time needed to cover that circumference:
- $v = 2\pi r/T = (2\pi \times 6500 \text{ km})/(90 \times 60 \text{ s}) = 7.56 \text{ km/s}$
- Light speed is almost exactly $c = 3 \times 10^5$ km/s. so the satellite moves at the fraction of the speed of light given by
- $(v/c)^2 = [(7.56 \text{ km/s})/(3 \times 10^5 \text{ km/s})]^2 = (2.52 \times 10^5)^2 = 6.35 \times 10^{-10}.$
- The relation between the time lapse $\Delta \tau$ recorded on the satellite clock and the time lapse Δt on the clock on Earth (ignoring the Earth's rotation and gravitational effects) is given by
- $\Delta \tau = (1 (v/c)^2)^{1/2} \Delta t$
- We want to know the difference between Δt and $\Delta \tau$ i.e. $\Delta t \Delta \tau$.
- We are asked to find the elapsed time for which the satellite clock and the Earth clock differ in their reading by one microsecond, i.e. $\Delta t \Delta \tau = 1 \mu s$
- Rearrange the above equation to read $\Delta t^2 \Delta \tau^2 = (\Delta t + \Delta \tau)(\Delta t \Delta \tau)$, one shall arrive at the relation that $\Delta t = [1+(1-(v/c)^2)^{1/2}](1\mu s) / (v/c)^2 \approx 3140s$
- This is approximately one hour. A difference of one microsecond between atomic clock is easily detectable.



Disagreement on simultaneity

Two events that are simultaneous in one frame are not necessarily simultaneous in a second frame in uniform relative motion

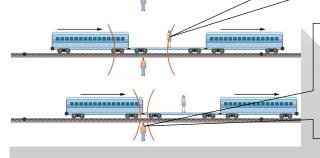


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Einstein Train illustration

• Lightning strikes the front and back of a moving train, leaving char marks on both track and train. Each emitted flash spreads out in all directions.

I am equidistant from the front and back char marks on the train. Light has the standard speed in my frame, and equal speed in both direction. The flash from the front of the train arrived first, therefore the flash must have left the front of the train first. The front lightning bolt fell first before the rear light bolt fell. I conclude that the two strokes are not simultaneous.



I stand by the tracks halfway between the char marks on the track. The flashes from the strokes reach me a the same time and I am equidistance from the char marks on the track. I conclude that two events were simultaneous

Why?

• This is due to the invariance of the space-time invariant in all frames, (i.e. the invariant must have the same value for all frames)

How invariance of space-time interval explains disagreement on simultaneity by two observers

- Consider a pair of events with space-time interval $s^2 = (c\Delta t)^2 (\Delta x)^2 = (c\Delta t')^2 (\Delta x')^2$
- where the primed and un-primed notation refer to space and time coordinates of two frames at relative motion (lets call them O and O')
- Say O observes two simultaneous event in his frame (i.e. $\Delta t = 0$) and are separate by a distance of (Δx) , hence the space-time interval is $s^2 = -(\Delta x)^2$
- The space-time interval for the same two events observed in another frame, O', $s^2 = (c\Delta t')^2 - (\Delta x')^2$ must read the same, as - $(\Delta x)^2$
- Hence, $(c\Delta t')^2 = (\Delta x')^2 (\Delta x)^2$ which may not be zero on the RHS. i.e. $\Delta t'$ is generally not zero. This means in frame O', these events are not observed to be occurring simultaneously ⁶⁹

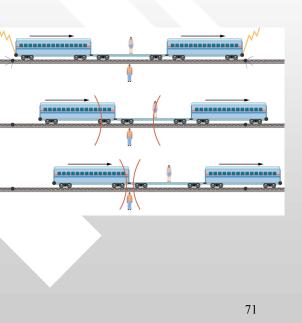
Simulation of disagreement on simultaneity by two observers (be aware that this simulation simulates the scenario in which the lady in the moving car sees simultaneity whereas the observer on the ground disagrees)



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RE 38-9

- Susan, the rider on the train pictured in the figure is carrying an audio tape player. When she received the light flash from the front of the train she switches on the tape player, which plays very loud music. When she receives the light flash from the back end of the train, Susan switches off the tape player. Will Sam, the observers on the ground be able to hear the music?
- Later Susan and Sam meet for coffee ' and examine the tape player. Will they agree that some tape has been wound from one spool to the other?
- The answer is: ...



Solution

- Music has been emitted from the tape player. This is a fact that must be true in both frames of reference. Hence Sam on the ground will be able to hear the music (albeit with some distortion).
- When the meet for coffee, they will both agree that some tape has been wound from one spool to the other in the tape recorder.

Touchstone Example 38-5: Principle

- of Relativity Applied Divide the following items into two lists, On one list, labeled SAME, place items that name properties and laws that are always the same in every frame. On the second list, labeled MAY BE DIF FERENT. place items that name properties that can be different in different frames:
- a. the time between two given events •
- b. the distance between two given events •
- c. the numerical value of Planck's constant h •
- d. the numerical value of the speed of light c •
- e. the numerical value of the charge e on the electron •
- f. the mass of an electron (measured at rest) •
- g. the elapsed time on the wristwatch of a person moving between two given • events
- h. the order ot elements in the periodic table
- i. Newton's First Law of Motion ("A particle initially at rest remains at rest, • and ...")
- j. Maxwell's equations that describe electromagnetic fields in a vacuum
- k. the distance between two simultaneous events

Solution

THE SAME IN ALL FRAMES

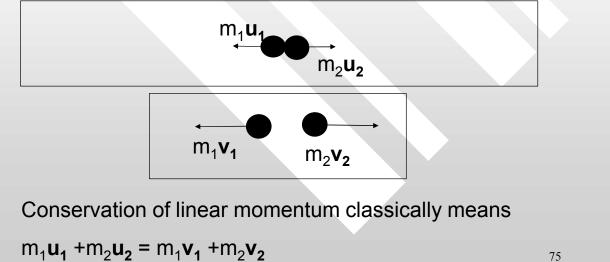
- c. numerical value of h
- d. numerical value of c
- e. numerical value of e
- f. mass of electron (at rest)
- g. wristwatch time between two event (this is the proper time interval between two event)
- h. order of elements in the periodic table
- i. Newton's First Law of Motion
- j. Maxwell's equations
- k distance between two simultaneous events

MAY BE DIFFERENT IN DIFFERENT FRAMES

- a. time between two given events
- b. distance between two give events

Relativistic Dynamics

- Where does $E = mc^2$ comes from?
- By Einstein's postulate, the observational law of linear momentum must also hold true in all frames of reference



Classical definition of linear

momentum

- Classically, one defines linear momentum as mass × velocity
- Consider, in a particular reference frame where the object with a mass m_0 is moving with velocity v, then the momentum is defined (according to classical mechanics) as

$$p = m_0 v.$$

- If v = 0, the mass m_0 is called the rest mass.
- Similarly, in the other frame, (say the O' frame), p' = m'v'
- According to Newton's mechanics, the mass m' (as seen in frame O') is the same as the mass m₀ (as seen in O frame). There is no distinction between the two.
- In particular, there is no distinction between the rest mass and the₇₆ 'moving mass'

Modification of expression of linear momentum

- However, simple analysis will reveal that in order to preserve the consistency between conservation of momentum and the Lorentz Transformation (to be discussed later), the definition of momentum has to be modified to
 - momentum = $\gamma m_0 v$
- where m_0 is the rest mass (an invariant quantity).
- A popular interpretation of the above re-definition of linear momentum holds that the mass of an moving object, m, is different from its value when it's at rest, m_0 , by a factor of γ , i.e

• $m = \gamma m_0$

• (however some physicists argue that this is actually not a correct interpretation. For more details, see the article by Okun posted on the course webpage. In any case, for pedagogical reason, we will stick to the "popular interpretation" of the "relativistic mass")

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In other words...

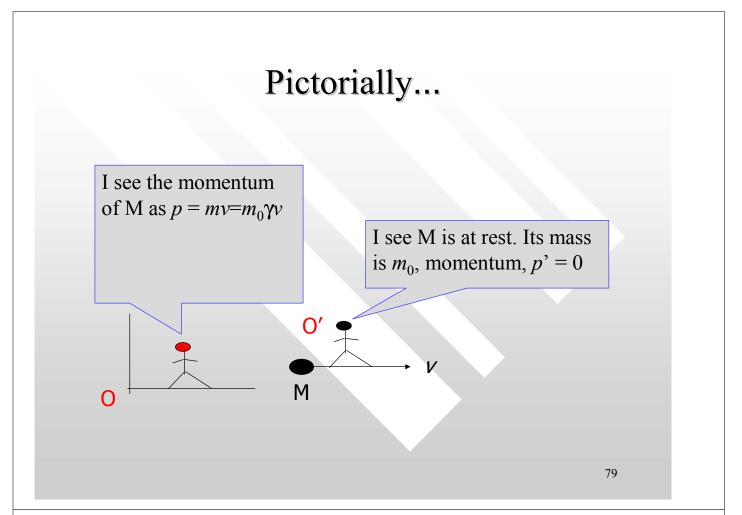
 In order to preserve the consistency between Lorentz transformation of velocity and conservation of linear momentum, the definition of 1-D linear momentum, classically defined as

 $p_{classical} = rest mass \times velocity,$

has to be modified to

 $p_{classical} \rightarrow p_{sr} = "relativistic mass" \times velocity$ = $mv = \gamma m_0 v$

- where the relativisitic mass $m = \gamma m_0$ is not the same the rest mass, m_0
- Read up the text for a more rigorous illustration why the definition of classical momentum is inconsistent with LT



Two kinds of mass

- Differentiate two kinds of mass: rest mass and relativistic mass
- m₀ = rest mass = the mass measured in a frame where the object is at rest. The rest mass of an object must be the same in all frames (not only in its rest frame).
- Relativistic mass $m = \gamma m_0$. The relativistic mass is speed-dependent

Behaviour of $p_{\rm SR}$ as compared to

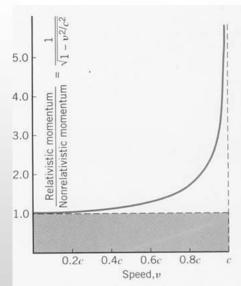


Figure 28.7 This graph shows how the ratio of the magnitude of the relativistic momentum to the magnitude of the nonrelativistic momentum increases as the speed of an object approaches the speed of light.

p_{classic}

- Classical momentum is constant in mass, $p_{\text{classic}} = m_0 v$
- Relativistic momentum is $p_{SR} = m_0 \gamma v$
- $p_{\text{SR}} / p_{\text{classic}} = \gamma \rightarrow \infty \text{ as } v \rightarrow c$
- In the other limit, $v \ll c$

 $p_{\rm SR} / p_{\rm classic} = 1$

Example

The rest mass of an electron is $m_0 = 9.11 \times 10^{-31} \text{kg}$.

m_0

If it moves with v = 0.75 c, what is its relativistic momentum?

$$p = m_0 \gamma u$$

Compare the relativistic p with that calculated with classical definition

Solution

- The Lorentz factor is $\gamma = [1 - (v/c)^2]^{-1/2} = [1 - (0.75c/c)^2]^{-1/2} = 1.51$
- Hence the relativistic momentum is simply
 - $p = \gamma m_0 \times 0.75c$
 - = $1.51 \times 9.11 \times 10^{-31} \text{kg} \times 0.75 \times 3 \times 10^8 \text{ m/s}$

$$= 3.1 \times 10^{-22}$$
 Ns

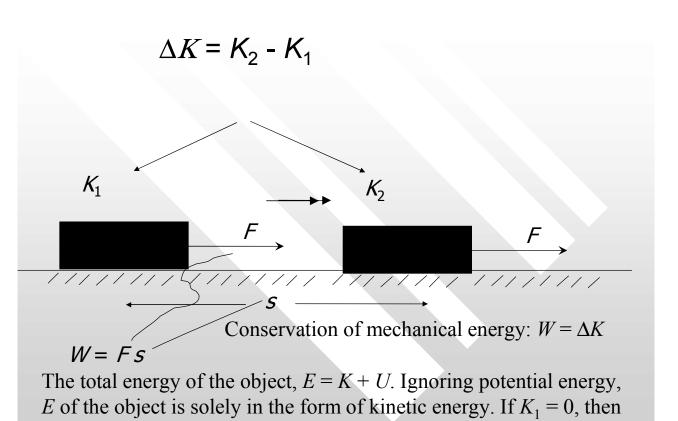
• In comparison, classical momentum gives $p_{\text{classical}} = m_0 \times 0.75c = 2.5 \times 10^{-22} \text{ Ns} - \text{about } 34\% \text{ lesser}$ than the relativistic value

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Work-Kinetic energy theorem

• Recall the law of conservation of mechanical energy:

Work done by external force on a system, W = the change in kinetic energy of the system, ΔK



 $E = K_2$. But in general, U also needs to be taken into account for E_{85} .

In classical mechanics, mechanical energy (kinetic + potential) of an object is closely related to its momentum and mass

Since in SR we have redefined the classical mass and momentum to that of relativistic version

$$m_{\text{class}}(\text{cosnt}, = m_0) \rightarrow m_{\text{SR}} = m_0 \gamma$$

$$p_{\text{class}} = m_{\text{class}} v \rightarrow p_{\text{SR}} = (m_0 \gamma) v$$

We must also modify the relation btw work and energy so that the law conservation of energy is consistent with SR

E.g, in classical mechanics, $K_{class} = p^2/2m = mv^2/2$. However, this relationship has to be supplanted by the relativistic version

$$K_{class} = mv^2/2 \rightarrow K_{SR} = E - m_0 c^2 = \gamma m_0 c^2 - m_0 c^2$$

We shall derive *K* in SR in the following slides

Force, work and kinetic energy

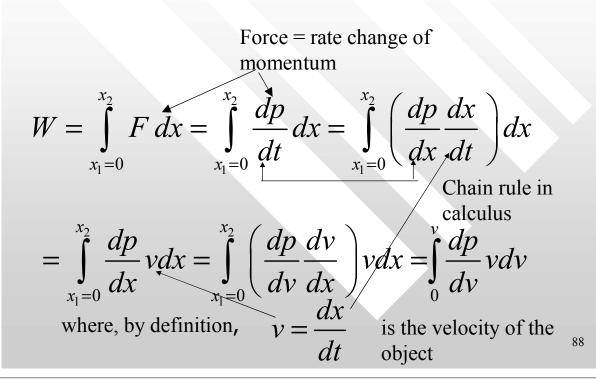
When a force is acting on an object with rest mass m₀, it will get accelerated (say from rest) to some speed (say v) and increase in kinetic energy from 0 to K

K as a function of *v* can be derived from first principle based on the definition of:

Force, F = dp/dt, work done, $W = \int F dx$, and conservation of mechanical energy, $\Delta K = W$

Derivation of relativistic kinetic energy

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Explicitly,
$$p = \gamma m_0 v$$
,
Hence, $dp/dv = d/dv (\gamma m_0 v)$
 $= m_0 [v (d\gamma/dv) + \gamma]$
 $= m_0 [\gamma + (v^2/c^2) \gamma^3] = m_0 (1 - v^2/c^2)^{-3/2}$
in which we have inserted the relation

$$\frac{d\gamma}{dv} = \frac{d}{dv} \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} = \frac{v}{c^2} \frac{1}{\left(1 - \frac{v^2}{c^2}\right)^{3/2}} = \frac{v}{c^2} \gamma^3$$

integrate
$$W = m_0 \int_0^v v \left(1 - \frac{v^2}{c^2}\right)^{-3/2} dv$$

$$\Rightarrow K = W = m_0 \gamma c^2 - m_0 c^2 = mc^2 - m_0 c^2$$

$$K = m_0 \gamma c^2 - m_0 c^2 = mc^2 - m_0 c^2$$

The relativistic kinetic energy of an object of rest mass m_0 traveling at speed v

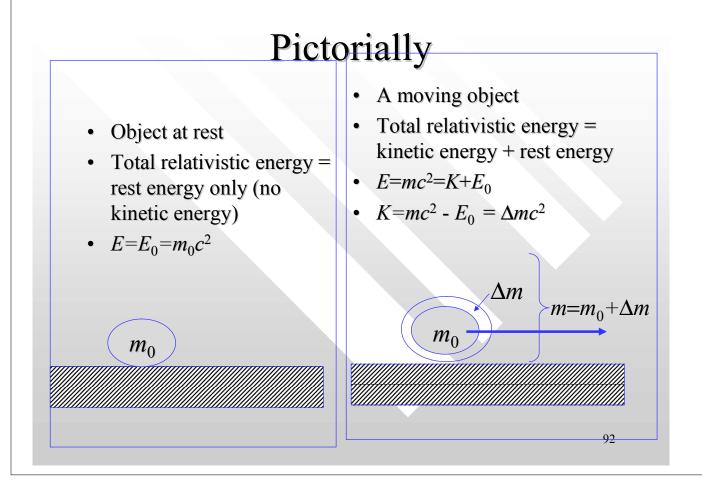
♦ E = mc² is the total relativistic energy of an moving object
♦ E₀ = m₀c² is called the rest energy of the object.
♦ Any object has non-zero rest mass contains energy E₀ = m₀c²
♦ One can imagine that masses are 'frozen energies in the form of masses' as per E₀ = m₀c²
♦ The rest energy (or rest mass) is an invariant

• Or in other words, the total relativistic energy of a moving object is the sum of its rest energy and its relativistic kinetic energy

$$E = mc^2 = m_0c^2 + K$$

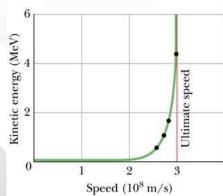
The (relativistic) mass of an moving object m is larger than its rest mass m_0 due to the contribution from its relativistic kinetic energy – this is a pure relativistic effect not possible in classical mechanics

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Relativistic Kinetic Energy of an electron



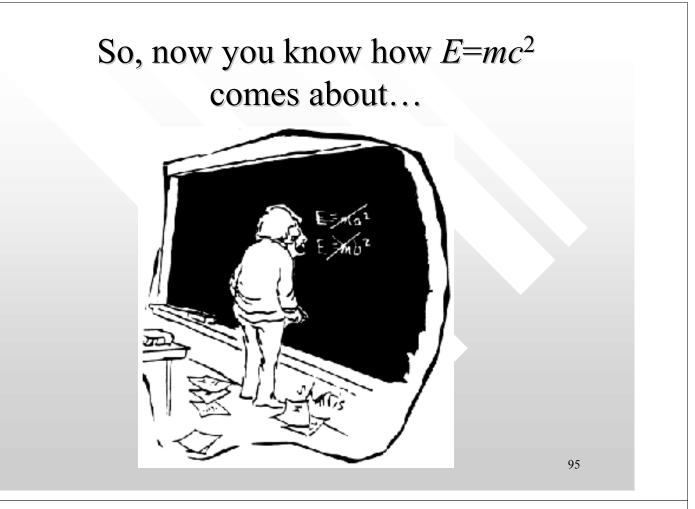
- The kinetic energy increases without limit as the particle speed *v* approaches the speed of light
- In principle we can add as much kinetic energy as we want to a moving particle in order to increase the kinetic energy of a particle without limit
- What is the kinetic energy required to accelerate an electron to the speed of light?
- Exercise: compare the classical kinetic energy of an object, $K_{clas} = m_0 v^2/2$ to the relativistic kinetic energy, $K_{sr} = (\gamma 1)m_0c^2$. What are their 93 difference?

Mass energy equivalence, $E = mc^2$

• $E = mc^2$ relates the relativistic mass of an object to the total energy released when the object is converted into pure energy

Example, 10 kg of mass, if converted into pure energy, it will be equivalent to $E = mc^2 = 10 \text{ x} (3 \text{ x} 10^8)^2 \text{ J} = 9 \text{ x} 10^{17} \text{J}$ - equivalent to a few tons of TNT explosive





Example 38-6: Energy of Fast Particle

- A particle of rest mass m_0 moves so fast that its total (relativistic) energy is equal to 1.1 times its rest energy.
- (a) What is the speed *v* of the particle?
- (b) What is the kinetic energy of the particle?

Solution

(a)

- Rest energy $E_0 = m_0 c^2$
- We are looking for a speed such that the energy is 1.1 times the rest energy.
- We know how the relativistic energy is related to the rest energy via
- $E = \gamma E_0 = 1.1 E_0$
- $\Rightarrow 1/\gamma^2 = 1/1.1^2 = 1/1.21 = 0.8264$
- $1 v^2/c^2 = 0.8264$
- $\Rightarrow v^2/c^2 = 1 0.8264 = 0.1736$
- \Rightarrow v = 0.4166 2c

(b) Kinetic energy is $K = E - E_0 = 1.1E_0 - E_0 = 0.1E_0 = 0.1 m_0 c^2$

Reduction of relativistic kinetic energy to the classical limit

• The expression of the relativistic kinetic energy

$$K = m_0 \gamma c^2 - m_0 c^2$$

must reduce to that of classical one in the limit $v/c \rightarrow 0$, i.e.

$$\lim_{v \ll c} K_{relativistic} = \frac{p_{classical}^2}{2m_0} \left(=\frac{m_0 v^2}{2}\right)$$

Expand γ with binomial expansion

For v << c, we can always expand γ in terms of (v/c)² as

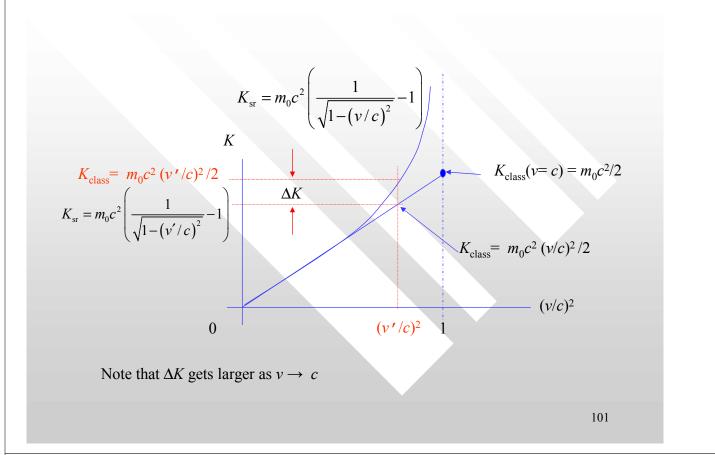
$$\gamma = \left(1 - \frac{v^2}{c^2}\right)^{-1/2} = 1 + \frac{v^2}{2c^2} + \text{ terms of order } \frac{v^4}{c^4} \text{ and higher}$$

$$K = mc^{2} - m_{0}c^{2} = m_{0}c^{2}(\gamma - 1)$$
$$= m_{0}c^{2}\left[\left(1 + \frac{1}{2}\frac{v^{2}}{c^{2}} + \dots\right) - 1\right] \approx \frac{m_{0}v^{2}}{2}$$

i.e., the relativistic kinetic energy reduces to classical expression in the $v \ll c$ limit

Exercise

- Plot K_{class} and K_{sr} vs (v/c)² on the same graph for (v/c)² between 0 and 1.
- Ask: In general, for a given velocity, does the classical kinetic energy of an moving object larger or smaller compared to its relativistic kinetic energy?
- In general does the discrepancy between the classical KE and relativistic KE increase or decrease as *v* gets closer to *c*?



Recap

• Important formula for total energy, kinetic energy and rest energy as predicted by SR:

E =total relativisitic energy;

$$m_0 = \text{rest mass};$$

- *m* = relativistic mass;
- $E_0 = \text{rest energy};$
- p = relativistic momentum,
- K = relativistic momentum;

$$m = \gamma m_0; p = \gamma m_0 v; K = \gamma m_0 c^2 - m_0 c^2; E_0 = m_0 c^2; E = \gamma m_0 c^2;$$

Example

- A microscopic particle such as a proton can be accelerated to extremely high speed of v = 0.85c in the Tevatron at <u>Fermi</u> <u>National Accelerator</u> <u>Laboratory</u>, US.
- Find its total energy and kinetic energy in eV.



Solution

Due to mass-energy equivalence, sometimes we express the mass of an object in unit of energy

- Proton has rest mass $m_p = 1.67 \times 10^{-27} \text{kg}$
- The rest mass of the proton can be expressed as energy equivalent, via
- $m_{\rm p}c^2 = 1.67 \times 10^{-31} \text{kg} \times (3 \times 10^8 \text{m/s})^2$

• =
$$1.5 \times 10^{-10} \text{ J}$$

- = $1.5 \times 10^{-10} \times (1.6 \times 10^{-19})^{-1} \text{ eV}$
- = 939,375,000 eV = 939 MeV

Solution

- First, find the Lorentz factor, $\gamma = 1.89$
- The rest mass of proton, m_0c^2 , is 939 MeV
- Hence the total energy is $E = mc^2 = \gamma (m_0 c^2) = 1.89 \times 939 \text{ MeV} = 1774 \text{ MeV}$
- Kinetic energy is the difference between the total relativistic energy and the rest mass, $K = E - m_0 c^2 = (1774 - 939) \text{ MeV} = 835 \text{ MeV}$

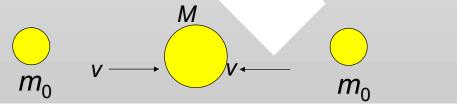
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Exercise

• Show that the rest mass of an electron is equivalent to 0.51 MeV

Conservation of Kinetic energy in relativistic collision

Calculate (i) the kinetic energy of the system and (ii) mass increase for a completely inelastic head-on of two balls (with rest mass m₀ each) moving toward the other at speed v/c = 1.5×10⁻⁶ (the speed of a jet plane). *M* is the resultant mass after collision, assumed at rest.



Solution

- (i) $K = 2mc^2 2m_0c^2 = 2(\gamma 1)m_0c^2$
- (ii) $E_{\text{before}} = E_{\text{after}} \Rightarrow 2\gamma m_0 c^2 = Mc^2 \Rightarrow M = 2\gamma m_0$
- Mass increase $\Delta M = M 2m_0 = 2(\gamma 1)m_0$
- Approximation: $v/c = ...=1.5 \times 10^{-6} \Rightarrow \gamma \approx 1 + \frac{1}{2} \frac{v^2}{c^2}$ (binomail expansion) $\Rightarrow M \approx 2(1 + \frac{1}{2} \frac{v^2}{c^2})m_0$
- Mass increase $\Delta M = M 2m_0$
 -)

$$\approx (v^2/c^2)m_0^2 = (1.5 \times 10^{-6})^2 m_0^2$$

- Comparing K with ΔMc^2 : the kinetic energy is not lost in relativistic inelastic collision but is converted into the mass of the final composite object, i.e. kinetic energy is conserved
- In contrast, in classical mechanics, momentum is conserved but kinetic energy is not in an inelastic collision

Relativistic momentum and relativistic Energy

In terms of relativistic momentum, the relativistic total energy can be expressed as followed

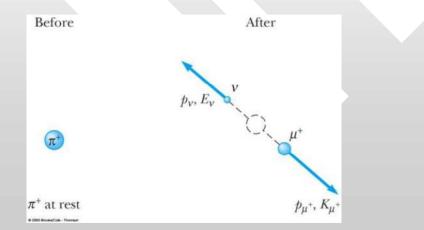
$$E^{2} = \gamma^{2} m_{0}^{2} c^{4}; p^{2} = \gamma^{2} m_{0}^{2} v^{2} \Rightarrow \frac{v^{2}}{c^{2}} = \frac{c^{2} p^{2}}{E^{2}}$$
$$\Rightarrow E^{2} = \gamma^{2} m_{0}^{2} c^{4} = \frac{m_{0}^{2} c^{4}}{1 - \frac{v^{2}}{c^{2}}} = \left(\frac{m_{0}^{2} c^{4} E^{2}}{E^{2} - c^{2} p^{2}}\right)$$
$$E^{2} = p^{2} c^{2} + m_{0}^{2} c^{4}$$
Conservation of energy-momentum

Invariance in relativistic dynamics

- Note that $E^2 p^2 c^2$ is an invariant, numerically equal to $(m_0 c^2)^2$
- i.e., in any dynamical process, the difference between the total energy squared and total momentum squared of a given system must remain unchanged
- In additional, when observed in other frames of reference, the total relativistic energy and total relativistic momentum may have different values, but their difference, $E^2 - p^2 c^2$, must remain invariant
- Such invariance greatly simplify the calculations in relativistic dynamics

Example: measuring pion mass using conservation of momentum-

- energy pi meson decays into a muon + massless neutrino
- If the mass of the muon is known to be $106 \text{ MeV}/c^2$, and the kinetik energy of the muon is measured to be 4.6 MeV, find the mass of the pion



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After

 $p_{\mu^{+}}, K_{\mu}$

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Solution

Relationship between Kinetic energy and momentum:

$$E_{\mu}^{2} = p_{\mu}^{2}c^{2} + m_{\mu}^{2}c^{2}$$

Mo

Conservation of relativistic energy: $E_{\pi} = E_{\mu} + E_{\nu}$

$$\Rightarrow m_{\pi}c^{2} = \sqrt{m_{\mu}^{2}c^{4} + c^{2}p_{\mu}^{2}} + \sqrt{2M_{\nu}^{2}c^{4} + c^{2}p_{\nu}^{2}}$$

$$\Rightarrow m_{\pi}c = \sqrt{m_{\mu}^{2}c^{2} + p_{\mu}^{2}} + p_{\mu}$$

Before
mentum conservation: $p_{\mu} = p_{\nu}$
Also, total energy = K.E. + rest energy
 $E_{\mu} = K_{\mu} + m_{\mu}c^{2} \Rightarrow E_{\mu}^{2} = (K_{\mu} + m_{\mu}c^{2})^{2}$
But $E_{\mu}^{2} = p_{\mu}^{2}c^{2} + m_{\mu}^{2}c^{4}$

$$\Rightarrow E_{\mu}^{2} = p_{\mu}^{2}c^{2} + m_{\mu}^{2}c^{4} = \left(K_{\mu} + m_{\mu}c^{2}\right)^{2}; \qquad \pi^{+} \text{ at rest}$$

$$p_{\mu}c = \sqrt{\left(K_{\mu} + m_{\mu}c^{2}\right)^{2} - m_{\mu}^{2}c^{4}}$$

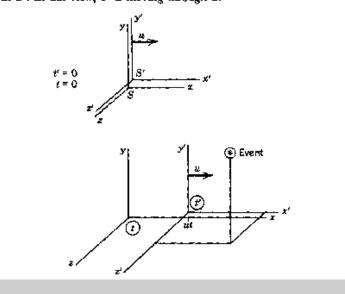
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Plug
$$p_{\mu}^{2}c^{2} = (K_{\mu} + m_{\mu}c^{2})^{2} - m_{\mu}^{2}c^{4}$$
 into
 $m_{\pi}c^{2} = \sqrt{m_{\mu}^{2}c^{4} + c^{2}p_{\mu}^{2}} + cp_{\mu}$
 $= \sqrt{m_{\mu}^{2}c^{4} + [(K_{\mu} + m_{\mu}c^{2})^{2} - m_{\mu}^{2}c^{4}]} + \sqrt{(K_{\mu} + m_{\mu}c^{2})^{2} - m_{\mu}^{2}c^{4}}$
 $= (K_{\mu} + m_{\mu}c^{2}) + \sqrt{(K_{\mu}^{2} + 2K_{\mu}m_{\mu}c^{2})}$
 $= (4.6 \text{MeV} + \frac{106 \text{MeV}}{c^{2}}c^{2}) + \sqrt{(4.6 \text{MeV})^{2} + 2(4.6 \text{MeV})(\frac{106 \text{MeV}}{c^{2}})c^{2}}$
 $= 111 \text{MeV} + \sqrt{996} \text{MeV} = 143 \text{MeV}$

Observing an event from lab frame and rocket frame

Figure 1-13

Reference systems S and S' in relative motion. An event occurs at (x, y, z, t) in S and (x', y', z', t') in S'. In this view, S' is moving through S.



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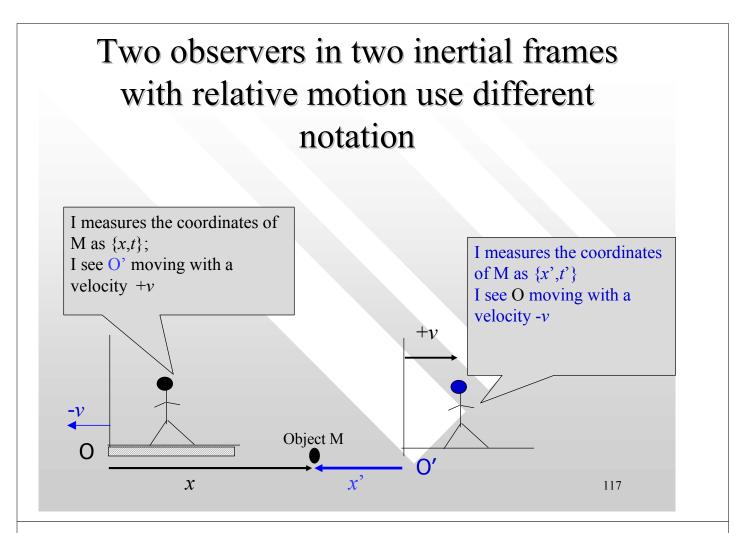
Lorentz Transformation

- All inertial frames are equivalent
- Hence all physical processes analysed in one frame can also be analysed in other inertial frame and yield consistent results
- Any event observed in two frames of reference must yield consistent results related by transformation laws
- Specifically such a transformation law is required to related the space and time coordinates of an event observed in one frame to that observed from the other

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Different frame uses different notation for coordinates

- O' frame uses {x',y',z';t'} to denote the coordinates of an event, whereas O frame uses {x,y,z;t}
- How to related $\{x', y', z', t'\}$ to $\{x, y, z; t\}$?
- In Newtonian mechanics, we use Galilean transformation

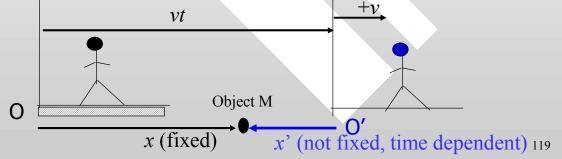


Galilean transformation (applicable only for v << c)

- For example, the spatial coordinate of the object M as observed in O is x and is being observed at a time t, whereas according to O', the coordinate for the space and time coordinates are x' and t'. At low speed v <<c, the transformation that relates {x',t'} to {x,t} is given by Galilean transformation
- {x'=x-vt, t'=t} (x' and t' in terms of x,t)
- $\{x = x' + vt, t = t'\}$ (x and t in terms of x',t')

Illustration on Galilean transformation

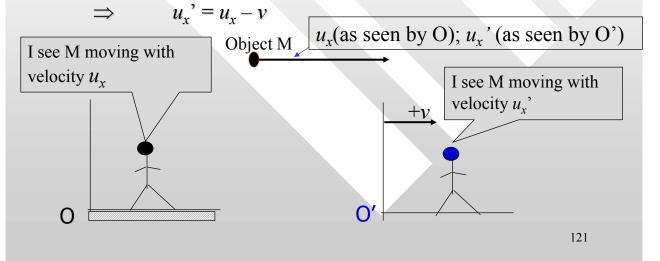
- of $\{x'=x-vt, t'=t\}$ Assume object M is at rest in the O frame, hence the coordinate of the object M in O frame is fixed at x
- Initially, when t = t' = 0, O and O' overlap
- O' is moving away from O at velocity +v
- The distance of the origin of O' is increasing with time. At time t (in O frame), the origin of O' frame is at an instantaneous distance of +vt away from O
- In the O' frame the object M is moving away with a velocity -v (to the left)
- Obviously, in O' frame, the coordinate of the object M, denoted by x', is timedependent, being x' = x - vt
- In addition, under current assumption (i.e. classical viewpoint) the rate of time flow is assumed to be the same in both frame, hence $t = \hat{t}$



However, GT contradicts the SR postulate when v approaches the speed of light, hence it has to be supplanted by a relativistic version of transformation law when near-to-light speeds are involved: Lorentz transformation (The contradiction becomes more obvious if GT on velocities, rather than on space and time, is considered)

Galilean transformation of velocity (applicable only for $u_x, v \ll c$)

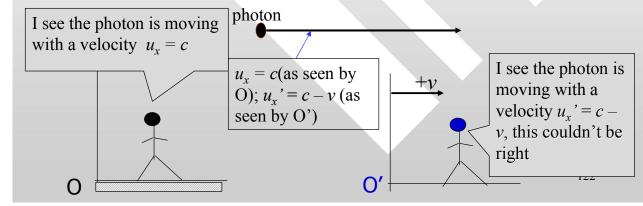
- Now, say object M is moving as a velocity of v wrp to the lab frame O
- What is the velocity of M as measured by O'?
- Differentiate x' = x vt wrp to t (=t'), we obtain
- d(x')/dt' = d(x vt)/dt = d(x)/dt v



If applied to light Galilean transformation of velocity

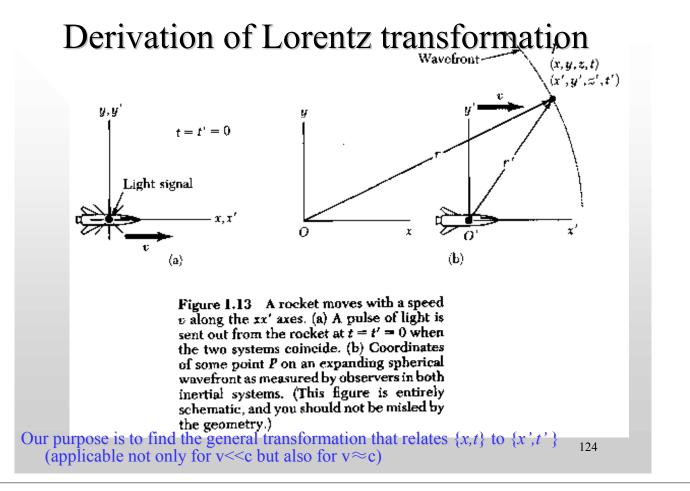
contradicts the SR Postulate Consider another case, now, a photon (particle of light) observed from

- Consider another case, now, a photon (particle of light) observed from different frames
- A photon, being a massless particle of light must move at a speed $u_x = c$ when observed in O frame
- However Galilean velocity addition law $u_x' = u_x v$, if applied to the photon, says that in O' frame, the photon shall move at a lower speed of $u_x' = u_x v = c v$
- This is a contradiction to the constancy of light speed in SR



Conclusion

- GT (either for spatial, temporal or velocity) cannot be applicable when dealing with object moving near or at the speed of light
- It has to be supplanted by a more general form of transformation – Lorentz transformation, LT
- LT must reduce to GT when *v* << *c*.



Read derivation of LT from the texts

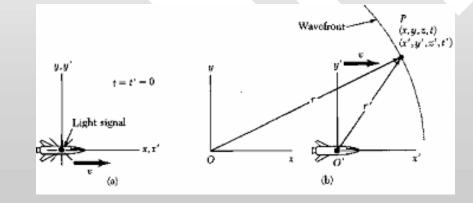
- Brehm and Mullin
- Krane
- Serway, Mayer and Mosses

Derivation of Lorentz transformation

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- Consider a rocket moving with a speed v (O' frame) along the xx' direction wrp to the stationary O frame
- A light pulse is emitted at the instant t' = t = 0 when the two origins of the two reference frames coincide
- The light signal travels as a spherical wave at a constant speed *c* in both frames
- After in time interval of *t*, the origin of the wave centred at O has a radius r = ct, where $r^2 = x^2 + y^2 + z^2$



Arguments

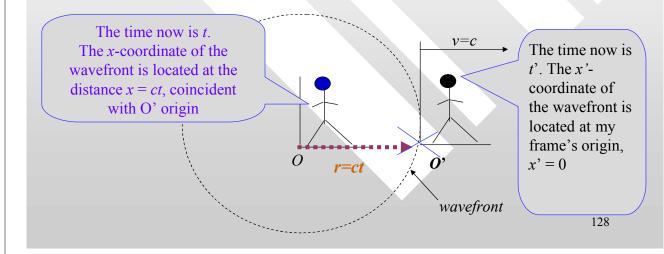
• From the view point of O', after an interval *t* ' the origin of the wave, centred at O' has a radius:

$$r' = ct', (r')^2 = (x')^2 + (y')^2 + (z')^2$$

- y'=y, z' = z (because the motion of O' is along the xx') axis no change for y,z coordinates (condition A)
- The transformation from x to x' (and vice versa) must be linear, i.e. $x' \propto x$ (condition B)
- Boundary condition (1): If v = c, from the viewpoint of O, the origin of O' is located on the wavefront (to the right of O)
- $\Rightarrow x' = 0$ must correspond to x = ct
- Boundary condition (2): In the same limit, from the viewpoint of O', the origin of O is located on the wavefront (to the left of O')
- $\Rightarrow x = 0$ corresponds to x' = -ct'
- Putting everything together we assume the transformation that relates x' to {x, t} takes the form x' = k(x ct) as this will fulfill all the conditions (B) and boundary condition (1); (k some proportional constant to be determined)
- Likewise, we assume the form x = k(x'+ct') to relate x to $\{x', t'\}$ as this is the form that fulfill all the conditions (B) and boundary condition (2)

Illustration of Boundary condition (1)

- x = ct ($x^2 = ct^2$) is defined as the x-coordinate (x²-coordinate) of the wavefront in the O (O²) frame
- Now, we choose O as the rest frame, O' as the rocket frame. Furthermore, assume O' is moving away to the right from O with light speed, i.e. v = +c
- Since u = c, this means that the wavefront and the origin of O' coincides all the time
- For O, the x-coordinate of the wavefront is moving away from O at light speed; this is tantamount to the statement that x = ct
- From O' point of view, the x'-coordinate of the wavefront is at the origin of it's frame; this is tantamount to the statement that x' = 0
- Hence, in our yet-to-be-derived transformation, x' = 0 must correspond to x = ct



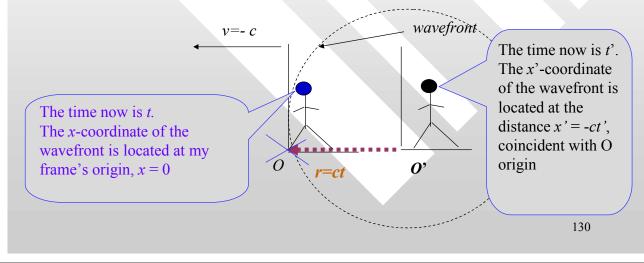
Permuting frames

- Since all frames are equivalent, physics analyzed in O' frame moving to the right with velocity +v is equivalent to the physics analyzed in O frame moving to the left with velocity -v
- Previously we choose O frame as the lab frame and O' frame the rocket frame moving to the right (with velocity +v wrp to O)
- Alternatively, we can also fix O' as the lab frame and let O frame becomes the rocket frame moving to the left (with velocity –v wrp to O')

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Illustration of Boundary condition (2)

- Now, we choose O' as the rest frame, O as the rocket frame. From O' point of view, O is moving to the left with a relative velocity v = -c
- From O' point of view, the wavefront and the origin of O coincides. The x'-coordinate of the wavefront is moving away from O' at light speed to the left; this is tantamount to the statement that x' = -ct'
- From O point of view, the x-coordinate of the wavefront is at the origin of it's frame; this is tantamount to the statement that x = 0
- Hence, in our yet-to-be-derived transformation, x = 0 must correspond to x' = -ct'



Finally, the transformation obtained

- We now have
- $r = ct, r^2 = x^2 + y^2 + z^2; y' = y, z' = z; x = k(x' + ct');$
- $r' = ct', r'^2 = x'^2 + y'^2 + z'^2; x' = k(x ct);$
- With some algebra, we can solve for $\{x',t'\}$ in terms of $\{x,t\}$ to obtain the desired transformation law (do it as an exercise)
- The constant k turns out to be identified as the Lorentz factor, γ

$$x' = \frac{x - vt}{\sqrt{1 - \left(\frac{v}{c}\right)^2}} = \gamma(x - vt) \qquad t' = \frac{t - \left(\frac{v}{c}\right)x}{\sqrt{1 - \left(\frac{v}{c}\right)^2}} = \gamma\left[t - \frac{v}{c^2}\right]x$$

(x' and t' in terms of x, t)

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Space and time now becomes stateof-motion dependent (via γ)

- Note that, now, the length and time interval measured become dependent of the state of motion (in terms of *γ*) in contrast to Newton's classical viewpoint
- Lorentz transformation reduces to Galilean transformation when *v* << *c* (show this yourself)
- i.e. LT \rightarrow GT in the limit $v \ll c$

How to express $\{x, t\}$ in terms of $\{x', t'\}$?

• We have expressed {*x'*,*t'*} in terms of {*x*,*t*} as per

$$x' = \frac{x - vt}{\sqrt{1 - \left(\frac{v}{c}\right)^2}} = \gamma(x - vt) \qquad t' = \frac{t - \left(\frac{v}{c}\right)x}{\sqrt{1 - \left(\frac{v}{c}\right)^2}} = \gamma\left[t - \left(\frac{v}{c}\right)x\right]$$

Now, how do we express {x, t } in terms of {x', t'}?

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Simply permute the role of x and x'and reverse the sign of v

$$x \leftrightarrow x', v \rightarrow -v$$
$$x' = \gamma(x - vt) \rightarrow x = \gamma(x' + vt')$$
$$t' = \gamma \left[t - (v/c^2)x \right] \rightarrow t = \gamma \left[t' + (v/c^2)x' \right]$$

The two transformations above are equivalent; use which is appropriate in a given question

Length contraction

- Consider the rest length of a ruler as measured in frame O' is
- $L' = \Delta x' = x'_2 x'_1$ (proper length) measured at the same instance in that frame $(t'_2 = t'_1)$
- What is the length of the rule as measured by O?
- The length in O, L, according the LT can be deduced as followed:

 $L' = \Delta x' = x'_{2} - x'_{1} = \gamma [(x_{2} - x_{1}) - \nu(t_{2} - t_{1})]$

- The length of the ruler in O, L, is simply the distance btw x_2 and x_1 measured at the same instance in that frame ($t_2 = t_1$). Hence we have
 - $L' = \gamma L$
- where L = is the improper length.
- As a consequence, we obtain the relation between the proper length measured by the observer at rest wrp to the ruler and that measured by an observer who is at a relative motion wrp to the ruler:

 $L' = \gamma L$

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Moving rulers appear shorter

$L' = \gamma L$

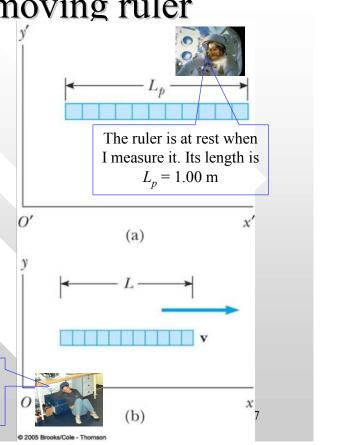
- L'is defined as the proper length = length of and object measured in the frame in which the object is at rest
- *L* is the length measured in a frame which is moving wrp to the ruler
- If an observer at rest wrp to an object measures its length to be L', an observer moving with a relative speed u wrp to the object will find the object to be shorter than its rest length by a factor $1 / \gamma$
- i.e., the length of a moving object is measured to be shorter than the proper length hence "length contraction"
- In other words, a moving rule will appear shorter!!

Example of a moving ruler

Consider a meter rule is carried on board in a rocket (call the rocket frame O')

- An astronaut in the rocket measure the length of the ruler. Since the ruler is at rest wrp to the astronaut in O', the length measured by the astronaut is the proper length, $L_p = 1.00$ m, see (a)
- Now consider an observer on the lab frame on Earth. The ruler appears moving when viewed by the lab observer. If the lab observer attempts to measure the ruler, the ruler would appear shorter than 1.00m

The ruler is at moving at a speed v when I measure it. Its length is L = 0.999 m

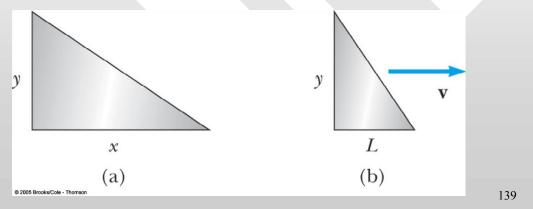


RE 38-11

• What is the speed v of a passing rocket in the case that we measure the length of the rocket to be half its length as measured in a frame in which the rocket is at rest?

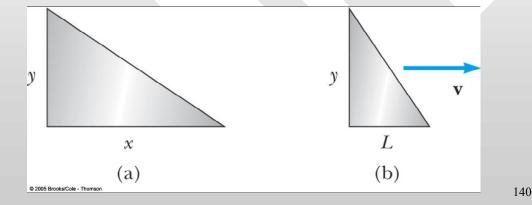
Length contraction only happens along the direction of motion

Example: A spaceship in the form of a triangle flies by an observer at rest wrp to the ship (see fig (a)), the distance x and y are found to be 50.0 m and 25.0 m respectively. What is the shape of the ship as seen by an observer who sees the ship in motion along the direction shown in fig (b)?



Solution

- The observer sees the horizontal length of the ship to be contracted to a length of
- $L = L_p / \gamma = 50 \text{ m} \sqrt{(1 0.950^2)} = 15.6 \text{ m}$
- The 25 m vertical height is unchanged because it is perpendicular to the direction of relative motion between the observer and the spaceship.



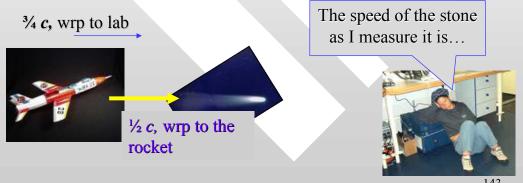
Similarly, one could also derive time dilation from the LT

Do it as homework

• Mr. Thompkins's in

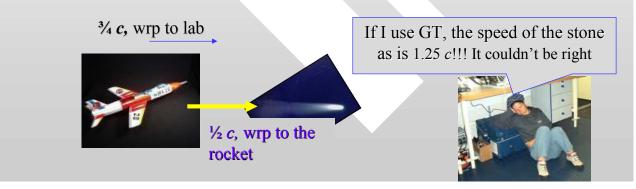
What is the velocities of the ejected stone?

 Imagine you ride on a rocket moving ³/₄ c wrp to the lab. From your rocket you launch a stone forward at ¹/₂ c, as measured in your rocket frame. What is the speed of the stone observed by the lab observer?



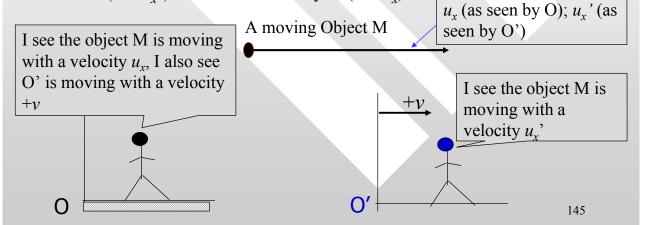
Adding relativistic velocities using Galilean transformation According to GT of velocity (which is valid at low speed regime v <<

- According to GT of velocity (which is valid at low speed regime v << c),
- the lab observer would measure a velocity of $u_x = u_x' + v = \frac{1}{2}c + \frac{3}{4}c$
- = 1.25 c for the ejected stone.
- However, in SR, *c* is the ultimate speed and no object can ever exceed this ultimate speed limit
- So something is no right here...Galilean addition law is no more valid to handle addition of relativistic velocities (i.e. at speed near to *c*)



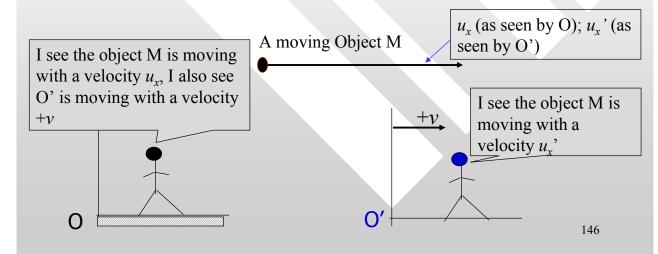
Relativity of velocities

- The generalised transformation law of velocity used for addition of relativistic velocities is called Lorentz transformation of velocities, derived from the Lorentz transformation of space-time
- Our task is to relate the velocity of the object M as observed by O' (i.e. u_x') to that observed by O (i.e. u_x).



Relativity of velocities

- Consider an moving object being observed by two observers, one in the lab frame and the other in the rocket frame
- We could derive the Lorentz transformation of velocities by taking time derivative wrp to the LT for space-time, see next slide



Derivation of Lorentz transformation of velocities

• By definition, $u_x = dx/dt$, $u'_x = dx'/dt'$

• The velocity in the O' frame can be obtained by taking the differentials of the Lorentz transformation

$$x' = \gamma(x - vt) \quad t' = \gamma \left[t - (v/c^2)x \right]$$

$$dx' = \gamma(dx - vdt), dt' = \gamma(dt - \frac{v}{c^2}dx)$$

Combining

$$u'_{x} = \frac{dx'}{dt'} = \frac{\gamma(dx - vdt)}{\gamma(dt - \frac{v}{c^{2}}dx)} = \frac{dt\left(\frac{dx}{dt} - v\frac{dt}{dt}\right)}{dt\left(\frac{dt}{dt} - \frac{v}{c^{2}}\frac{dx}{dt}\right)}$$
$$= \frac{u_{x} - v}{1 - \frac{vu_{x}}{c^{2}}}$$
where we have made used of the definition
$$u_{x} = \frac{dx}{dt}$$

Comparing the LT of velocity with that of GT

Lorentz transformation of velocity:

$$u'_{x} = \frac{dx'}{dt'} = \frac{u_{x} - v}{1 - \frac{u_{x}v}{c^{2}}}$$

Galilean transformation of velocity:

$$u'_x = u_x - v$$

LT reduces to GT in the limit $u_x v \ll c^2$

		_
1	4	9

 Please try to make a clear distinction among the definitions of various velocities, i.e. u_x, u'_x, v so that you wont get confused

LT is consistent with the constancy of speed of light

- In either O or O' frame, the speed of light seen must be the same, c. LT is consistent with this requirement.
- Say object M is moving with speed of light as seen by O, i.e. $u_x = c$
- According to LT, the speed of M as seen by O' is

$$u'_{x} = \frac{u_{x} - v}{1 - \frac{u_{x}v}{c^{2}}} = \frac{c - v}{1 - \frac{cv}{c^{2}}} = \frac{c - u}{1 - \frac{v}{c}} = \frac{c - v}{\frac{1}{c}(c - v)} = c$$

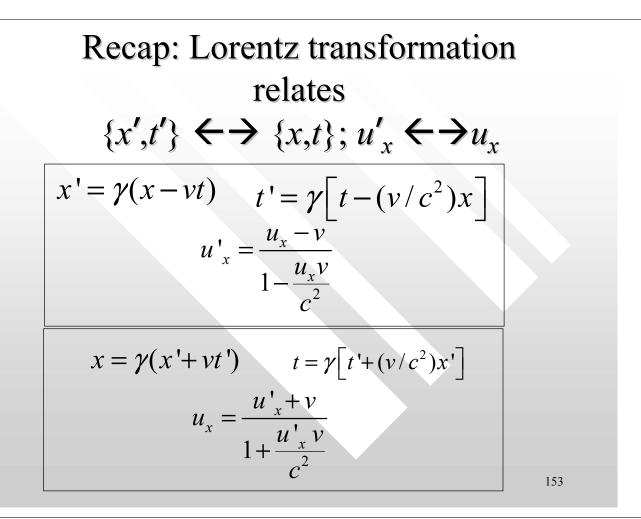
• That is, in either frame, both observers agree that the speed of light they measure is the same, $c = 3 \times 10^8$ m/s

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How to express u_x in terms of u_x' ?

• Simply permute v with -v and change the role of u_x with that of u_x' :

$$u_x \to u'_x, u'_x \to u_x, v \to -v$$
$$u'_x = \frac{u_x - v}{1 - \frac{u_x v}{c^2}} \to u_x = \frac{u'_x + v}{1 + \frac{u'_x v}{c^2}}$$



RE 38-12

A rocket moves with speed 0.9c in our lab frame. A flash of light is sent toward from the front end of the rocket. Is the speed of that flash equal to 1.9 c as measured in our lab frame? If not, what is the speed of the light flash in our frame? Verify your answer using LT of velocity formula.

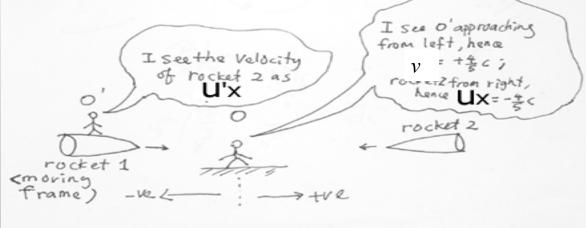
Example (relativistic velocity addition)

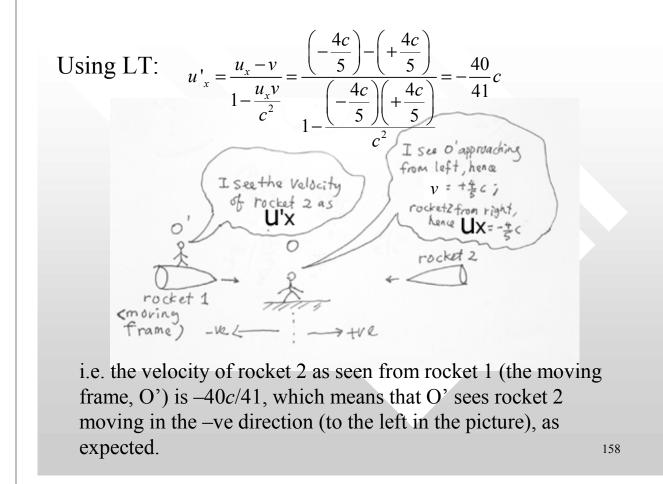
 Rocket 1 is approaching rocket 2 on a head-on collision course. Each is moving at velocity 4c/5 relative to an independent observer midway between the two. With what velocity does rocket 2 approaches rocket 1?

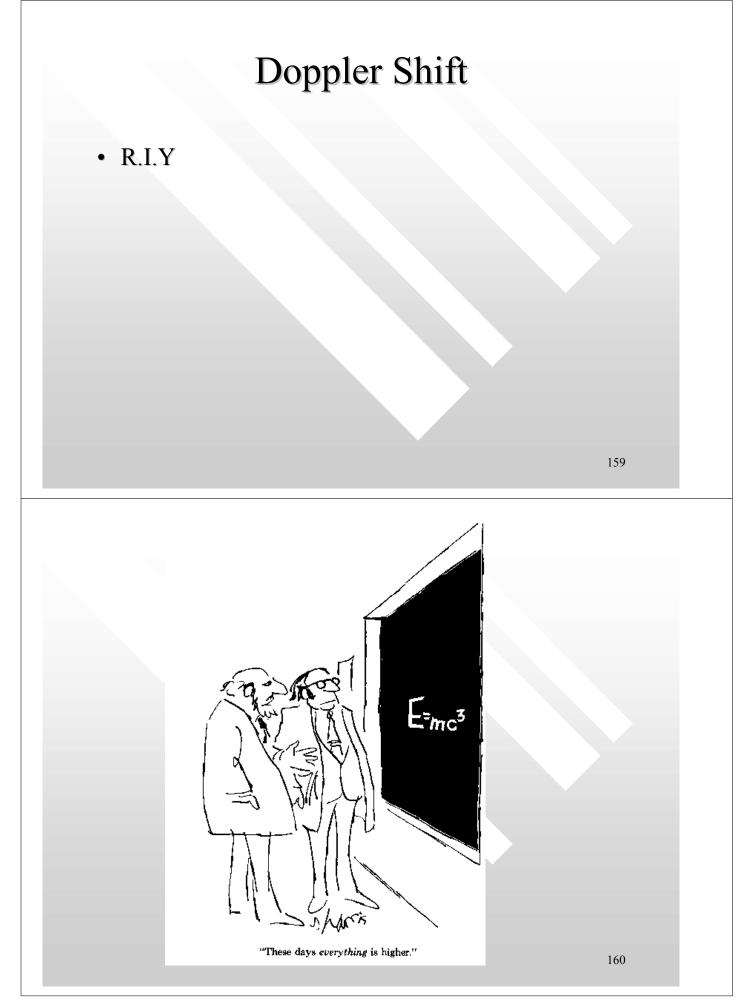
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Diagramatical translation of the question in text I see O approaching from left, hence I see the Velocity of rocket 2 as rocketz from right, U'x hence UX=-#c rocket 2 rocket 1 cmoving (Trame) >+VR -W2 L-Note: c.f. in GT, their relative speed would just be 4c/5 + 4c/5 = 1.6 cwhich violates constancy of speed of light postulate. See how LT handle this situation: 156

- Choose the observer in the middle as in the stationary frame, O
- Choose rocket 1 as the moving frame O'
- Call the velocity of rocket 2 as seen from rocket 1 *u*'x. This is the quantity we are interested in
- Frame O' is moving in the +ve direction as seen in O, so v = +4c/5
- The velocity of rocket 2 as seen from O is in the
- -ve direction, so ux = -4c/5
- Now, what is the velocity of rocket 2 as seen from frame O', u 'x = ? (intuitively, u 'x must be in the negative direction)







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CHAPTER 3

EXPERIMENTAL EVIDENCES FOR PARTICLE-LIKE PROPERTIES OF WAVES

Photoelectricity

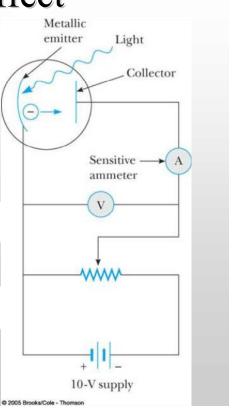
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2

- Classically, light is treated as EM wave according to Maxwell equation
- However, in a few types of experiments, light behave in ways that is not consistent with the wave picture
- In these experiments, light behave like particle instead
- So, is light particle or wave? (recall that wave and particle are two mutually exclusive attributes of existence)
- This is a paradox that we will discuss in the rest of the course wave particle duality

Photoelectric effect

- Photoelectrons are ejected from a metal surface when hit by radiation of sufficiently high frequency *f* (usually in the uv region)
- The photoelectrons are attracted to the collecting anode (positive) by potential difference applied on the anode and detected as electric current by the external circuits
- A negative voltage, relative to that of the emitter, can be applied to the collector.
- When this retarding voltage is sufficiently large the emitted electrons are repelled, and the current to the collector drops to zero (see later explanation).



Photocurrent I vs applied voltage V at constant fPhotocurrent No current flows for a saturation photocurrent retarding potential more I_2 at higher radiation I_2 intensity, R_2 negative than $-V_{s}$ The photocurrent I saturates for potentials near or above zero saturation photocurrent Why does the *I*-*V* curve I_1 at lower radiation rises gradually from $-V_s$ intensity, R₁ towards more positive VApplied voltage before it flat off? $-V_{s}K_{max} = eV_{s} \int_{(a)} f constant$

Features of the experimental result

- When the external potential difference V = 0, the current is not zero because the photoelectrons carry some kinetic energy, K
- K range from 0 to a maximal value, K_{max}
- As V becomes more and more positive, there are more electrons attracted towards the anode within a given time interval. Hence the pthotocurrent, I, increases with V
- Saturation of *I* will be achieved when all of the ejected electron are immediately attracted towards the anode once they are kicked out from the metal plates (from the curve this happens approximately when $V \approx 0$ or larger

- On the other direction, when V becomes more negative, the photocurrent detected decreases in magnitude because the electrons are now moving against the potential
- K_{max} can be measured. It is given by eV_s , where V_s , is the value of |V| when the current flowing in the external circuit = 0
- $V_{\rm s}$ is called the '**stopping potential**'
- When $V = -V_s$, e of the highest KE will be sufficiently retarded by the external electric potential such that they wont be able to reach the collector

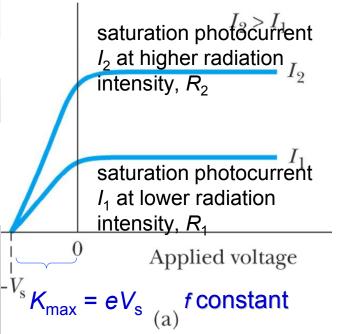
$I_2 > I_1$ because more electrons are kicked out per unit time by radiation of larger intensity, *R*

- The photocurrent saturates at a larger value of I_2 when it is irradiated by higher radiation intensity R_2
- This is expected as larger *R* means energy are imparted at a higher rate on the metal surface

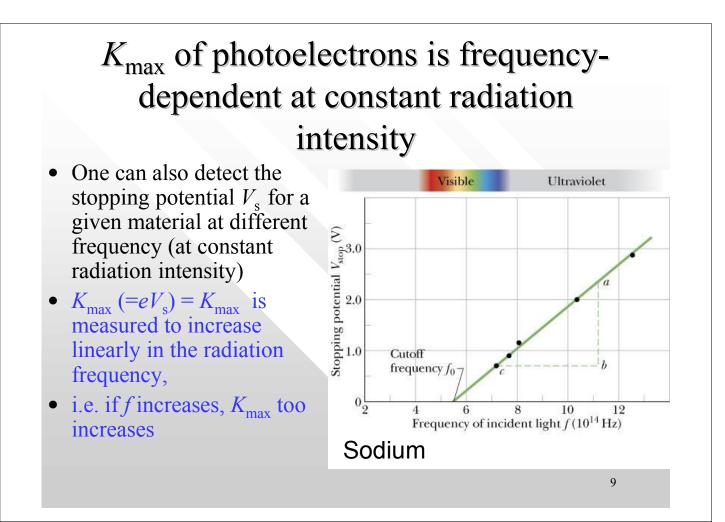
Stopping potential V_s is radiation intensity-independent

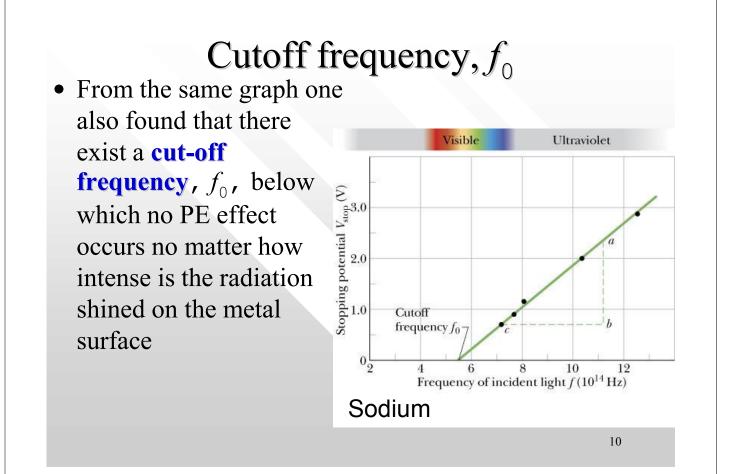
- Experimentalists observe that for a given type of surface:
- At constant frequency the maximal kinetic energy of the photoelectrons is measured to be a constant independent of the intensity of light.
- (this is a puzzle to those who thinks that light is wave)

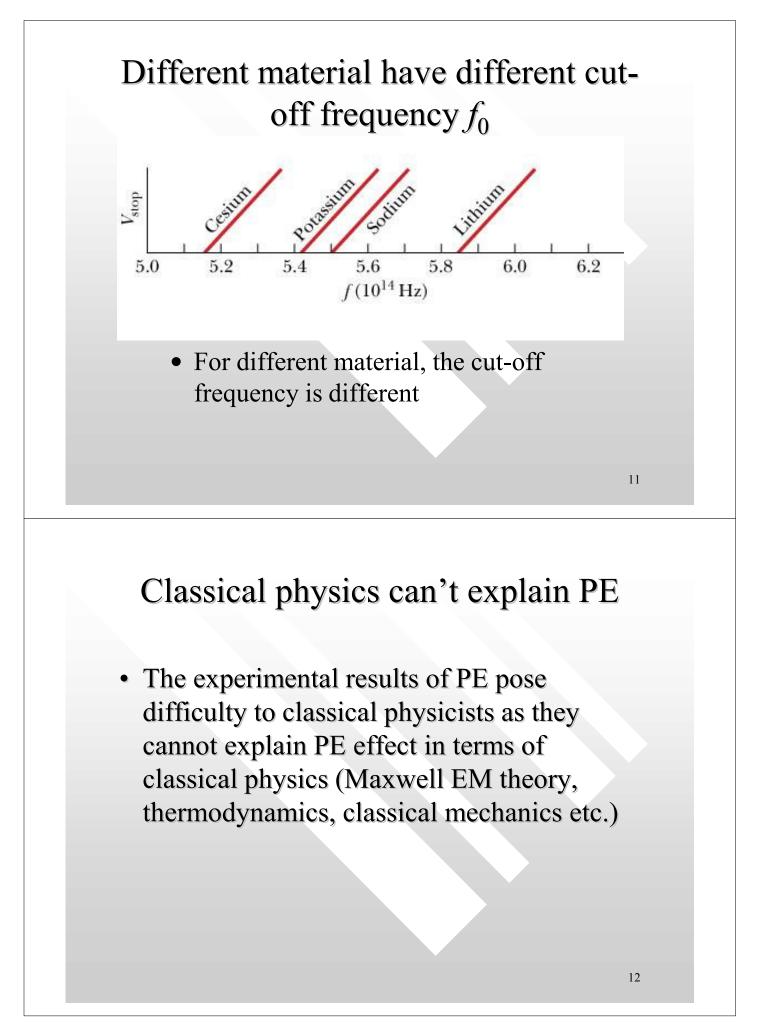
Photocurrent



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Puzzle one

- If light were wave, the energy carried by the radiation will increases as the intensity of the monochromatic light increases
- Hence we would also expect K_{max} of the electron to increase as the intensity of radiation increases (because K.E. of the photoelectron must come from the energy of the radiation)
- YET THE OBSERVATION IS OTHERWISE.

Puzzle two

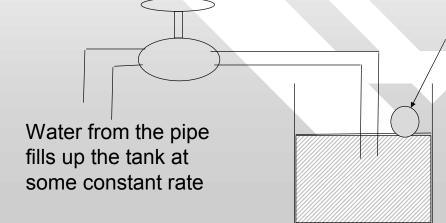
- Existence of a characteristic cut-off frequency, v₀. (previously I use f₀)
- Wave theory predicts that photoelectric effect should occur for any frequency as long as the light is intense enough to give the energy to eject the photoelectrons.
- No cut-off frequency is predicted in classical physics.

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Puzzle three

- No detection time lag measured.
- Classical wave theory needs a time lag between the instance the light impinge on the surface with the instance the photoelectrons being ejected. Energy needs to be accumulated for the wave front, at a rate proportional to $S = \frac{E_0}{2\mu_0 c}$, before it has enough energy to eject photoelectrons. (*S* = energy flux of the EM radiation)
- But, in the PE experiments, PE is almost immediate

Cartoon analogy: in the wave picture, accumulating the energy required to eject an photoelectron from an atom is analogous to filling up a tank with water from a pipe until the tank is full. One must wait for certain length of time (time lag) before the tank can be filled up with water at a give rate. The total water filled is analogous to the total energy absorbed by electrons before they are ejected from the metal surface at



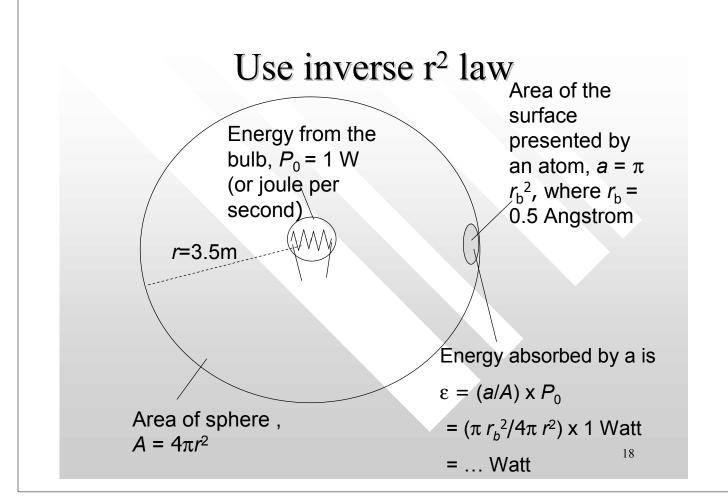
Electron spills out from the tank when the water is filled up gradually after some 'time lag' 16

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Wave theory and the time delay problem

A potassium foil is placed at a distance r = 3.5 m from a light source whose output power P₀ is 1.0 W. How long would it take for the foil to soak up enough energy (=1.8 eV) from the beam to eject an electron? Assume that the ejected electron collected the energy from a circular area of the foil whose radius is 5.3 x 10⁻¹¹ m

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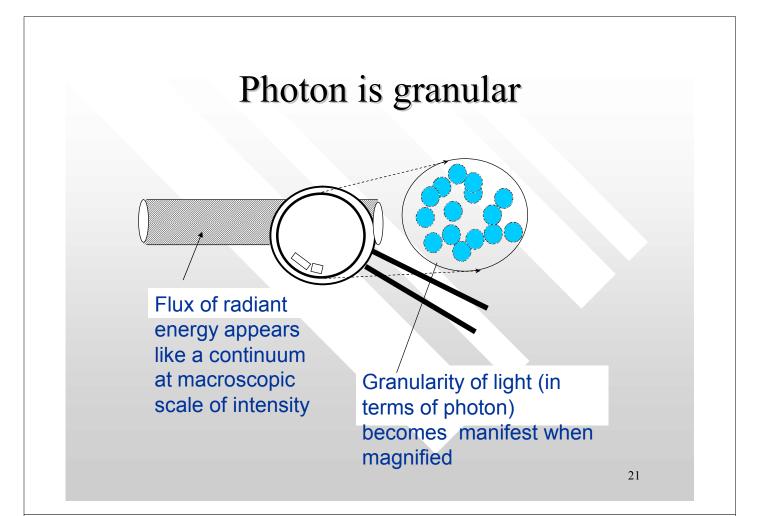


- Time taken for a to absorb 1.8 eV is simply 1.8 x $1.6 \ge 10^{-19} \text{ J} / \epsilon = 5000 \text{ s} = 1.4 \text{ h}!!!$
- In PE, the photoelectrons are ejected almost immediately but not 1.4 hour later
- This shows that the wave model used to calculate the time lag in this example fails to account for the almost instantaneous ejection of photoelectron in the PE experiment

Einstein's quantum theory of the photoelectricity (1905)

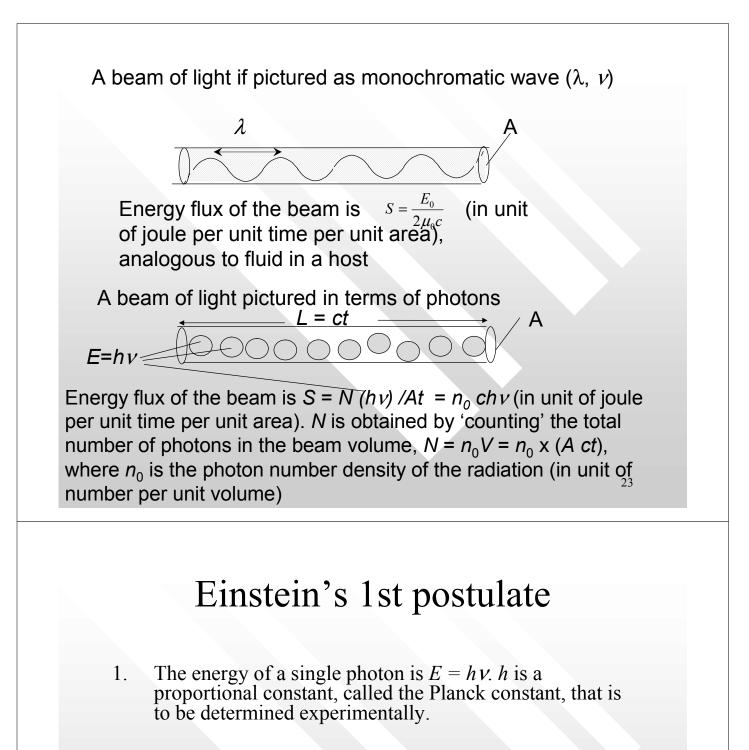
- A Noble-prize winning theory
- To explain PE, Einstein postulates that the radiant energy of light is quantized into concentrated bundle. The discrete entity that carries the energy of the radiant energy is called photon
- Or, in quantum physics jargon, we say "photon is the quantum of light"
- Wave behaviour of light is a result of collective behaviour of very large numbers of photons

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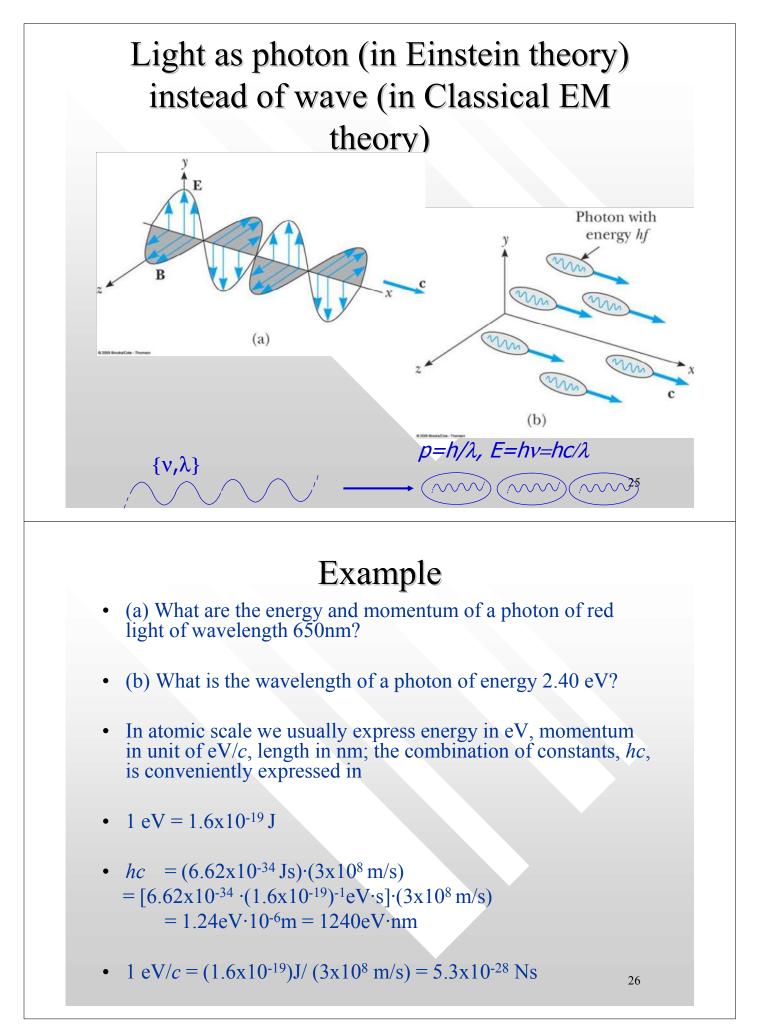


Wave and particle carries energy differently

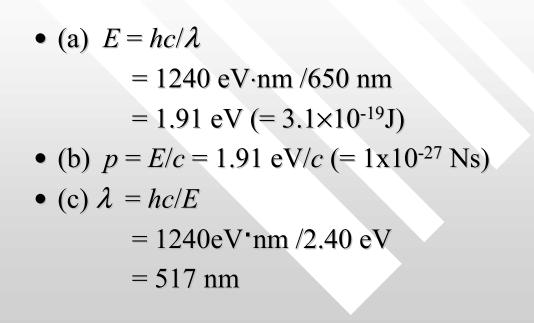
- The way how photon carries energy is in in contrast to the way wave carries energy.
- For wave the radiant energy is continuously distributed over a region in space and not in separate bundles
- (always recall the analogy of water in a hose and a stream of ping pong ball to help visualisation)



- With this assumption, a photon will have a momentum given by $p = E/c = h/\lambda$.
- This relation is obtained from SR relationship $E^2 = p^2 c^2 + (m_0 c^2)^2$, for which the mass of a photon is zero.
- Note that in classical physics momentum is intrinsically a particle attribute not defined for wave.
 By picturing light as particle (photon), the definition of momentum for radiation now becomes feasible



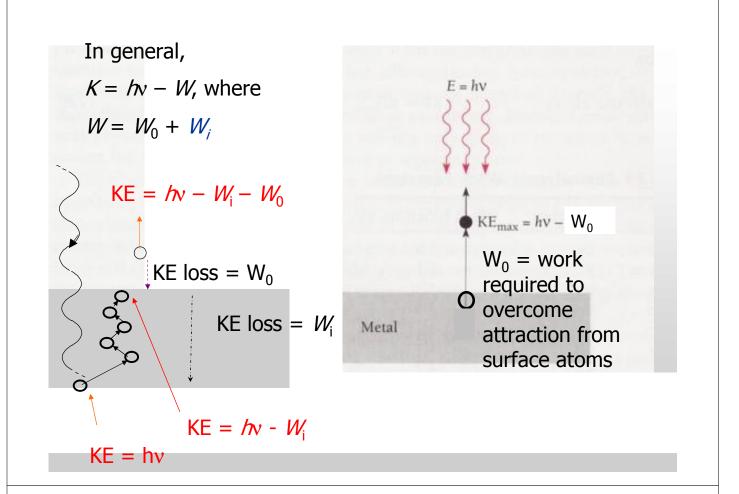
solution



Einstein's 2nd postulate

- In PE one photon is completely absorbed by one atom in the photocathode.
- Upon the absorption, one electron is 'kicked out' by the absorbent atom.
- The kinetic energy for the ejected electron is
 K = hv W
- *W* is the worked required to
- (i) cater for losses of kinetic energy due to internal collision of the electrons (W_i),
- (ii) overcome the attraction from the atoms in the surface (W_0)
- When no internal kinetic energy loss (happens to electrons just below the surface which suffers minimal loss in internal collisions), *K* is maximum:

•
$$K_{max} = hv - W_0$$



Einstein theory manage to solve the three unexplained features:

- First feature:
- In Einstein's theory of PE, $K_{max} = hv W_0$
- Both hv and W_0 do not depend on the radiation intensity
- Hence K_{max} is independent of irradiation intensity
- Doubling the intensity of light wont change K_{max} because only depend on the energy hv of individual photons and W_0
- *W*₀ is the intrinsic property of a given metal surface

Second feature explained

- The cut-off frequency is explained
- Recall that in Einstein assumption, a photon is completely absorbed by one atom to kick out one electron.
- Hence each absorption of photon by the atom transfers a discrete amount of energy by *hv* only.
- If *hv* is not enough to provide sufficient energy to overcome the required work function, *W*₀, no photoelectrons would be ejected from the metal surface and be detected as photocurrent

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Cut-off frequency is related to work function of metal surface $W_0 = h v_0$

- A photon having the cut-off frequency v_0 has just enough energy to eject the photoelectron and none extra to appear as kinetic energy.
- Photon of energy less than hv_0 has not sufficient energy to kick out any electron
- Approximately, electrons that are eject at the cut-off frequency will not leave the surface.
- This amount to saying that the have got zero kinetic energy: $K_{\text{max}} = 0$
- Hence, from $K_{\text{max}} = hv W_0$, we find that the cut-off frequency and the work function is simply related by

$$W_0 = h v_0$$

• Measurement of the cut-off frequency tell us what the $_{32}$ work function is for a given metal

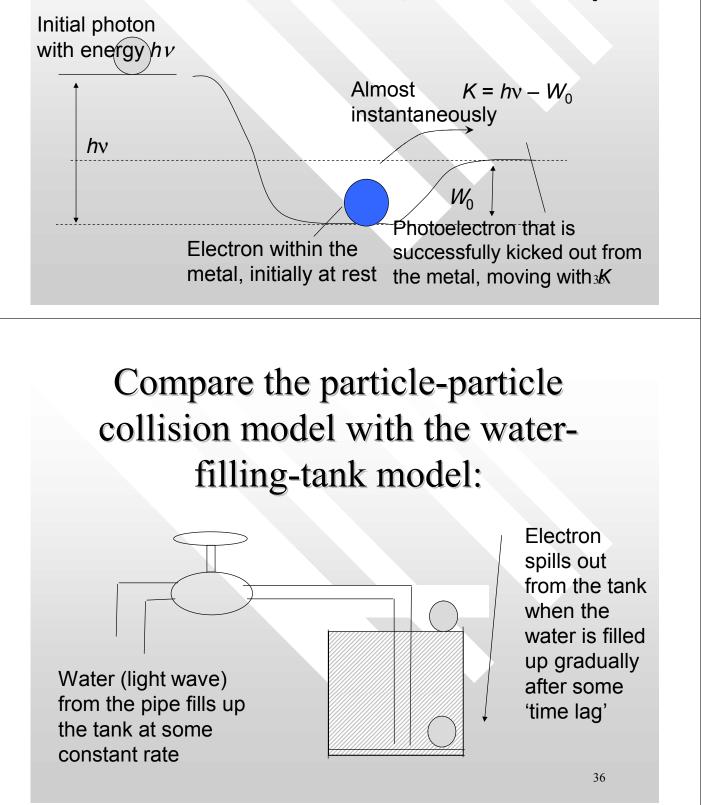
$E = hv_0$		Table 3.1 Some Photoelectric Work Functions $W_0 = hv_0$	
333		Material	W(eV
* * *		Na	2.28
		Al	4.08
		Co	3.90
		Cu	4.70
• KE = 0		Zn	4.31
1		Ag	4.73
0	Metal	Pt	6.35
The second second second second second		Pb	4.14

Third feature explained

- The required energy to eject photoelectrons is supplied in concentrated bundles of photons, not spread uniformly over a large area in the wave front.
- Any photon absorbed by the atoms in the target shall eject photoelectron immediately.
- Absorption of photon is a discrete process at quantum time scale (almost 'instantaneously'): it either got absorbed by the atoms, or otherwise.
- Hence no time lag is expected in this picture

A simple way to picture photoelectricity in terms of particleparticle collision:

Energy of photon is transferred during the instantaneous collision with the electron. The electron will either get kicked up against the barrier threshold of W_0 almost instantaneously, or fall back to the bottom of the valley if hv is less than W_0



Experimental determination of Planck constant from PE

- Experiment can measure eV_s (= K_{max}) for a given metallic surface (e.g. sodium) at different frequency of impinging radiation
- We know that the work function and the stopping potential of a given metal is given by

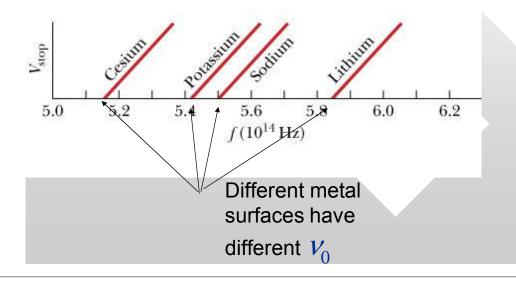
•
$$eV_s = hv - W_0$$

In experiment, we can measure the slope in the graph of V_s verses frequency v for different metal surfaces. It gives a universal value of $h/e = 4.1 \times 10^{-15}$ Vs. Hence, $h = 6.626 \times 10^{-34}$ Js

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 $V_s = (h/e) v - V_0$



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PYQ 2.16, Final Exam 2003/04

- Planck constant
- (i) is a universal constant
- (ii) is the same for all metals
- (iii) is different for different metals
- (iv) characterises the quantum scale
- **A.** I,IV **B.** I,II, IV **C.** I, III,IV
- **D.** I, III **E.** II, III
- ANS: B, Machlup, Review question 8, pg. 496, modified

PYQ 4(a,b) Final Exam 2003/04

- (a) Lithium, beryllium and mercury have work functions of 2.3 eV, 3.9 eV and 4.5 eV, respectively. If a 400-nm light is incident on each of these metals, determine
- (i) which metals exhibit the photoelectric effect, and
- (ii) the maximum kinetic energy for the photoelectron in each case (in eV)

Solution for Q3a

- The energy of a 400 nm photon is $E = hc/\lambda =$ 3.11 eV
- The effect will occur only in lithium*
- Q3a(ii)
- For lithium, $K_{\text{max}} = hv W_0$

= 3.11 eV - 2.30 eV= 0.81 eV

*marks are deducted for calculating "K_{max}" for beryllium and mercury which is meaningless

PYQ 4(a,b) Final Exam 2003/04

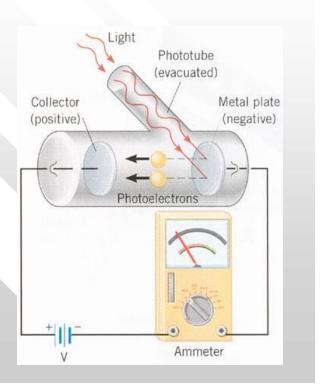
- (b) Molybdenum has a work function of 4.2 eV.
- (i) Find the cut-off wavelength (in nm) and threshold frequency for the photoelectric effect.
- (ii) Calculate the stopping potential if the incident radiation has a wavelength of 180 nm.

Solution for Q4b

- Q3a(ii)
- Known $h v_{\text{cutoff}} = W_0$
- Cut-off wavelength = $\lambda_{\text{cutoff}} = c/\nu_{\text{cutoff}}$ = hc/W_0 = 1240 nm eV / 4.2 eV = **295 nm**
- Cut-off frequency (or threshold frequency), $v_{\text{cutoff}} = c / \lambda_{\text{cutoff}} = 1.01 \text{ x } 1015 \text{ Hz}$
- Q3b(ii)
- Stopping potential $V_{\text{stop}} = (hc/\lambda W_0) / e = (1240 \text{ nm} \cdot \text{eV}/180 \text{ nm} 4.2 \text{ eV}) / e = 2.7 \text{ V}$

Example (read it yourself)

- Light of wavelength 400 nm is incident upon lithium $(W_0 = 2.9 \text{ eV})$. Calculate
- (a) the photon energy and
- (b) the stopping potential, $V_{\rm s}$
- (c) What frequency of light is needed to produce electrons of kinetic energy 3 eV from illumination of lithium?



Solution:

- (a) $E = hv = hc/\lambda = 1240 \text{eV} \cdot \text{nm}/400 \text{ nm} = 3.1 \text{ eV}$
- (b) The stopping potential x e = Max Kinetic energy of the photon

• =>
$$eV_s = K_{max} = hv - W_0 = (3.1 - 2.9) eV$$

- Hence, $V_s = 0.2 \text{ V}$
- i.e. a retarding potential of 0.2 V will stop all photoelectrons
- (c) $hv = K_{max} + W_0 = 3 \text{ eV} + 2.9 \text{ eV} = 5.9 \text{ eV}.$ Hence the frequency of the photon is $v = 5.9 \text{ x} (1.6 \text{ x} 10^{-19} \text{ J}) / 6.63 \text{ x} 10^{-34} \text{ Js}$ $= 1.42 \text{ x} 10^{15} \text{ Hz}$

PYQ, 1.12 KSCP 2003/04

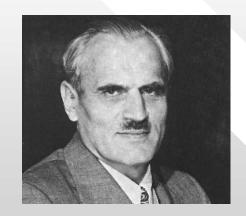
Which of the following statement(s) is (are) true?

- I The energy of the quantum of light is proportional to the frequency of the wave model of light
- II In photoelectricity, the photoelectrons has as much energy as the quantum of light which causes it to be ejected
- III In photoelectricity, no time delay in the emission of photoelectrons would be expected in the quantum theory
- A. II, III B. I, III C. I, II, III D. I ONLY
- E. Non of the above
- Ans: B
- Murugeshan, S. Chand & Company, New Delhi, pg. 136, Q28 (for I), Q29, Q30 (for II,III)

To summerise: In photoelectricity (PE), light behaves like particle rather than like wave.

Compton effect

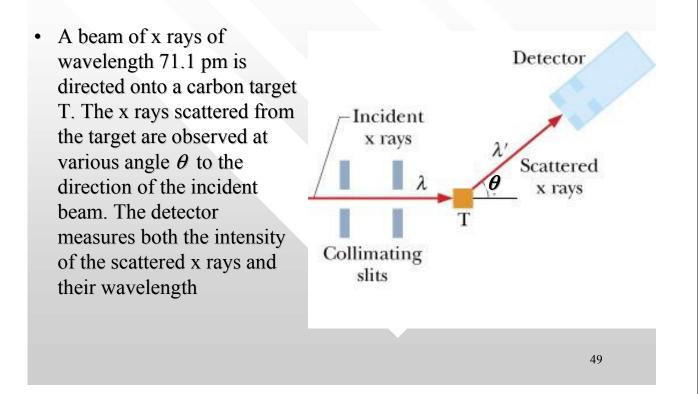
• Another experiment revealing the particle nature of X-ray (radiation, with wavelength $\sim 10^{-10}$ m)



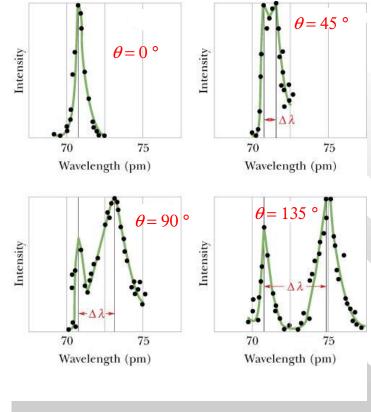
Compton, Arthur Holly (1892-1962), American physicist and Nobel laureate whose studies of <u>X rays</u> led to his discovery in 1922 of the so-called Compton effect.

The Compton effect is the change in wavelength of high energy <u>electromagnetic</u> <u>radiation</u> when it scatters off <u>electrons</u>. The discovery of the Compton effect confirmed that electromagnetic radiation has both wave and particle properties, a central principle of <u>quantum theory</u>.

Compton's experimental setup



Experimental data



Although initially the incident beam consists of only a single well-defined wavelength (λ) the scattered x-rays at a given angle θ have intensity peaks at two wavelength (λ ' in addition), where $\lambda' > \lambda$

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Compton shouldn't shift, according to classical wave theory of light

- Unexplained by classical wave theory for radiation
- No shift of wavelength is predicted in wave theory of light

Modelling Compton shift as "particle-particle" collision

- Compton (and independently by Debye) explain this in terms of collision between collections of (particle-like) photon, each with energy E = hv = pc, with the *free* electrons in the target graphite (imagine billard balls collision)
- $E^2 = (mc^2)^2 + c^2 p^2$

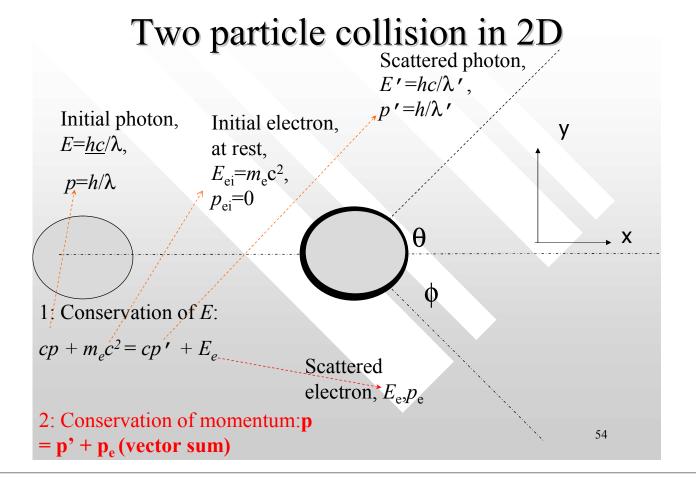
• $E_{\nu}^{2} = (m_{\nu}c^{2})^{2} + c^{2}p^{2} = c^{2}p^{2}$

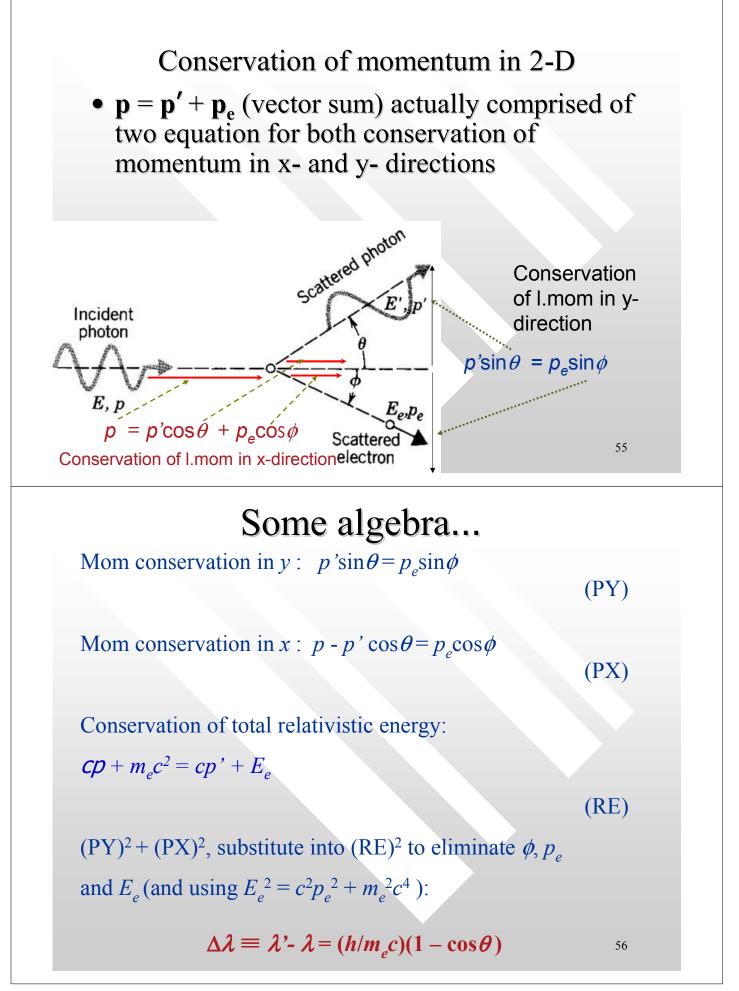
Photographic picture of a Compton electron

- Part of a bubble chamber picture (Fermilab'15 foot Bubble Chamber', found at the University of Birmingham). An electron was knocked out of an atom by a high energy photon.
- Photon is not shown as the photographic plate only captures the track of charged particle, not light.

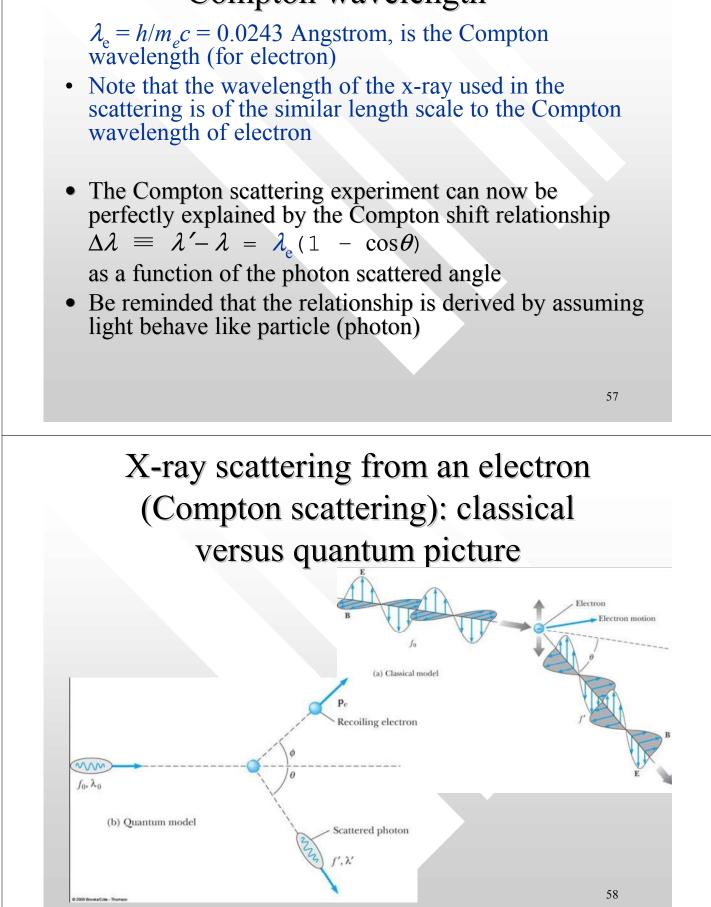


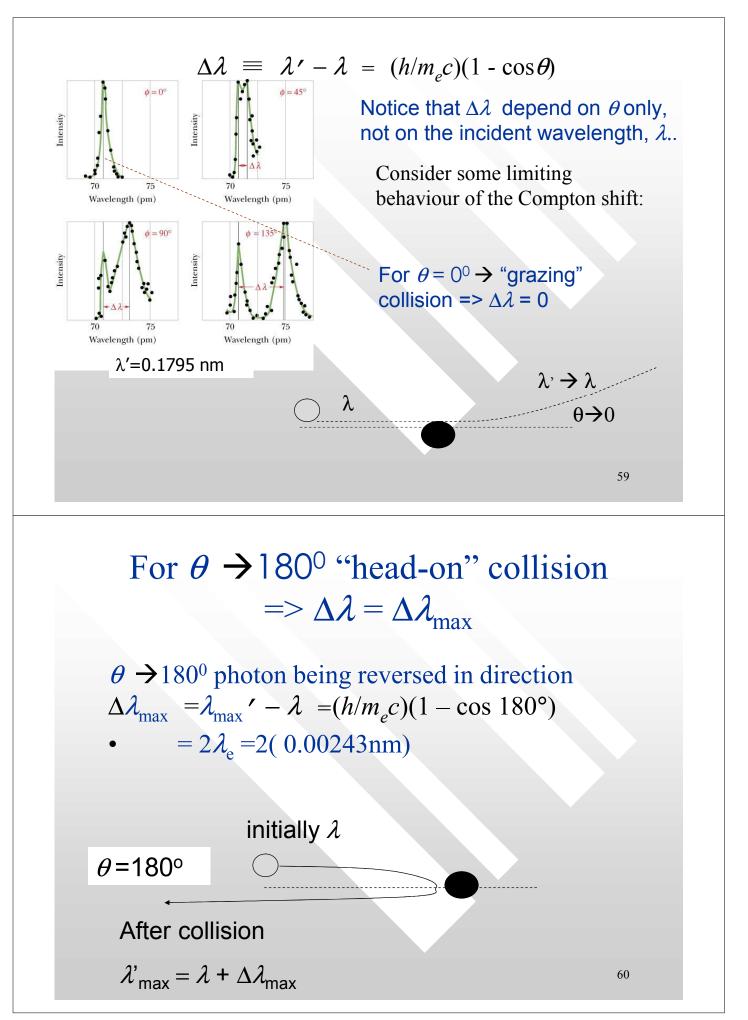






Compton wavelength





PYQ 2.2 Final Exam 2003/04

Suppose that a beam of 0.2-MeV photon is scattered by the electrons in a carbon target. What is the wavelength of those photon scattered through an angle of 90°?

- A. 0.00620 nm
- B. 0.00863 nm
- C. 0.01106 nm
- D. 0.00243 nm
- E. Non of the above

Solution

First calculate the wavelength of a 0.2 MeV photon: $E = hc/\lambda = 1240 \text{ eV} \cdot \text{nm}/\lambda = 0.2 \text{ MeV}$

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 $\lambda = 1240 \text{ nm} / 0.2 \text{ x} 10^6 = 0.062 \text{ nm}$

From Compton scattering formula, the shift is $\Delta \lambda = \lambda' - \lambda = \lambda_e (1 - \cos 90^\circ) = \lambda_e$ Hence, the final wavelength is simply $\lambda' = \Delta \lambda + \lambda = \lambda_e + \lambda = 0.00243 \text{nm} + 0.062 \text{ nm} = 0.00863$ nm

ANS: B, Schaum's 3000 solved problems, Q38.31, pg. 712

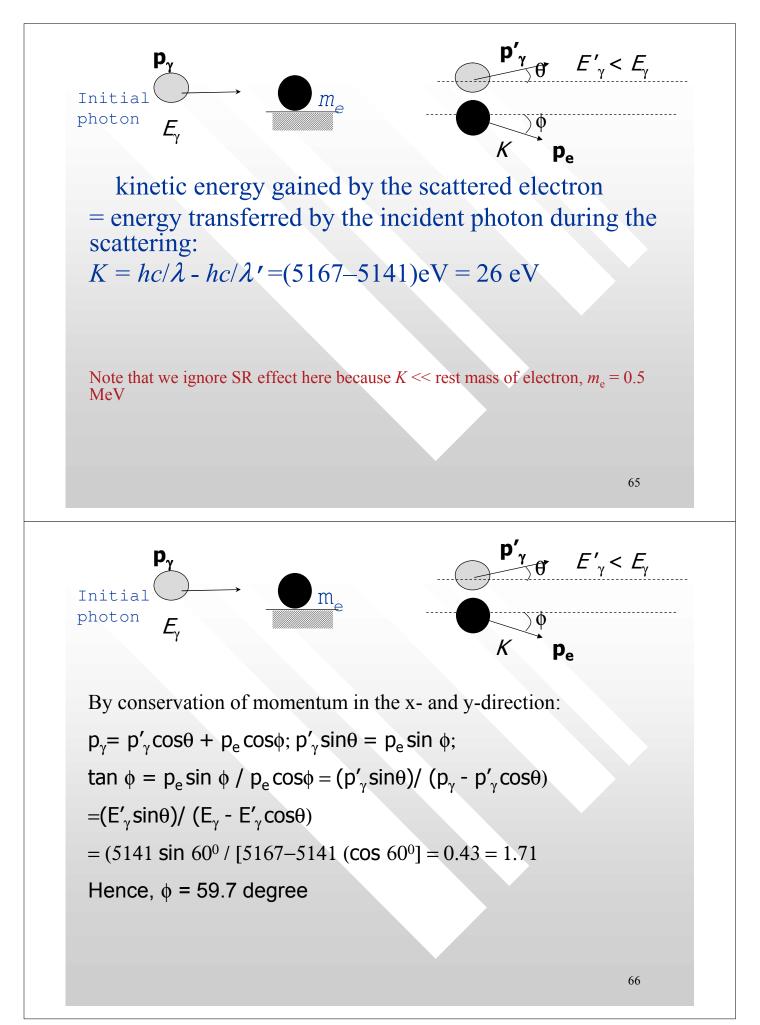
Example

- X-rays of wavelength 0.2400 nm are Compton scattered and the scattered beam is observed at an angle of 60 degree relative to the incident beam.
- Find (a) the wave length of the scattered xrays, (b) the energy of the scattered x-ray photons, (c) the kinetic energy of the scattered electrons, and (d) the direction of travel of the scattered electrons

solution

 $\lambda' = \lambda + \lambda_e (1 - \cos \theta)$ = 0.2400nm+0.00243nm(1-cos60°) = 0.2412 nm

 $E' = hc/\lambda'$ = 1240 eV·nm /0.2412 nm = 5141 eV



PYQ 3(c), Final exam 2003/04

- (c) A 0.0016-nm photon scatters from a free electron. For what scattering angle of the photon do the recoiling electron and the scattered photon have the same kinetic energy?
- Serway solution manual 2, Q35, pg. 358

Solution

- The energy of the incoming photon is $E_i = hc/\lambda = 0.775 \text{ MeV}$
- Since the outgoing photon and the electron each have half of this energy in kinetic form,
- $E_f = hc/\lambda' = 0.775 \text{ MeV} / 2 = 0.388 \text{ MeV}$ and $\lambda' = hc/E_f = 1240 \text{ eV} \cdot \text{nm} / 0.388 \text{ MeV} = 0.0032 \text{ nm}$
- The Compton shift is $\Delta \lambda = \lambda' - \lambda = (0.0032 - 0.0016) \text{ nm} = 0.0016 \text{ nm}$
- By $\Delta \lambda = \lambda_c (1 \cos \theta)$

•
$$= (h/m_e c) (1 - \cos \theta) 0.0016 \text{ nm}$$

• =
$$0.00243 \text{ nm} (1 - \cos \theta)$$

$$\theta = 70^{\circ}$$

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PYQ 1.10 KSCP 2003/04

Which of the following statements is (are) true?

- I. Photoelectric effect arises due to the absorption of electrons by photons
- II. Compton effect arises due to the scattering of photons by free electrons
- **III.** In the photoelectric effect, only part of the energy of the incident photon is lost in the process
- IV. *I*n the Compton effect, the photon completely disappears and all of its energy is given to the Compton electron
- A. I,II
- B. II,III,IV
- C. I, II, III

- D. III,IV Ans: E
- [I = false; II = true; III = false; IV = false]
- Murugeshan, S. Chand & Company, New Delhi, pg. 134, Q13,

X-ray: The inverse of photoelectricity

X-ray, discovered by Wilhelm Konrad Roentgen (1845-1923). He won the first Nobel prize in 1902. He refused to benefit financially from his work and died in poverty in the German inflation that followed the end of World War 1.



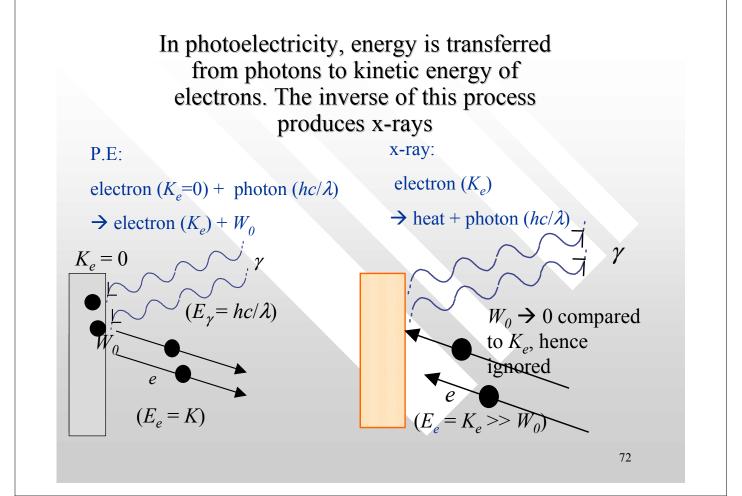
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X-rays are simply EM radiation with very short wavelength, $\sim 0.01 \text{ nm} - 10 \text{ nm}$

Some properties:

- energetic, according to $E = hc/\lambda \sim 0.1 100 \text{ keV}$ (c.f. $E \sim a$ few eV for visible light)
- travels in straight lines
- is unaffected by electric and magnetic fields
- passes readily through opaque materials highly penetrative
- causes phosphorescent substances to glow
- exposes photographic plates

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PE and x-rays production happen at different energy scale

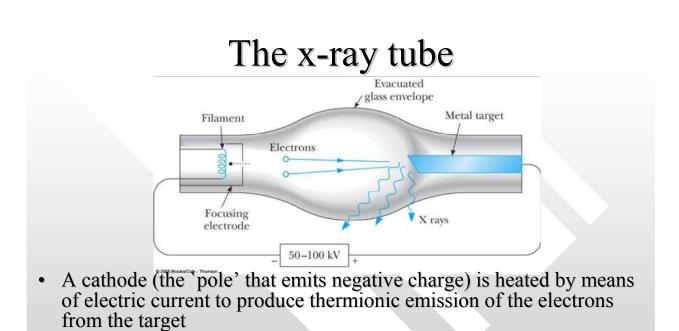
- However, both process occur at disparately different energy scale
- Roughly, for PE, it occurs at eV scale with ultraviolet radiation
- For x-ray production, the energy scale involved is much higher at the order of 100 eV 100 keV

X-ray production

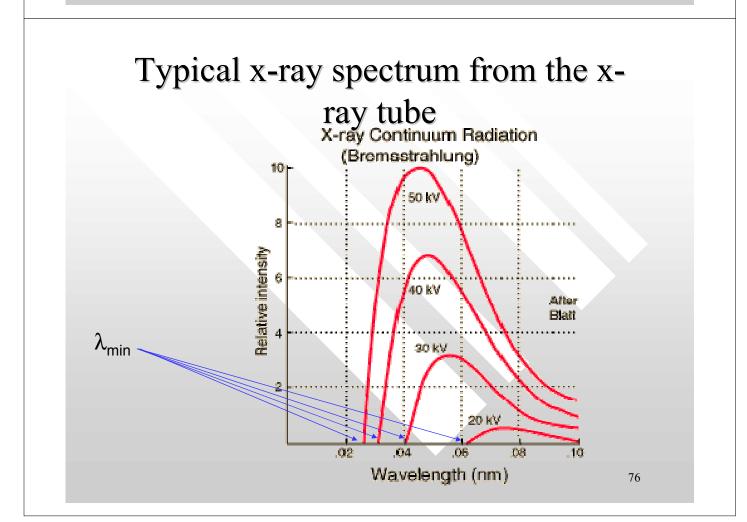
е

K

- X-rays is produced when electrons, accelerated by an electric field in a vacuum cathode-ray tube, are impacted on the glass end of the tube
- Part or all of the kinetic energy of a moving electron is converted into a x-ray photon



- A high potential difference V is maintained between the cathode and a metallic target
- The thermionic electrons will get accelerated toward the latter
- The higher the accelerating potential *V*, the faster the electron and the shorter the wavelengths of the x-rays 75

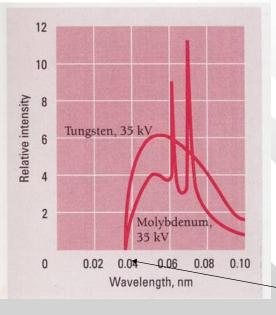


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Important features of the x-ray spectrum

- 1. The spectrum is continuous
- 2. The existence of a minimum wavelength λ_{\min} for a given *V*, below which no x-ray is observed
- 3. Increasing V decreases λ_{\min}

$\lambda_{\min} \propto 1/V$, the same for all material surface



At a particular V, λ_{min} is approximately the same for different target materials.
Experimentally one finds that λ_{min} is inversely proportional to V,

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Wavelength, nm $\lambda_{\min} = \left(\frac{1.24 \times 10^{-6}}{V}\right) \text{m} \cdot \text{V}$ The peaks in the spectrum are due to the electronic transition occurring between the adjacent shells (orbit) in the atom. We would not discuss them further here.

X-ray production heats up the target material

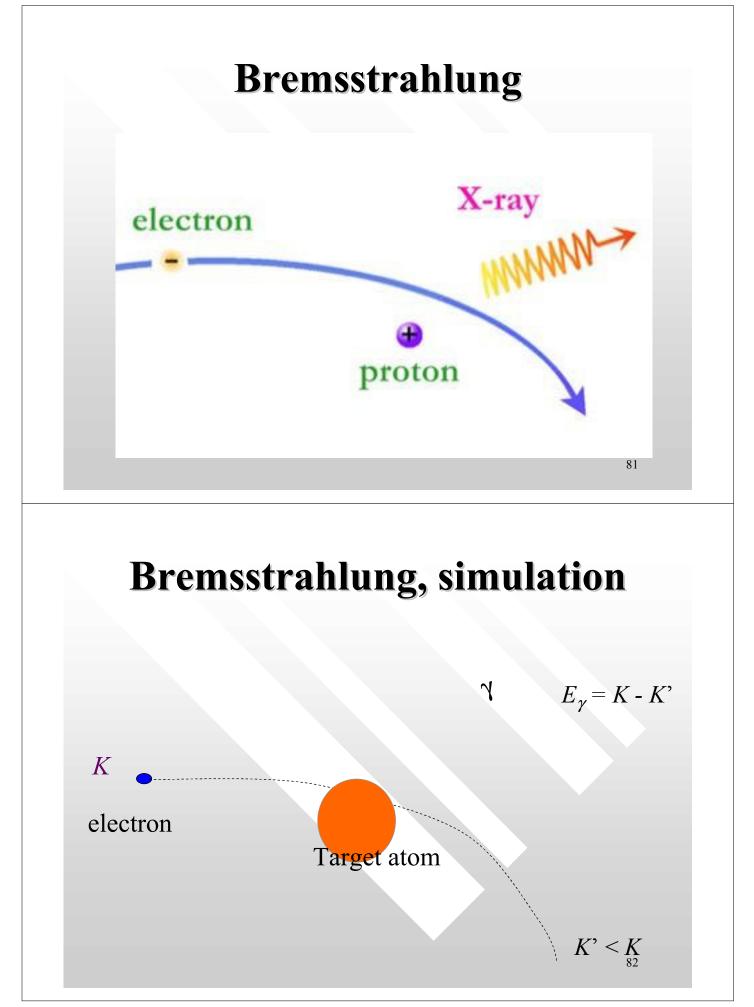
- Due to conversion of energy from the impacting electrons to x-ray photons is not efficient, the difference between input energy, K_e and the output x-ray energy E_{γ} becomes heat
- Hence the target materials have to be made from metal that can stand heat and must have high melting point (such as Tungsten and Molybdenum)

Classical explanation of continuous x-

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ray spectrum:

- The continuous X-ray spectrum is explained in terms of Bremsstrahlung: radiation emitted when a moving electron "tekan brake"
- According to classical EM theory, an accelerating or decelerating electric charge will radiate EM radiation
- Electrons striking the target get slowed down and brought to eventual rest because of collisions with the atoms of the target material
- Within the target, many electrons collides with many atoms for many times before they are brought to rest
- Each collision causes some non-unique losses to the kinetic energy of the Bremsstrahlung electron
- As a net effect of the collective behavior by many individual collisions, the radiation emitted (a result due to the lost of KE of the electron) forms a continuous spectrum



Bremsstrahlung cannot explain

• Notice that in the classical **Bremsstrahlung** process the x-ray radiated is continuous and there is no lower limit on the value of the wavelength emitted (because classical physics does not relate energy with wavelength). Hence, the existence of λ_{min} is not explained with the classical **Bremsstrahlung** mechanism. All range of λ from 0 to a maximum should be possible in this classical picture.

 λ_{\min} can only be explained by assuming light as photons but not as EM wave ⁸³

Energy of the x-ray photon in the quantum picture

• According to Einstein assumption on the energy of a photon, the energy of the photon emitted in the Bremsstrahlung is simply the difference between the initial and final kinetic energy of the electron:

$$hv = K - K'$$

- The shortest wavelength of the emitted photon gains its energy, $E = hv_{max} = hc/\lambda_{min}$ corresponds to the maximal loss of the K.E. of an electron in a single collision (happen when K' = 0 in a single collision)
- This (i.e. the maximal lose on KE) only happens to a small sample of collisions. Most of the other collisions loss their KE gradually in smaller amount in an almost continuous manner.

Theoretical explanation of the experimental Value of λ_{min}

- *K* (of the Bremsstrahlung electron) is converted into the photon with $E = hc/\lambda_{min}$
- Experimentally *K* is caused by the external potential *V* that accelerates the electron before it bombards with the target, hence

$$K = eV$$

• Conservation of energy requires

$$K = eV = hc/\lambda_{\min}$$

• or, $\lambda_{\min} = hc/eV = (1240 \text{ nm} \cdot \text{eV})/eV = (1240 \text{V}/V) \text{ nm}$ which is the value measured in x-ray experiments

Why is λ_{\min} the same for different material?

- The production of the x-ray can be considered as an inverse process of PE
- Hence, to be more rigorous, the conservation of energy should take into account the effects due to the work potential of the target material during the emission of x-ray process, W_0
- However, so far we have ignored the effect of W_0 when we were calculating the relationship between λ_{\min} and K
- This approximation is justified because of the following reason:
- The accelerating potentials that is used to produce x-ray in a x-ray vacuum tube, *V*, is in the range of 10,000 V
- Whereas the work function W_0 is only of a few eV
- Hence, in comparison, W_0 is ignored wrp to eV
- This explains why λ_{\min} is the same for different target materials

Example

• Find the shortest wavelength present in the radiation from an x-ray machine whose accelerating potential is 50,000 V

• Solution:
$$\lambda_{\min} = \frac{hc}{eV} = \frac{1.24 \times 10^{-6} \,\mathrm{V} \cdot \mathrm{m}}{5.00 \times 10^{4} \,\mathrm{V}} = 2.48 \times 10^{-11} \,\mathrm{m} = 0.0248 \,\mathrm{nm}$$

This wavelength corresponds to the frequency

$$v_{\text{max}} = \frac{c}{\lambda_{\text{min}}} = \frac{3 \times 10^8 \,\text{m/s}}{2.48 \times 10^{-11} \,\text{m}} = 1.21 \times 10^{19} \,\text{Hz}$$

PYQ 1. 9 Final Exam 2003/04

- To produce an x-ray quantum energy of 10⁻¹⁵ J electrons must be accelerated through a potential difference of about Solution.
- A. 4 kV The energy of the x-rays photon comes from the
- B. 6 kV external accelerating potential, V
- C. 8 kV $E_{\lambda} = eV$
- D. 9 kV

• E. 10 kV
$$V = E_{\lambda} / e = 1 \times 10^{-15} \text{ J/}e = \left(\frac{1 \times 10}{1.6 \times 10^{-19}}\right) \text{eV}/e = 6250 \text{ V}$$

 1×10^{-15}

• ANS: B, OCR ADVANCED SUBSIDIARY GCE PHYSICS B (PDF), Q10, pg. 36

PYQ 1.9 KSCP 2003/04

Which of the following statement(s) is (are) true?

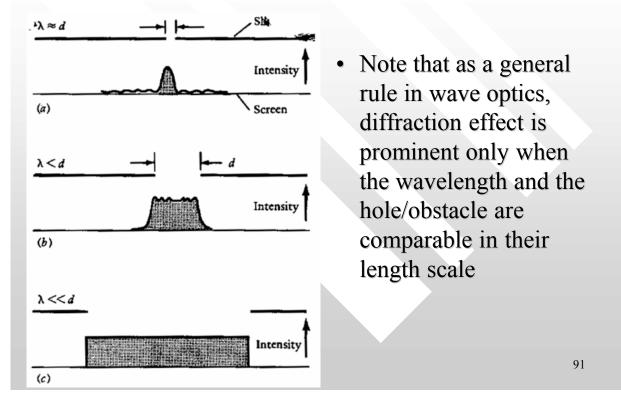
- I. γ -rays have much shorter wavelength than *x*-rays
- II. The wavelength of *x*-rays in a *x*-ray tube can be controlled by varying the accelerating potential
- III. *x*-rays are electromagnetic waves
- **IV.** *x*-rays show diffraction pattern when passing through crystals
- A. I,II B. I,II,III,IV C. I, II, III
- **D. III.IV E.** Non of the above
- Ans: B Murugeshan, S. Chand & Company, New Delhi, pg. 132, Q1.(for I), pg. 132, Q3 (for II), pg. 132, Q4 (for III,IV)

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X-ray diffraction

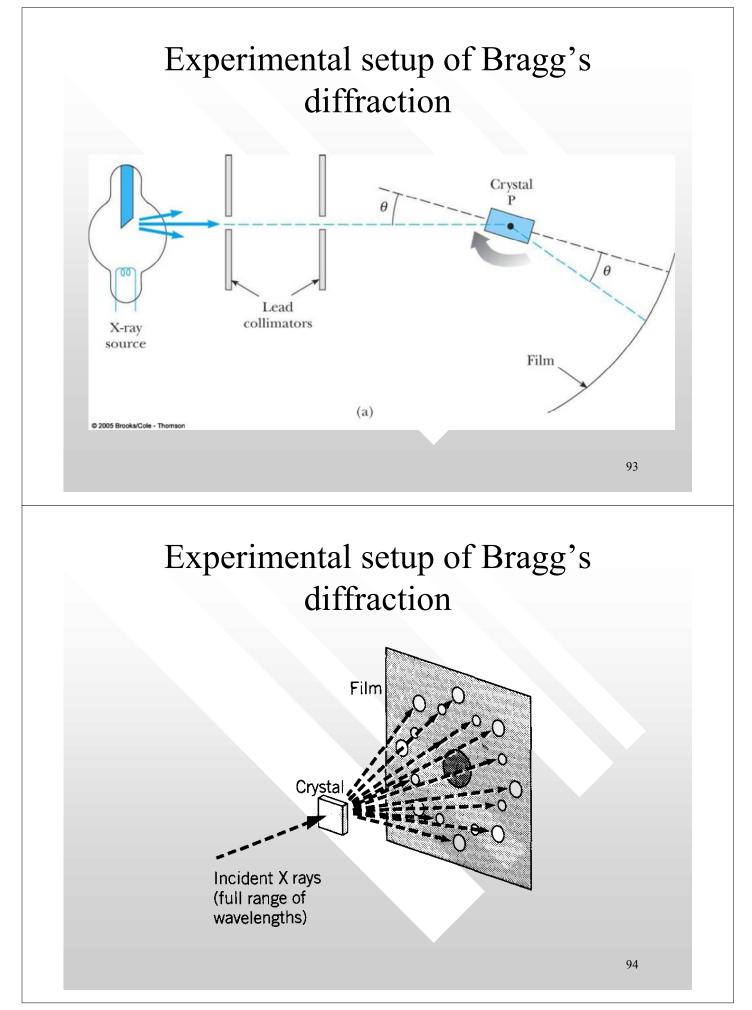
- X-ray wavelengths can be determined through diffraction in which the x-ray is diffracted by the crystal planes that are of the order of the wavelength of the x-ray, ~ 0.1 nm
- The diffraction of x-ray by crystal lattice is called 'Bragg's diffraction'
- It is also used to study crystal lattice structure (by analysing the diffraction pattern)

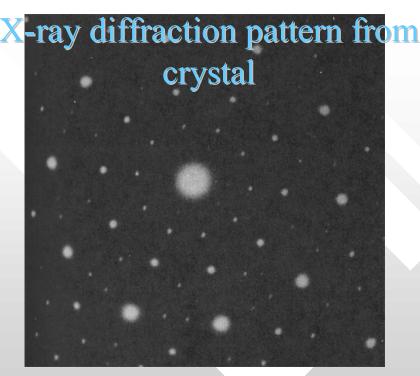
Condition for diffraction



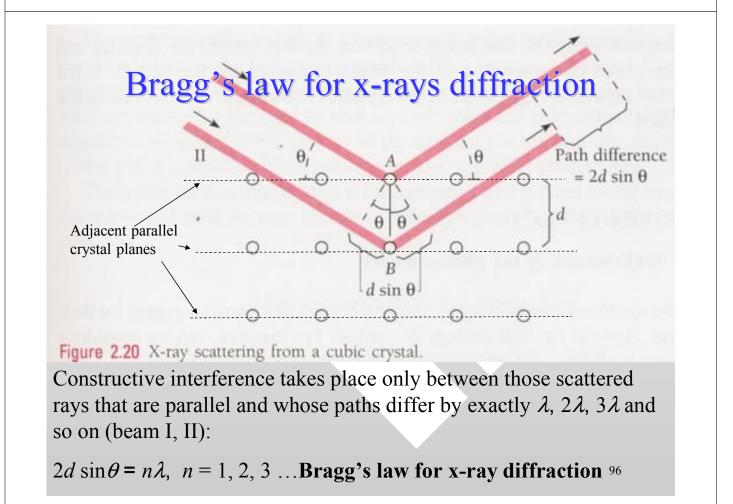
Use atoms in a crystal lattice to diffract X-rays

- Since wavelength of x-rays is very small, what kind of "scatterer" has sufficiently tiny separation to produce diffraction for x-rays?
- ANS: Atoms in a crystal lattice. Only the atomic separation in a crystal lattice is small enough (~ nm) to diffract X-rays which are of the similar order of length scale.





The bright spots correspond to the directions where x-rays (full ranges of wavelengths) scattered from various layers (different Braggs planes) in the crystal interfere constructively.



An X-rays can be reflected from many different crystal planes

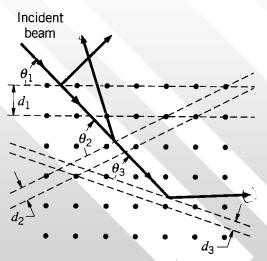


FIGURE 3.6 An incident beam of X rays can be reflected from many different crystal planes.

Example

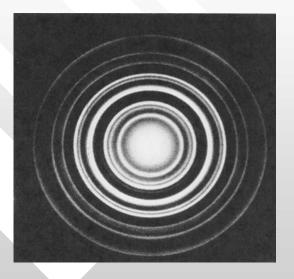
 A single crystal of table salt (NaCl) is irradiated with a beam of x-rays of unknown wavelength. The first Bragg's reflection is observed at an angle of 26.3 degree. Given that the spacing between the interatomic planes in the NaCl crystal to be 0.282 nm, what is the wavelength of the x-ray?

Solution

• Solving Bragg's law for the n = 1 order, $\lambda = 2d \sin \theta = 2 \times 0.282 \text{ nm} \times \sin (26.3^{\circ})$ = 0.25 nm $0 \sin \theta = 1 \text{ order:}$ $2d \sin \theta = \lambda$ $0 \sin \theta = \lambda$ $0 \sin \theta = \lambda$

If powder specimen is used (instead of single crystal)

• We get diffraction ring due to the large randomness in the orientation of the planes of scattering in the power specimen



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Why ring for powdered sample?

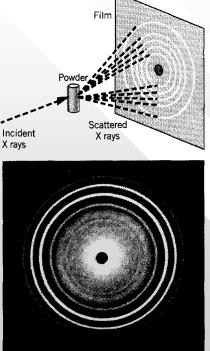


FIGURE 3.9 (Top) Apparatus for observing X-ray scattering from a powdered sample. Because the many crystals in a powder have all possible different orientations, each scattered ray of Figure 3.7 becomes a cone which forms a circle on the film. (Bottom) Diffraction pattern (known as *Debye-Scherrer* pattern) of a powder sample.

X-rays "finger print" of crystals

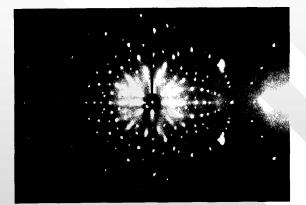


FIGURE 3.7 (Top) Apparatus for observing X-ray scattering by a crystal. An interference maximum (dot) appears on the film whenever a set of crystal planes happens to satisfy the Bragg condition for a particular wavelength. (Bottom) Laue pattern of NaCl crystal.

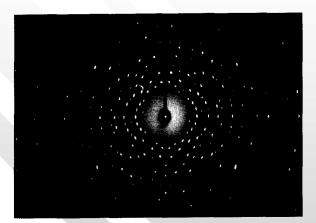
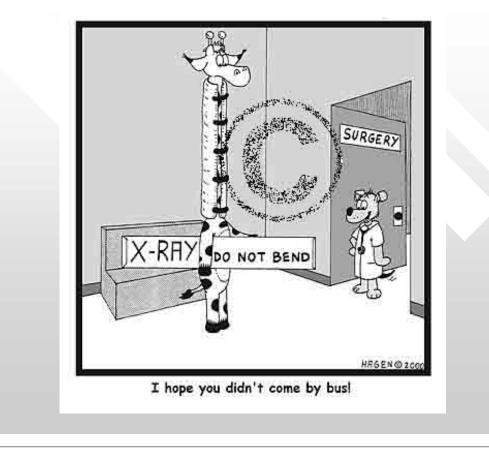


FIGURE 3.8 Laue pattern of a quartz crystal. The difference in crystal structure and spacing between quartz and NaCl makes this pattern look different from Figure 3.7.

PYQ 6 Test I, 2003/04

- X-ray of wavelength 1.2 Angstrom strikes a crystal of *d*-spacing 4.4 Angstrom. Where does the diffraction angle of the second order occur?
- A.16° B. 33° C.55 °
- **D.** 90° **E.** Non of the above
- Solution: $n\lambda = 2d \sin \theta$
- $\sin\theta = n\lambda/2d = 2 \ge 2.2 / (2 \ge 4.4) = 0.5$ $\theta = 30$ °
- ANS: B, Schaum's 3000 solved problems, Q38.46, pg. 715



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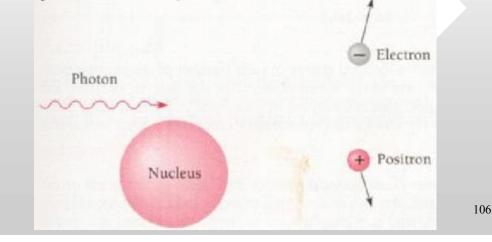
Pair Production: Energy into matter

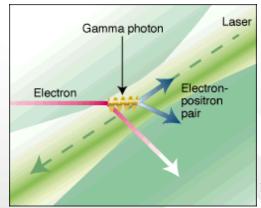
- In photoelectric effect, a photon gives an electron all of its energy. In Compton effect, a photon give parts of its energy to an electron
- A photon can also materialize into an electron and a positron
- Positron = anti-electron, positively charged electron with the exactly same physical characteristics as electron except opposite in charge and spin
- In this process, called pair production, electromagnetic energy is converted into matter
- Creation of something (electron-positron pair) out of nothing (pure EM energy) triggered by strong external EM field

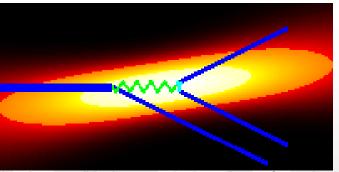
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Pictorial visualisation of pair production

• In the process of pair production, a photon of sufficient energy is converted into electron-positron pair. The conversion process must occur only in the presence of some external EM field (such as near the vicinity of a nucleus)







An electron (blue) enters the laser beam from the left, and collides with a laser photon to produce a high-energy gamma ray (wiggly yellow line). The electron is deflected downwards. The gamma ray then collides with four or more laser photons to produce an electron-positron pair

Boom! From Light Comes Matter



Conservational laws in pairproduction

- The pair-production must not violate some very fundamental laws in physics:
- Charge conservation, total linear momentum, total relativistic energy are to be obeyed in the process
- Due to kinematical consideration (energy and linear momentum conservations) pair production cannot occur in empty space
- Must occur in the proximity of a nucleus
- Will see this in an example

Energy threshold

- Due to conservation of relativistic energy, pair production can only occur if E_{γ} is larger than 2 $m_e = 2 \times 0.51$ MeV = 1.02 MeV
- Any additional photon energy becomes kinetic energy of the electron and positron, K

$$E_{\gamma} = \frac{nc}{\lambda} = 2m_e c^2 + K$$

nucleus

09

Example

- What is the minimal wavelength of a EM radiation to pair-produce an electron-positron pair?
- Solutions: minimal photon energy occurs if the pair have no kinetic energy after being created, *K* = 0. Hence,

 $\lambda_{\min} = \frac{hc}{2m_e c^2} = \frac{1240 \,\mathrm{nm} \cdot \mathrm{eV}}{2 \cdot 0.51 \,\mathrm{MeV}} = 1.21 \times 10^{-12} \,\mathrm{m}$

These are very energetic EM radiation called gamma rays and are found in nature as one of the emissions from radioactive nuclei and in cosmic rays.

Electron-positron creation

incident photon

111

electror

р

θ

θ

 Part of a bubble chamber picture (Fermilab'15 foot Bubble Chamber', found at the University of Birmingham). The curly line which turns to the left is an electron. Positron looks similar but turn to the right The magnetic field is perpendicular to the picture plan

Pair Production cannot occur in empty space

- Conservation of energy must me fulfilled, $hf = 2mc^2$
- Conservation of linear momentum must be fulfilled:

$$E_{\gamma} = h f_{\gamma}$$

•
$$\Rightarrow p_{\gamma} = hf/c = 2p \cos \theta$$

- Since p = mv for electron and positron,
- $\Rightarrow hf = 2c(mv) \cos \theta = 2mc^2 (v/c) \cos \theta$
- Because v/c < 1 and $\cos \theta \le 1$, $hf < 2mc^2$
- But conservation of energy requires $hf = 2mc^2$. Hence it is impossible for pair production to conserve both energy and momentum unless some other object (such as a nucleus) in involved in the process to carry away part of the initial of the photon momentum

Pair-annihilation

• The inverse of pair production occurs when a positron is near an electron and the two come together under the influence of their opposite electric charges

$$e^+ + e^- \rightarrow \gamma + \gamma$$

- Both particles vanish simultaneously, with the lost masses becoming energies in the form of two gamma-ray photons
- Positron and electron annihilate because they are anti particles to each other

Before

 (e^{-})

Pair annihilation

• Part of a bubble-chamber picture from a neutrino experiment performed at the Fermilab (found at the University of Birmingham). A positron in flight annihilate with an electron. The photon that is produced materializes at a certain distance, along the line of flight, resulting a new electron-positron pair (marked with green)



After

Initial energy = $2m_ec^2 + K$

Final energy = $hc/\lambda + hc/\lambda$

Conservation of relativistic energy:

 $2m_e c^2 + K = 2 h c / \lambda$

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Energy and linear momentum are always conserved in pair annihilation

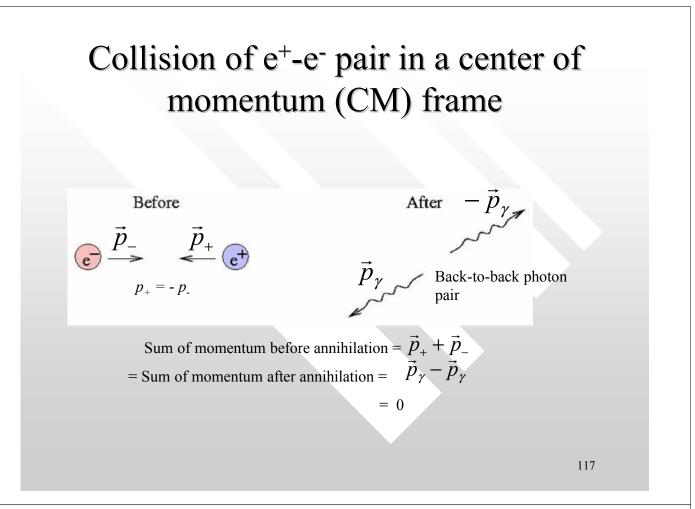
• The total relativistic energy of the e^--e^+ pair is

• $E = 2m_e c^2 + K = 1.02 \text{ MeV} + K$

- where K the total kinetic energy of the electron-positron pair before annihilation
- Each resultant gamma ray photon has an energy

$$hf = 0.51 \text{ MeV} + K/2$$

- Both energy and linear momentum are automatically conserved in pair annihilation (else it wont occur at all)
- For e⁻-e⁺ pair annihilation in which each particle collide in a head-on manner with same magnitude of momentum, i.e., $p_+ = -p_-$, the gamma photons are always emitted in a back-to-back manner due to kinematical reasons (conservation of linear momentum). (see explanation below and figure next page)
- In such a momentum-symmetric collision, the sum of momentum of the system is zero. Hence, after the photon pair is created, the sum their momentum must also be zero. Such kinematical reason demands that the photon pair be emitted back-to-back.
- No nucleus or other particle is needed for pair annihilation to take place
- Pair annihilation always occurs whenever a matter comes into contact with its antimatter



As a tool to observe anti-world

- What is the characteristic energy of a gamma-ray that is produced in a pair-annihilation production process? What is its wavelength?
- Answer: 0.51 MeV, $\lambda_{annih} = hc / 0.51$ MeV = 0.0243 nm
- The detection of such characteristic gamma ray in astrophysics indicates the annihilation of matterantimatter in deep space

PYQ 4, Test I, 2003/04

- An electron and a positron collide and undergo pair-annihilation. If each particle is moving at a speed of 0.8*c* relative to the laboratory before the collision, determine the energy of each of the resultant photon.
- **A.** 0.85MeV **B.** 1.67 MeV
- **C.** 0.51 MeV **D.** 0.72MeV
- E. Non of the above

Solution

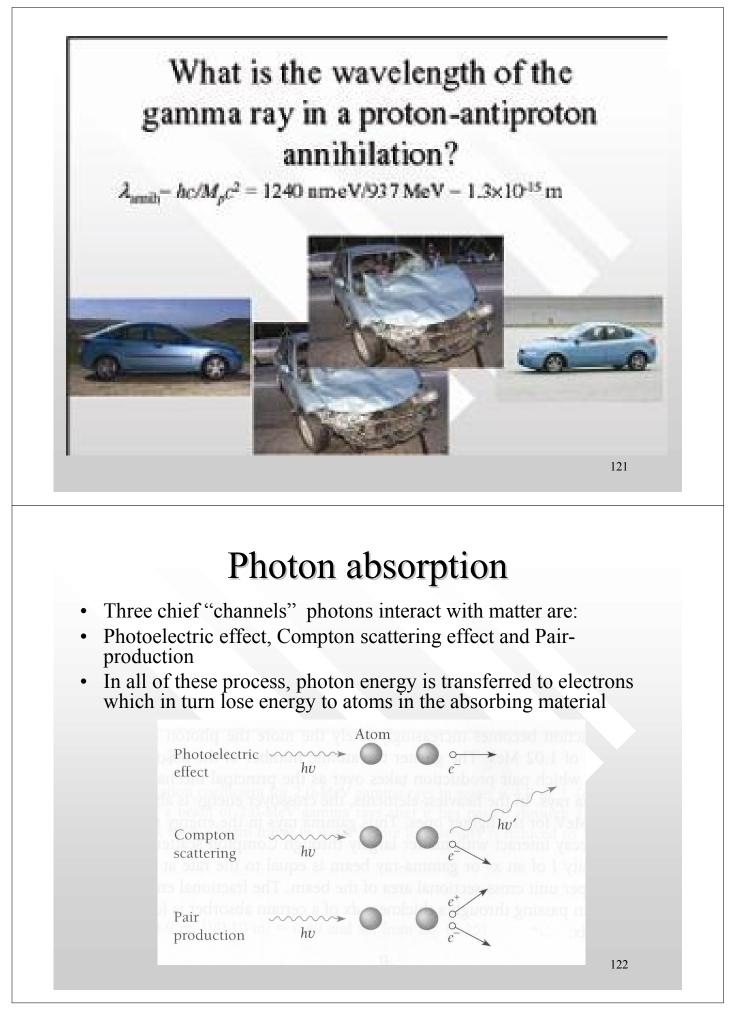
Total energy before and after annihiation must remain the same: *i.e.* the energy of each electron is converted into the energy of each photon. Hence the energy of each photon is simple equal to the total relativistic energy of each electron travelling at 0.8c:

$$E_{\gamma} = E_e = \gamma m_e c^2$$

where $\gamma = 1/\sqrt{1 - (0.8)^2} = 1.678$ Hence $E_{\gamma} = 1.678 \times 0.51$ MeV = 0.85 MeV

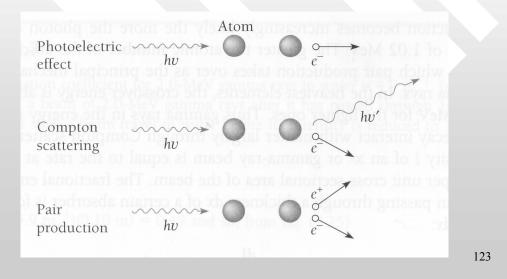
• ANS: A, Cutnell, Q17, pg. 878, modified

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Photon absorption

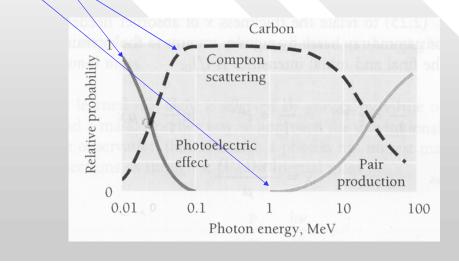
- The probability (cross section) of a photon undergoes a given channel of interaction with matter depends on
- (1) Photon energy, and
- (2) Atomic number of the absorbing material



Relative probabilities of photon absorption channels For a fixed atomic number (say Carbon, A = 12)

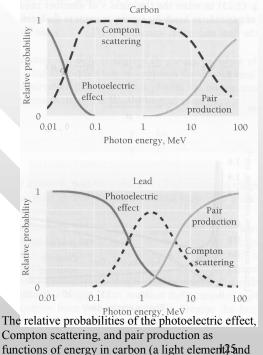
- At low energy photoelectric effect dominates. It diminishes fast when E_{ν} approaches tens of keV
- At E_{γ} = a few tens of keV, Compton scattering start to take over
- Once E_{γ} exceeds the threshold of $2m_{e}c^{2} = 1.02$ MeV, pair production becomes more likely. Compton scattering diminishes as energy increases from 1 MeV.

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Relative probabilities between Compare with Lead absorber (much

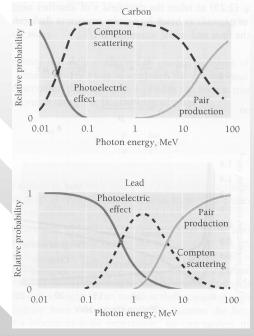
- higher A:):
- Photoelectric effect remains dominant up to a higher energy of a few hundreds of keV (c.f. Carbon of a few tens of keV)
- This is because the heavier the nucleus the better it is in absorbing the momentum transfer that occurs when the energetic photon imparts its momentum to the atom
- Compton scattering starts to appears after a much higher energy of 1 MeV (c.f. a few tens of keV for Carbon).
- This is because a larger atomic number binds an electron stronger, rendering the electron less 'free'> In this case, to Compton scatter off an "free" electron the photon has to be more energetic
- (recall that in Compton scattering, only free electrons are scattered by photon).



Relative probabilities between different absorbers different

lead (a heavy element).

- The energy at which pair production takes over as the principle mechanism of energy loss is called the crossover energy
- The crossover energy is 10 MeV for Carbon, 4 for Lead
- The greater atomic number, the lower the crossover energy
- This is because nuclear with larger atomic number has stronger electric field that is necessary to trigger paircreation

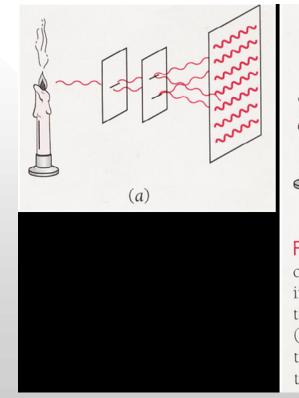


What is a photon?

- Like an EM wave, photons move with speed of light *c*
- They have zero mass and rest energy
- The carry energy and momentum, which are related to the frequency and wavelength of the EM wave by E=hf and $p = h/\lambda$
- They can be created or destroyed when radiation is emitted or absorbed
- They can have particle-like collisions with other particles such as electrons

Contradictory nature of light

- In Photoelectric effect, Compton scatterings, inverse photoelectric effect, pair creation/annihilation, light behaves as particle. The energy of the EM radiation is confined to localised bundles
- In Young's Double slit interference, diffraction, Bragg's diffraction of X-ray, light behave as waves. In the wave picture of EM radiation, the energy of wave is spread smoothly and continuously over the wavefronts.



(b) Figure 2.14 (a) The wave theory

Figure 2.14 (*a*) The wave theory of light explains diffraction and interference, which the quantum theory cannot account for. (*b*) The quantum theory explains the photoelectric effect, which the wave theory cannot account

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Is light particle? Or is it wave?

- Both the wave and particle explanations of EM radiation are obviously mutually exclusive
- So how could we reconcile these seemingly contradictory characteristics of light?
- The way out to the conundrum:
 - WAVE-PARTICLE DUALITY

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Interference pattern observed

So, (asking for the second time) is light wave of particle?

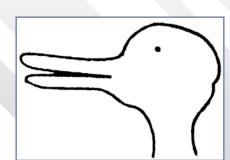
- So, it is not *either* particle or wave but *both* particles and waves
- However, both typed of nature cannot be simultaneously measured in a single experiment
- The light only shows one or the other aspect, depending on the kind of experiment we are doing
- Particle experiments show the particle nature, while a wave-type experiment shows the wave nature

Photoelectron observed

The identity of photon depends on how the experimenter decide to look at it



The face of a young or an old woman?



Is this a rabbit or a duck?

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Coin a simile of wave-particle duality

- It's like a coin with two faces. One can only sees one side of the coin but not the other at any instance
- This is the so-called waveparticle duality
- Neither the wave nor the particle picture is wholly correct all of the time, that both are needed for a complete description pf physical phenomena
- The two are *complementary* to another

photon as particle

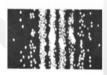
Photon as wave



Interference experiment with a single photon Consider an double slit experiment using an extremely weak

- Consider an double slit experiment using an extremely weak source (say, a black body filament) that emits only one photon a time through the double slit and then detected on a photographic plate by darkening individual grains.
- When one follows the time evolution of the pattern created by these individual photons, interference pattern is observed
- At the source the light is being emitted as photon (radiated from a dark body) and is experimentally detected as a photon which is absorbed by an individual atom on the photographic plate to form a grain
- In between (e.g. between emission and detection), we must interpret the light as electromagnetic energy that propagates smoothly and continuously as a wave
- However, the wave nature between the emission and detection is not directly detected. Only the particle nature are detected in this procedure.
- The correct explanation of the origin and appearance of the interference pattern comes from the wave picture, and the correct interpretation of the evolution of the pattern on the screen comes from the particle picture;
- Hence to completely explain the experiment, the two pictures must somehow be taken together this is an example for which *both pictures are complimentary to each other*

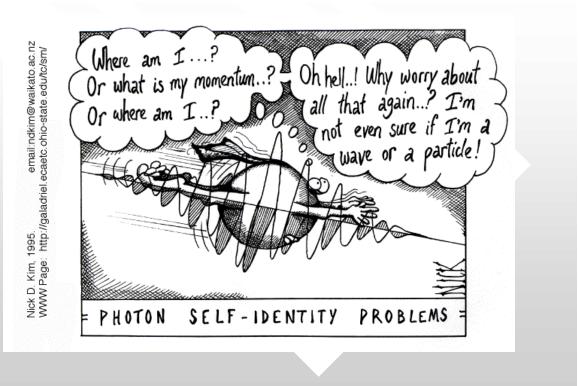






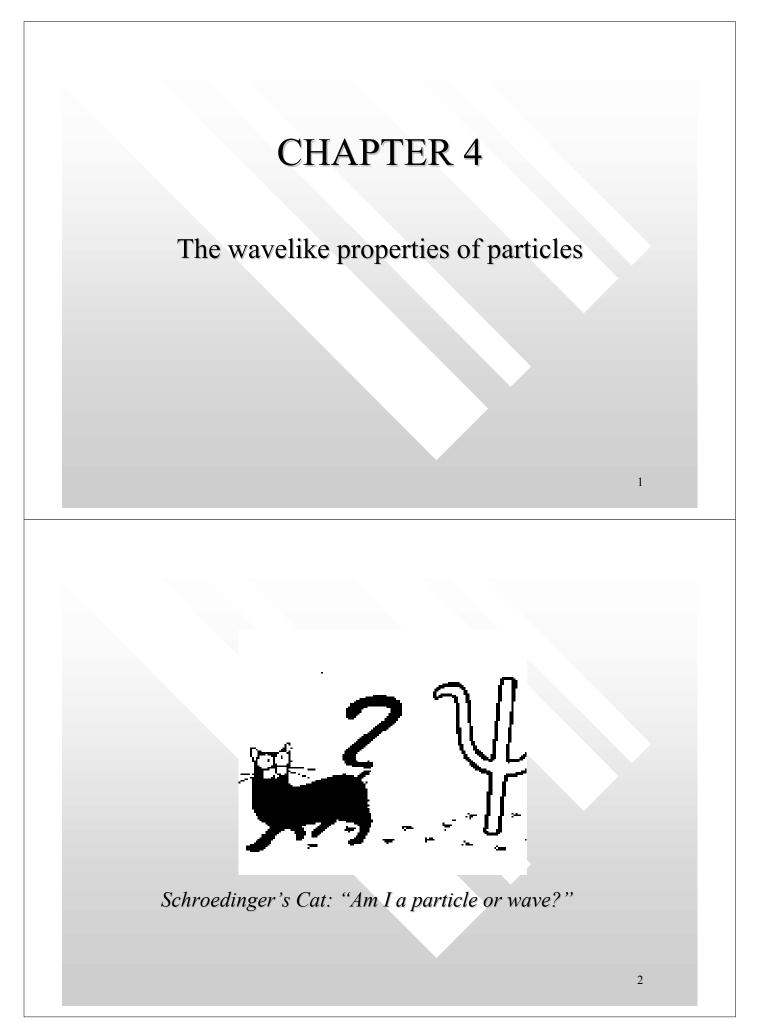


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Both light and material particle display wave-particle duality

- Not only light manifest such wave-particle duality, but other microscopic material particles (e.g. electrons, atoms, muons, pions well).
- In other words:
- Light, as initially thought to be wave, turns out to have particle nature;
- Material particles, which are initially thought to be corpuscular, also turns out to have wave nature (next topic)



Wave particle duality

- "Quantum nature of light" refers to the particle attribute of light
- "Quantum nature of particle" refers to the wave attribute of a particle
- Light (classically EM waves) is said to display "wave-particle duality" – it behave like wave in one experiment but as particle in others (c.f. a person with schizophrenia)

- Not only light does have "schizophrenia", so are other microscopic "particle" such as electron, i.e. particles also manifest wave characteristics in some experiments
- Wave-particle duality is essentially the manifestation of the quantum nature of things
- This is an very weird picture quite contradicts to our conventional assumption with is deeply rooted on classical physics or intuitive notion on things

Planck constant as a measure of quantum effect

- When investigating physical systems involving its quantum nature, the theory usually involves the appearance of the constant h
- e.g. in Compton scattering, the Compton shift is proportional to *h*; So is photoelectricity involves *h* in its formula
- In general, when *h* appears, it means quantum effects arise
- In contrary, in classical mechanics or classical EM theory, *h* never appear as both theories do not take into account of quantum effects
- Roughly quantum effects arise in microscopic system (e.g. on the scale approximately of the order 10⁻¹⁰ m or smaller)

Wavelike properties of particle

- In 1923, while still a graduate student at the University of Paris, Louis de Broglie published a brief note in the journal *Comptes rendus* containing an idea that was to revolutionize our understanding of the physical world at the most fundamental level:
- That particle has intrinsic wave properties
- For more interesting details:
- http://www.davisinc.com/physics/index.shtml



Prince de Broglie, 1892-1987

de Broglie's postulate (1924)

• The postulate: there should be a symmetry between matter and wave. The wave aspect of matter is related to its particle aspect in exactly the same quantitative manner that is in the case for radiation. The total (i.e. relativistic) energy *E* and momentum *p* of an entity, for both matter and wave alike, is related to the frequency *f* of the wave associated with its motion via Planck constant

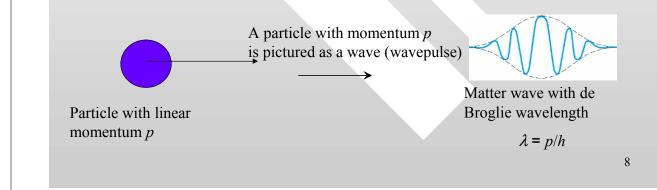
> $p = h/\lambda,$ E = hf

> > 7

A particle has wavelength!!!

$\lambda = h/p$

- is the de Broglie relation predicting the wave length of the matter wave λ associated with the motion of a material particle with momentum *p*
- Note that classically the property of wavelength is only reserved for wave and particle was never associate with any wavelength
- But, following de Broglie's postulate, such distinction is removed



A physical entity possess both aspects of particle and wave in a complimentary manner

BUT why is the wave nature of material particle

not observed?

Because ...

- Because...we are too large and quantum effects are too small
- Consider two extreme cases:
- (i) an electron with kinetic energy K = 54 eV, de Broglie wavelength, $\lambda = h/p = h/(2m_eK)^{1/2} = 1.65$ Angstrom.
- Such a wavelength is comparable to the size of atomic lattice, and is experimentally detectable
- (ii) As a comparison, consider an macroscopic object, a billard ball of mass m = 100 g moving with momentum p
- $p = mv \approx 0.1 \text{ kg} \times 10 \text{ m/s} = 1 \text{ Ns}$ (relativistic correction is negligible)
- It has de Broglie wavelength $\lambda = h/p \approx 10^{-34}$ m, too tiny to be observed in any experiments
- The total energy of the billard ball is
 - $E = K + m_0 c^2 \approx m_0 c^2 = 0.1 \times (3 \times 10^8)^2 \text{ J} = 9 \times 10^{15} \text{ J}$ (K is ignored since $K \ll m_0 c^2$)
- The frequency of the de Broglie wave associated with the billard ball is $f = E/h = m_0 c^2/h = (9 \times 10^{15}/6.63 \times 10^{34}) \text{ Hz} = 10^{78} \text{ Hz}$, impossibly high for any experiment to detect

Matter wave is a quantum phenomena

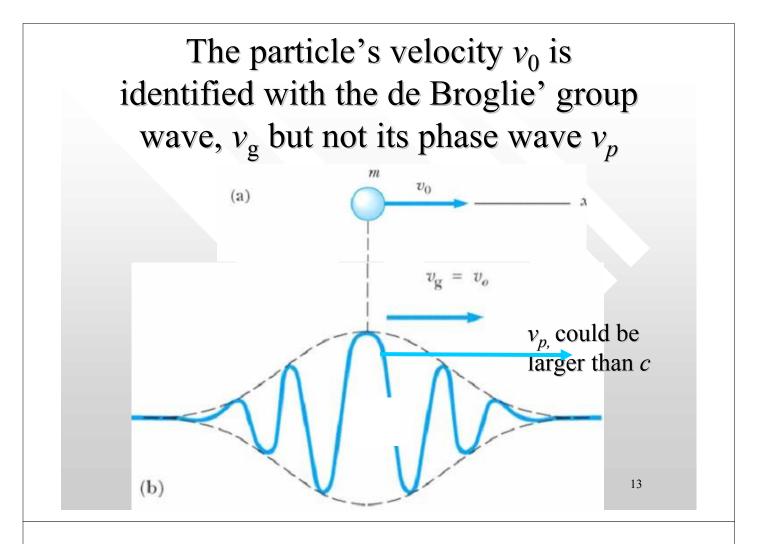
- This also means that the wave properties of matter is difficult to observe for macroscopic system (unless with the aid of some specially designed apparatus)
- The smallness of *h* in the relation $\lambda = h/p$ makes wave characteristic of particles hard to be observed
- The statement that when $h \rightarrow 0$, λ becomes vanishingly small means that:
- the wave nature will become effectively "shut-off" and appear to loss its wave nature whenever the relevant *p* of the particle is too large in comparison with the quantum scale characterised by *h*

How small is small?

- More quantitatively, we could not detect the quantum effect if $h/p \sim 10^{-34}$ Js/p (dimension: length, L) becomes too tiny in comparison to the length scale discernable by an experimental setup (e.g. slit spacing in a diffraction experiment)
- For a numerical example: For a slit spacing of *l*~ nm (interatomic layer in a crystal), and a momentum of *p*=10 Ns (100 g billard ball moving with 10 m/s),

 $h/p = 10^{-34} \text{ Js}/p = 10^{-34} \text{ Js}/10 \text{ Ns} \sim 10^{-35} \text{ m} \ll l \sim \text{nm}$

- LHS, i.e. h/p (~10⁻³⁵ m), is the length scale of the de Broglie (quantum) wavelength;
- RHS, i.e. *l* (~ nm), is the length scale charactering the experiment
- Such an experimental set up could not detect the wave length of the moving billard ball.



Example

- An electron has a de Broglie wavelength of 2.00 pm. Find its kinetic energy and the group velocity of its de Broglie waves.
- Hint:
- The group velocity of the dB wave of electron v_g is equal to the velocity of the electron, v.
- Must treat the problem relativistically.
- If the electron's de Broglie wavelength λ is known, so is the momentum, *p*. Once *p* is known, so is the total energy, *E* and velocity *v*. Once *E* is known, so will the kinetic energy, *K*.

Solution

• Total energy $E^2 = c^2 p^2 + m_0^2$

•
$$K = E - m_0 c^2$$

= $(c^2 p^2 + m_0^2 c^4)^{\frac{1}{2}} - m_0 c^2$
= $((hc/\lambda)^2 + m_0^2 c^4)^{\frac{1}{2}} - m_0 c^2 = 297 \text{ keV}$

•
$$v_g = v; 1/\gamma^2 = 1 - (v/c)^2;$$

•
$$(pc)^2 = (\gamma m_0 vc)^2 = (hc/\lambda)^2$$
 (from Relativity and de Broglie's postulate)

 $\Rightarrow (\gamma v/c)^2 = (hc/\lambda)^2 / (m_0 c^2)^2 = (620 \text{ keV}/510 \text{ keV})^2 = 1.4884;$ $(\gamma v/c)^2 = (v/c)^2 / 1 - (v/c)^2$ $\Rightarrow v_g/c = \sqrt{(1.4884/(1+1.4884))} = 0.77$

Alternatively

• The previous calculation can also proceed via:

•
$$K=(\gamma-1)m_{\rm e}c^2$$

• $\Rightarrow \gamma = K/(m_e c^2) + 1 = 297 \text{ keV}/(510 \text{ keV}) + 1$ =1.582;

•
$$p = h/\lambda = \gamma m_e v \Longrightarrow v = hc/(\lambda \gamma m_e c)$$

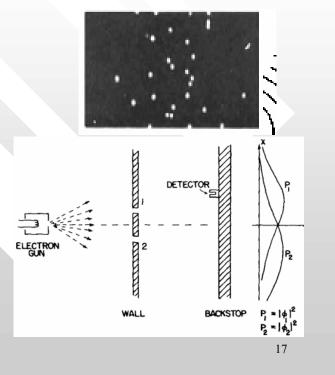
•
$$\Rightarrow v/c = hc/(\lambda \gamma m_{\rm e}c^2)$$

 $= (1240 \text{ nm} \cdot \text{eV}) / (2\text{pm} \cdot 1.582 \cdot 0.51 \text{MeV})$

$$= 0.77$$

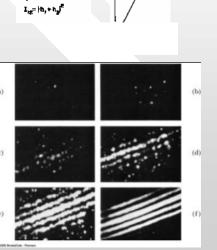
Interference experiment with a single electron, firing one in a time

- Consider an double slit experiment using an extremely small electron source that emits only one electron a time through the double slit and then detected on a fluorescent plate
- When hole 1 (hole 2) is blocked, distribution P1 (P2) is observed.
- P1 are P2 are the distribution pattern as expected from the behaviour of particles.
- Hence, electron behaves like particle when one of the holes is blocked
- What about if both holes are not blocked? Shall we see the distribution simply be P1 + P2? (This would be our expectation for particle: Their distribution simply adds)



Electrons display interference pattern

- When one follows the time evolution of the pattern created by these individual electron with both hole opened, what sort of pattern do you think you will observed?
- It's the interference pattern that are in fact observed in experiments
- At the source the electron is being emitted as particle and is experimentally detected as a electron which is absorbed by an individual atom in the fluorescent plate
- In between, we must interpret the electron in the form of a wave. The double slits change the propagation of the electron wave so that it is 'processed' to forms diffraction pattern on the screen.
- Such process would be impossible if electrons are particle (because no one particle can go through both slits at the same time. Such a simultaneous penetration is only possible for wave.)
- Be reminded that the wave nature in the intermediate states is not measured. Only the particle nature are detected in this procedure.



- The correct explanation of the origin and appearance of the interference pattern comes from the wave picture
- Hence to completely explain the experiment, the two pictures must somehow be taken together – this is an example for which *both pictures are complimentary to each other*
- Try to compare the last few slides with the slides from previous chapter for photon, which also displays wave-particle duality

So, is electron wave or particle?

- They are both...but not simultaneously
- In any experiment (or empirical observation) only one aspect of either wave or particle, but not both can be observed simultaneously.
- It's like a coin with two faces. But one can only see one side of the coin but not the other at any instance
- This is the so-called waveparticle duality

ConstructionElectron as
waveElectron as
wave

Detection of electron as particle destroy the interference pattern

- If in the electron interference experiment one tries to place a detector on each hole to determine through which an electron passes, the wave nature of electron in the intermediate states are destroyed
- i.e. the interference pattern on the screen shall be destroyed
- Why? It is the consistency of the wave-particle duality that demands such destruction must happen (think of the logics yourself or read up from the text)

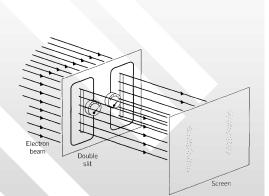
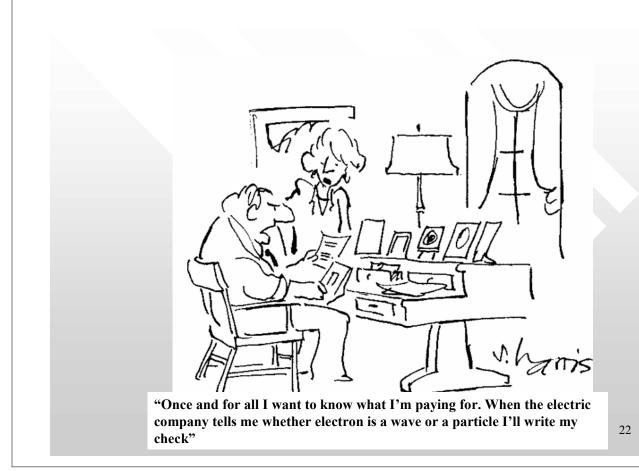


FIGURE 4.15 Apparatus to record passage of electrons through slits. Each slit is surrounded by a loop with a meter that signals the passage of an electron through the slit. No interference finges are seen on the screen.

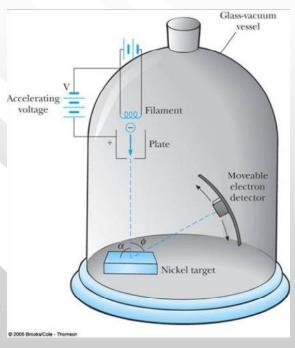


Extra readings

- Those quantum enthusiasts may like to read more about wave-particle duality in Section 5.7, page 179-185, Serway, Moses and Mayer.
- An even more recommended reading on waveparticle duality: the Feynman lectures on physics, vol. III, chapter 1 (Addison-Wesley Publishing)
- It's a very interesting and highly intellectual topic to investigate

Davisson and Gremer experiment

- DG confirms the wave nature of electron in which it undergoes Bragg's diffraction
- Thermionic electrons are produced by hot filament, accelerated and focused onto the target (all apparatus is in vacuum condition)
- Electrons are scattered at an angle φ into a movable detector



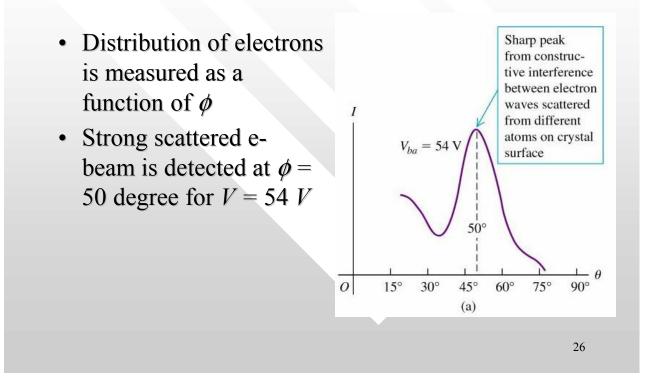
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Pix of Davisson and Gremer



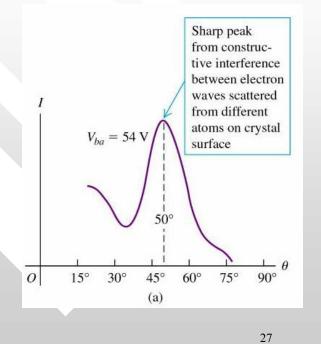
Result of the DG experiment

25



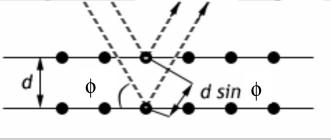
How to interpret the result of DG?

- Electrons get diffracted by the atoms on the surface (which acted as diffraction grating) of the metal as though the electron acting like they are WAVES
- Electrons do behave like waves as postulated by de Broglie



Bragg diffraction of electron by parallel lattice planes in the crystal

- Bragg law: $d \sin \phi = n\lambda$
- The peak of the diffraction pattern is the m=1st order constructive interference: $d \sin \phi = 1\lambda$
- where $\phi = 50$ degree for V = 54 V
- From x-ray Bragg's diffraction experiment done independently we know d = 2.15 Amstrong
- Hence the wavelength of the electron is $\lambda = d\sin \phi = 1.65$ Angstrom
- Here, 1.65 Angstrom is the experimentally inferred value, which is to be checked against the theoretical value predicted by de Broglie



Theoretical value of λ of the electron

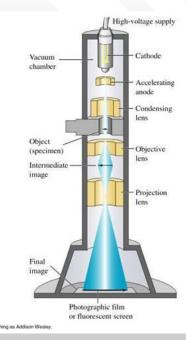
- An external potential *V* accelerates the electron via *eV=K*
- In the DG experiment the kinetic energy of the electron is accelerated to K = 54 eV (non-relativistic treatment is suffice because $K \ll m_e c^2 = 0.51 \text{ MeV}$)
- According to de Broglie, the wavelength of an electron accelerated to kinetic energy of $K = p^2/2m_e = 54 \text{ eV}$ has a equivalent matter wave wavelength $\lambda = h/p = h/(2Km_e)^{1/2} = 1.67 \text{ Amstrong}$
- In terms of the external potential, $\lambda = h/(2eVm_e)^{1/2}$

Theory's prediction matches measured value

- The result of DG measurement agrees almost perfectly with the de Broglie's prediction: 1.65 Angstrom measured by DG experiment against 1.67 Angstrom according to theoretical prediction
- Wave nature of electron is hence experimentally confirmed
- In fact, wave nature of microscopic particles are observed not only in e- but also in other particles (e.g. neutron, proton, molecules etc. – most strikingly Bose-Einstein condensate)

Application of electrons wave: electron microscope, Nobel Prize 1986 (Ernst Ruska)

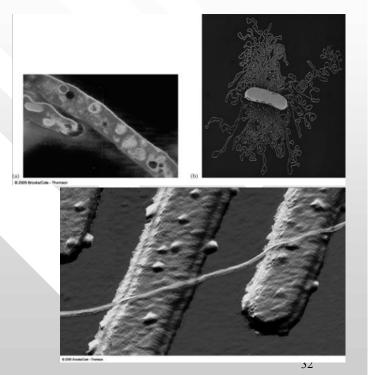




• Electron's de Broglie wavelength can be tuned via $\lambda = h/(2eVm_e)^{1/2}$

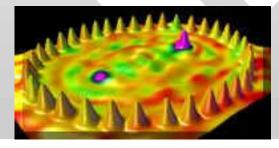
s/Cole - Tho

 Hence electron microscope can magnify specimen (x4000 times) for biological specimen or 120,000 times of wire of about 10 atoms in width



Not only electron, other microscopic particles also behave like wave at the quantum scale

- The following atomic structural images provide insight into the threshold between prime radiant flow and the interference structures called matter.
- In the right foci of the ellipse a real cobalt atom has been inserted. In the left foci of the ellipse a phantom of the real atom has appeared. The appearance of the phantom atom was not expected.
- The ellipsoid coral was constructed by placing 36 cobalt atom on a copper surface. This image is provided here to provide a visual demonstration of the attributes of material matter arising from the harmonious interference of background radiation.



http://home.netcom.co m/~sbyers11/g_fav11E .htm

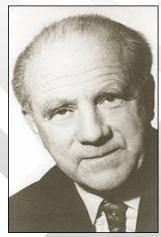
Heisenberg's uncertainty principle (Nobel Prize,1932)

• WERNER HEISENBERG (1901 - 1976)

QUANTUM

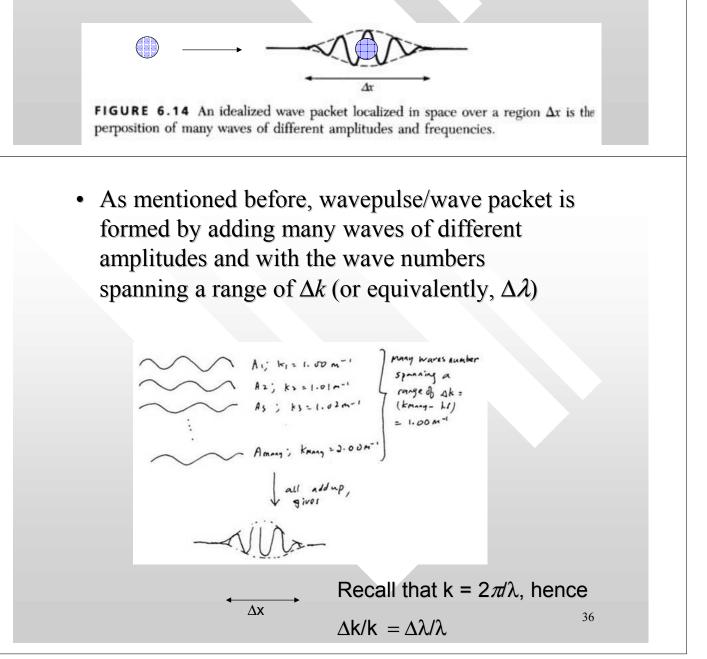
CORAL

- was one of the greatest physicists of the twentieth century. He is best known as a founder of <u>quantum mechanics</u>, the new physics of the atomic world, and especially for the <u>uncertainty principle</u> in quantum theory. He is also known for his controversial role as a leader of Germany's <u>nuclear fission</u> research during World War II. After the war he was active in elementary particle physics and West German <u>science policy</u>.
- <u>http://www.aip.org/history/heisenberg/p01.</u>
 <u>htm</u>



A particle is represented by a wave packet/pulse

- Since we experimentally confirmed that particles are wave in nature at the quantum scale *h* (matter wave) we now have to describe particles in term of waves (relevant only at the quantum scale)
- Since a real particle is localised in space (not extending over an infinite extent in space), the wave representation of a particle has to be in the form of wave packet/wave pulse



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Still remember the uncertainty relationships for classical waves?

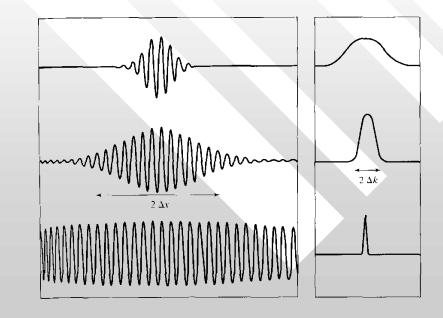
• As discussed earlier, due to its nature, a wave packet must obey the uncertainty relationships for classical waves (which are derived mathematically with some approximations)

$$\Delta \lambda \Delta x > \lambda^2 \equiv \Delta k \Delta x > 2\pi \qquad \Delta t \Delta v \ge 1$$

• However a more rigorous mathematical treatment (without the approximation) gives the exact relations

$$\Delta \lambda \Delta x \ge \frac{\lambda^2}{4\pi} \equiv \Delta k \Delta x \ge 1/2 \qquad \Delta v \Delta t \ge \frac{1}{4\pi}$$

- To describe a particle with wave packet that is localised over a small region Δx requires a large range of wave number; that is, Δk is large. Conversely, a small range of wave number cannot produce a wave packet localised within a small distance.
 - A narrow wave packet (small Δx) corresponds to a large spread of wavelengths (large Δk).
 - A wide wave packet (large Δx) corresponds to a small spread of wavelengths (small Δk).



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Matter wave representing a particle must also obey similar wave uncertainty relation

• For matter waves, for which their momentum and wavelength are related by $p = h/\lambda$, the uncertainty relationship of the classical wave

•
$$\Delta \lambda \Delta x \ge \frac{\lambda^2}{4\pi} \equiv \Delta k \Delta x \ge 1/2$$
 is translated into

$$\Delta p_x \Delta x \ge \frac{\hbar}{2}$$

- where $\hbar = h / 2\pi$
- Prove this relation yourselves (hint: from $p = h/\lambda$, $\Delta p/p = \Delta \lambda/\lambda$)

Time-energy uncertainty

• Just as $\Delta p_x \Delta x \ge \frac{\hbar}{2}$ implies position-momentum uncertainty relation, the classical wave uncertainty relation $\Delta v \Delta t \ge \frac{1}{2}$ also implies a corresponding relation bet Ween time and energy \hbar

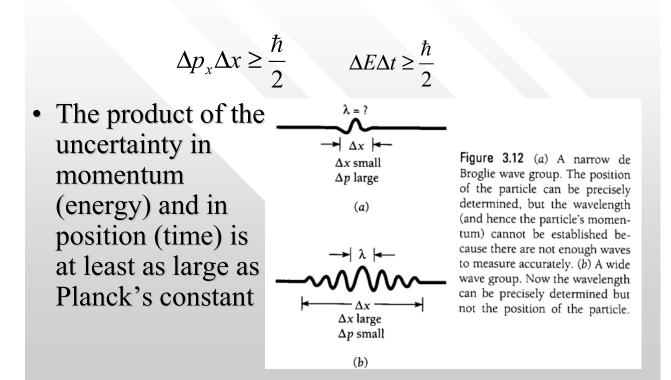
$$\Delta E \Delta t \ge \frac{\hbar}{2}$$

• This uncertainty relation can be easily obtained:

$$h\Delta v\Delta t \ge \frac{h}{4\pi} = \frac{\hbar}{2};$$

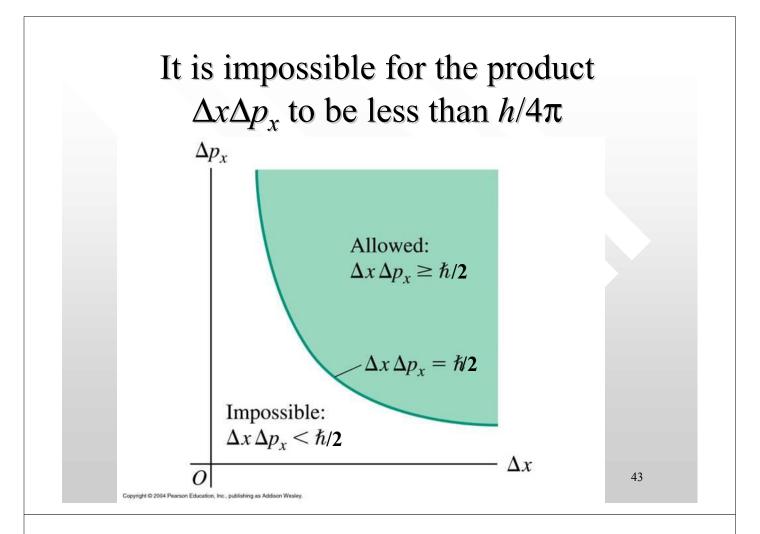
 $\therefore E = hV, \Delta E = h\Delta v \Longrightarrow \Delta E\Delta t = h\Delta v\Delta t = \frac{\hbar}{2}$

Heisenberg uncertainty relations



What
$$\Delta p_x \Delta x \ge \frac{\hbar}{2}$$
 means

- It sets the intrinsic lowest possible limits on the uncertainties in knowing the values of p_x and x, no matter how good an experiments is made
- It is impossible to specify simultaneously and with infinite precision the linear momentum and the corresponding position of a particle



What
$$\Delta E \Delta t \ge \frac{\hbar}{2}$$
 means

- Uncertainty principle for energy.
- The energy of a system also has inherent uncertainty, ΔE
- ΔE is dependent on the *time interval* Δt during which the system remains in the given states.
- If a system is known to exist in a state of energy *E* over a limited period Δt, then this energy is uncertain by at least an amount h/(4πΔt). This corresponds to the 'spread' in energy of that state (see next page)
- Therefore, the energy of an object or system can be measured with infinite precision ($\Delta E=0$) only if the object of system exists for an infinite time ($\Delta t \rightarrow \infty$)₄₄

What $\Delta E \Delta t \ge \frac{\hbar}{2}$ means

A system that remains in a metastable state for a very long time (large Δt) can have a very well-defined energy (small ΔE), but if remain in a state for only a short time (small Δt), the uncertainty in energy must be correspondingly greater (large ΔE).

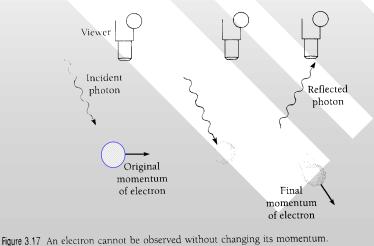


Conjugate variables (Conjugate observables)

- {*p_x*,*x*}, {*E*,*t*} are called *conjugate variables*
- The conjugate variables cannot in principle be measured (or known) to infinite precision simultaneously

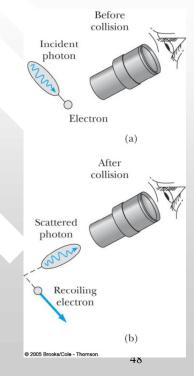
Heisenberg's Gedanken experiment

- The U.P. can also be understood from the following gedanken experiment that tries to measure the position and momentum of an object, say, an electron at a certain moment
- In order to measure the momentum and position of an electron it is necessary to "interfere" it with some "probe" that will then carries the required information back to us such as shining it with a photon of say a wavelength of λ



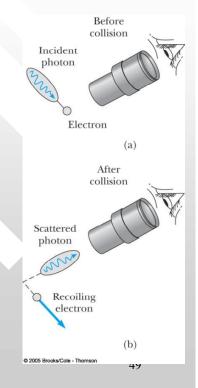
Heisenberg's Gedanken experiment

- Let's say the "unperturbed" electron was initially located at a "definite" location *x* and with a "definite" momentum *p*
- When the photon 'probes' the electron it will be bounced off, associated with a changed in its momentum by some uncertain amount, Δp .
- Δp cannot be predicted but must be of the similar order of magnitude as the photon's momentum h/λ
- Hence $\Delta p \approx h/\lambda$
- The longer λ (i.e. less energetic) the smaller the uncertainty in the measurement of the electron's momentum
- In other words, electron cannot be observed without changing its momentum



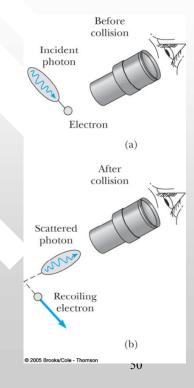
Heisenberg's Gedanken experiment

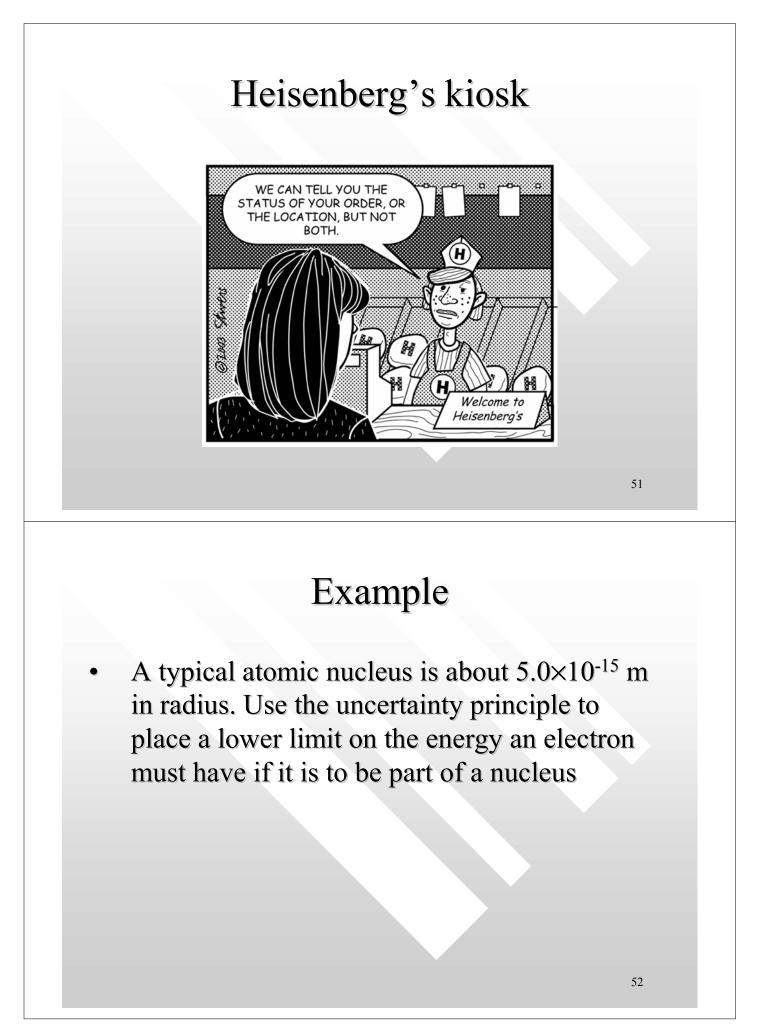
- How much is the uncertainty in the position of the electron?
- By using a photon of wavelength λ we cannot determine the location of the electron better than an accuracy of $\Delta x = \lambda$
- Hence $\Delta x \ge \lambda$
- Such is a fundamental constraint coming from optics (Rayleigh's criteria).
- The shorter the wavelength λ (i.e. more energetic) the smaller the uncertainty in the electron's position



Heisenberg's Gedanken experiment

- However, if shorter wavelength is employed (so that the accuracy in position is increased), there will be a corresponding decrease in the accuracy of the momentum, measurement (recall $\Delta p \approx h/\lambda$)
- A higher photon momentum will disturb the electron's motion to a greater extent
- Hence there is a 'zero sum game' here
- Combining the expression for Δx and Δp , we then have $\Delta p \ \Delta \lambda \ge h$, a result consistent with $\Delta p \ \Delta \lambda \ge h/2$

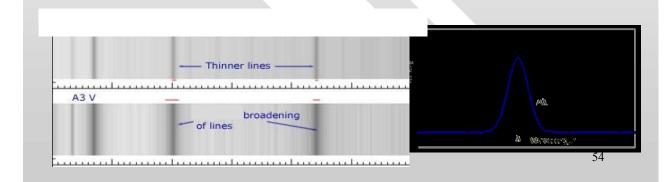




- Letting $\Delta x = 5.0 \times 10^{-15}$ m, we have
- $\Delta p \ge h/(4\pi\Delta x) = ... = 1.1 \times 10^{-20} \text{ kg·m/s}$ If this is the uncertainty in a nuclear electron's momentum, the momentum *p* must be at lest comparable in magnitude. An electron of such a momentum has a
- KE = $pc \ge 3.3 \times 10^{-12} \text{ J}$ = 20.6 MeV >> $m_e c^2 = 0.5 \text{ MeV}$
- i.e., if electrons were contained within the nucleus, they must have an energy of at least 20.6 MeV
- However such an high energy electron from radioactive nuclei never observed
- Hence, by virtue of the uncertainty principle, we conclude that electrons emitted from an unstable nucleus cannot comes from within the nucleus

Broadening of spectral lines due to uncertainty principle

• An excited atom gives up it excess energy by emitting a photon of characteristic frequency. The average period that elapses between the excitation of an atom and the time is radiates is 1.0×10^{-8} s. Find the inherent uncertainty in the frequency of the photon.



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- The photon energy is uncertain by the amount
- $\Delta E \ge hc/(4c\pi\Delta t) = 5.3 \times 10^{-27} \text{ J} = 3.3 \times 10^{-8} \text{ eV}$
- The corresponding uncertainty in the frequency of light is $\Delta v = \Delta E/h \ge 8 \times 10^6 \text{ Hz}$
- This is the irreducible limit to the accuracy with which we can determine the frequency of the radiation emitted by an atom.
- As a result, the radiation from a group of excited atoms does not appear with the precise frequency v.
- For a photon whose frequency is, say, 5.0×10^{14} Hz,
- $\Delta v/v = 1.6 \times 10^{-8}$

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- Assume that the uncertainty in the position of a particle is equal to its de Broglie wavelength. What is the minimal uncertainty in its velocity, v_x?
- A. $v_x/4\pi$ B. $v_x/2\pi$
- D. v_x E. v_x/π
- ANS: A, Schaum's 3000 solved problems, Q38.66, pg. 718

C. $v_{r}/8\pi$

 $\Delta x \Delta p_x \ge \hbar/2; \Delta p_x = m \Delta v_x.$ Given $\Delta x = \lambda$, $\Rightarrow m \Delta x \Delta v_x = m \lambda \Delta v_x \ge \hbar/2;$ $\Rightarrow \Delta v_x \ge \hbar/2m\lambda = h/4\pi m\lambda$ But $p_x = h/\lambda$ $\Rightarrow \Delta v_x \ge h/4\pi m\lambda = p_x/4\pi m$ $= m v_x/4\pi m = v_x/4\pi$

Example

A measurement established the position of a proton with an accuracy of ±1.00×10⁻¹¹ m. Find the uncertainty in the proton's position 1.00 s later. Assume v << c.

- Let us call the uncertainty in the proton's position Δx_0 at the time t = 0.
- The uncertainty in its momentum at t = 0is

$\Delta p \geq h/(4\pi \Delta x_0)$

• Since v << c, the momentum uncertainty is

$\Delta p = m \Delta v$

• The uncertainty in the proton's velocity is

$\Delta v = \Delta p / m \ge h / (4\pi m \Delta x_0)$

• The distance x of the proton covers in the time t cannot be known more accurately than

 $\Delta x = t \Delta v \ge ht/(4\pi m \Delta x_0)$

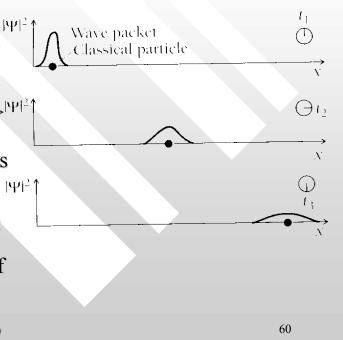
•
$$m=970 \text{ MeV}/c^2$$

The value of Δx at t = 1.00 s is 3.15 km.

A moving wave packet spreads out

 $\Delta x = t \Delta v \ge ht/(4\pi \Delta x_0)$ in space

- Note that Δx is inversely proportional to Δx_0
- It means the more we know about the proton's position at t = 0 the less we know about its later position at $t > |\Psi|^2$ 0.
- The original wave group has spread out to a much wider $|\Psi|^{2}$ one because the phase velocities of the component wave vary with wave number and a large range of wave numbers must have been present to produce the narrow original wave group



Example

Estimating quantum effect of a macroscopic particle

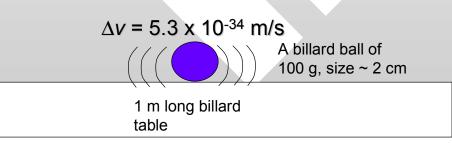
• Estimate the minimum uncertainty velocity of a billard ball ($m \sim 100$ g) confined to a billard table of dimension 1 m

Solution

For $\Delta x \sim 1$ m, we have

$$\Delta p \geq h/4\pi\Delta x = 5.3 \times 10^{-35} \text{ Ns},$$

- So $\Delta v = (\Delta p) / m \ge 5.3 \times 10^{-34} \text{ m/s}$
- One can consider $\Delta v = 5.3 \times 10^{-34}$ m/s (extremely tiny) is the speed of the billard ball at anytime caused by quantum effects
- In quantum theory, no particle is absolutely at rest due to the Uncertainty Principle

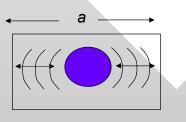


A particle contained within a finite region must has some minimal KE

- One of the most dramatic consequence of the uncertainty principle is that a particle confined in a small region of finite width cannot be exactly at rest (as already seen in the previous example)
- Why? Because...
- ...if it were, its momentum would be precisely zero, (meaning $\Delta p = 0$) which would in turn violate the uncertainty principle

What is the K_{ave} of a particle in a box due to Uncertainty Principle?

- We can estimate the minimal KE of a particle confined in a box of size *a* by making use of the U.P.
- If a particle is confined to a box, its location is uncertain by $\Delta x = a$
- Uncertainty principle requires that $\Delta p \ge (h/2\pi)a$
- (don't worry about the factor 2 in the uncertainty relation since we only perform an estimation)



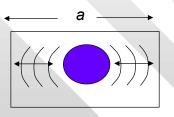
Zero-point energy

63

64

$$K_{\text{ave}} = \left(\frac{p^2}{2m}\right)_{av} > \frac{(\Delta p)^2}{2m} > \frac{\hbar^2}{2ma^2}$$

This is the zero-point energy, the minimal possible kinetic energy for a quantum particle confined in a region of width a



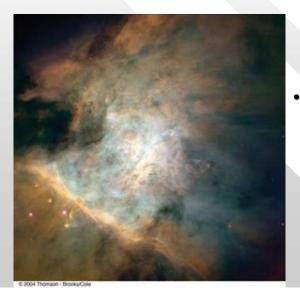
Particle in a box of size a can never be at rest (e.g. has zero K.E) but has a minimal KE K_{ave} (its zero-point energy)

We will formally re-derived this result again when solving for the Schrodinger equation of this system (see later).

Recap Measurement necessarily involves interactions between observer and the observed system Matter and radiation are the entities available to us for such measurements The relations $p = h/\lambda$ and E = hv are applicable to both • matter and to radiation because of the intrinsic nature of wave-particle duality When combining these relations with the universal waves • properties, we obtain the Heisenberg uncertainty relations In other words, the uncertainty principle is a necessary consequence of particle-wave duality 65 OH ALICE YOURE GUANTUM WORLD THE ONE FOR ME HOW CAN WE BE SU

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CHAPTER 5 Atomic Models



Much of the luminous matter in the Universe is hydrogen. In fact hydrogen is the most abundance atom in the Universe. The colours of this Orion Nebula
come from the transition between the quantized states in hydrogen atoms.

INTRODUCTION

- The purpose of this chapter is to build a simplest atomic model that will help us to understand the structure of atoms
- This is attained by referring to some basic experimental facts that have been gathered since 1900's (e.g. Rutherford scattering experiment, atomic spectral lines etc.)
- In order to build a model that well describes the atoms which are consistent with the experimental facts, we need to take into account the wave nature of electron
- This is one of the purpose we explore the wave nature of particles in previous chapters

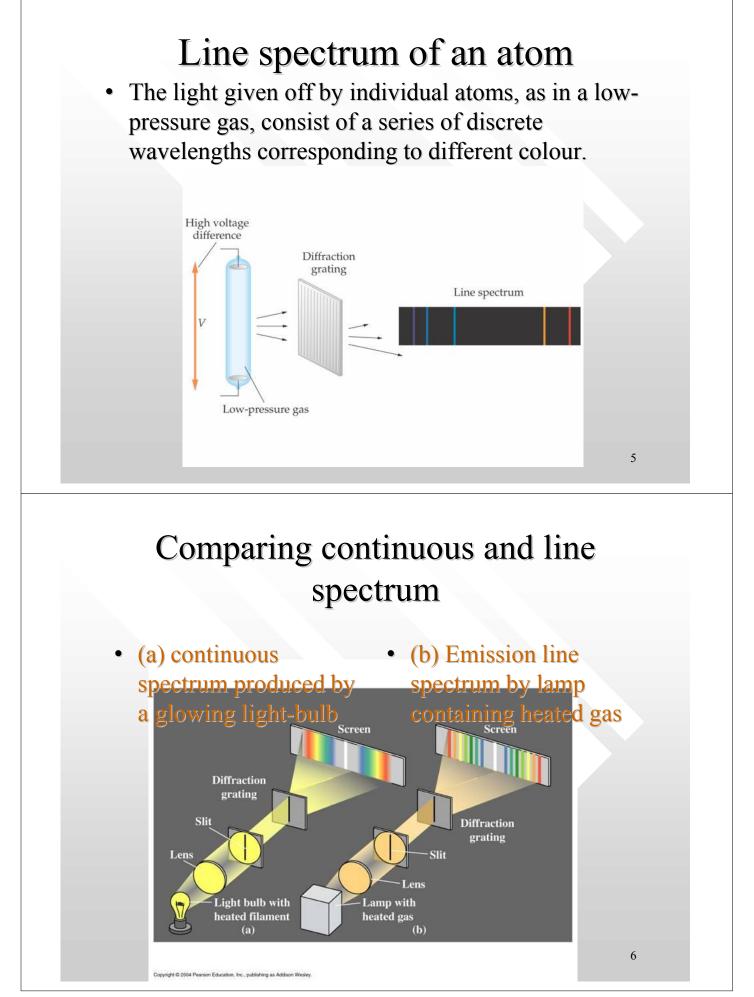
Basic properties of atoms

- 1) Atoms are of microscopic size, $\sim 10^{-10}$ m. Visible light is not enough to resolve (see) the detail structure of an atom as its size is only of the order of 100 nm.
- 2) Most atoms are stable (i.e. atoms that are non radioactive)
- 3) Atoms contain negatively charges, electrons, but are electrically neutral. An atom with Z electrons must also contain a net positive charge of +Ze.
- 4) Atoms emit and absorb EM radiation (in other words, atoms interact with light quite readily)

Because atoms interacts with EM radiation quite strongly, it is usually used to probe the structure of an atom. The typical of such EM probe can be found in the₃ atomic spectrum as we will see now

Emission spectral lines

- Experimental fact: A single atom or molecule in a very diluted sample of gas emits radiation characteristic of the particular atom/molecule species
- The emission is due to the de-excitation of the atoms from their excited states
- e.g. if heating or passing electric current through the gas sample, the atoms get excited into higher energy states
- When a excited electron in the atom falls back to the lower energy states (de-excites), EM wave is emitted
- The spectral lines are analysed with *spectrometer*, which give important physical information of the atom/molecules by analysing the wavelengths composition and pattern of these lines.

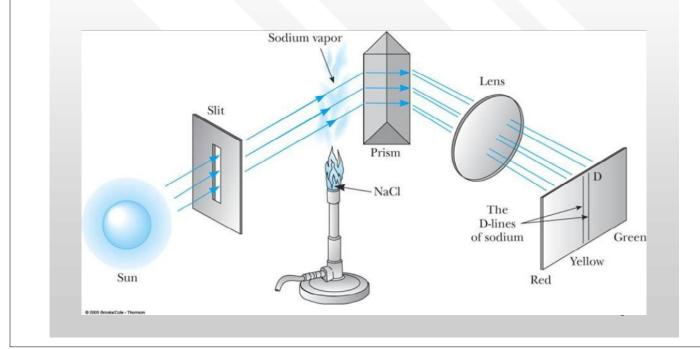


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Absorption line spectrum

• We also have absorption spectral line, in which white light is passed through a gas. The absorption line spectrum consists of a bright background crossed by dark lines that correspond to the absorbed wavelengths by the gas atom/molecules.

Experimental arrangement for the observation of the absorptions lines of a sodium vapour

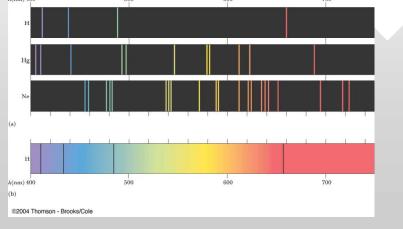


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Comparing emission and absorption spectrum

The emitted and absorption radiation displays characteristic discrete sets of spectrum which contains certain discrete wavelengths only

(a) shows 'finger print' emission spectral lines of H, Hg and Ne. (b) shows absorption lines for H

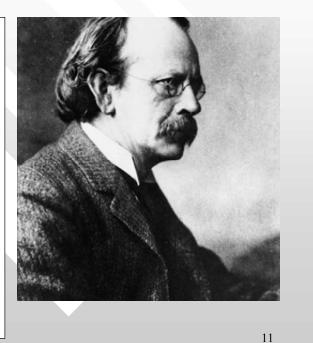


A successful atomic model must be able to explain the observed discrete atomic spectrum

We are going to study two attempts to built model that describes the atoms: the Thompson Plum-pudding model (which fails) and the Rutherford-Bohr model (which succeeds)

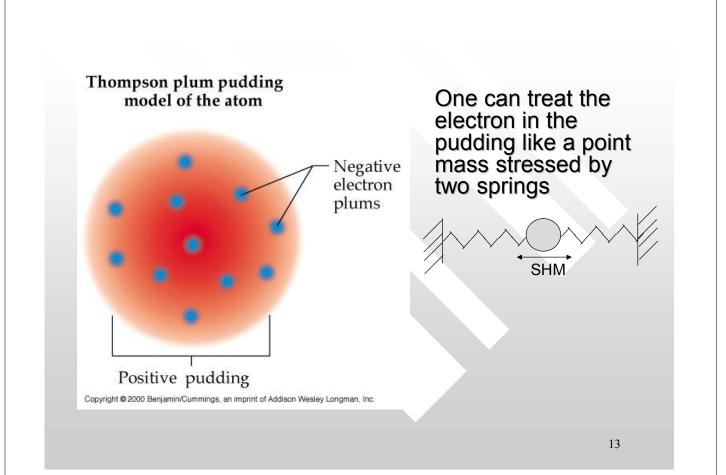
The Thompson model – Plumpudding model

Sir J. J. Thompson (1856-1940) is the Cavandish professor in Cambridge who discovered electron in cathode rays. He was awarded Nobel prize in 1906 for his research on the conduction of electricity by bases at low pressure. He is the first person to establish the particle nature of electron. Ironically his son, another renown physicist proves experimentally electron behaves like wave...



Plum-pudding model

- An atom consists of Z electrons is embedded in a cloud of positive charges that exactly neutralise that of the electrons'
- The positive cloud is heavy and comprising most of the atom's mass
- Inside a stable atom, the electrons sit at their respective equilibrium position where the attraction of the positive cloud on the electrons balances the electron's mutual repulsion



The "electron plum" stuck on the pudding vibrates and executes SHM

• The electron at the EQ position shall vibrate like a simple harmonic oscillator with a frequency

$$\nu = \left(\frac{1}{2\pi}\right)\sqrt{\frac{k}{m}}$$

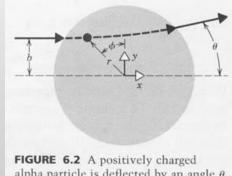
- Where $k = \frac{Ze^2}{4\pi\varepsilon_o R^3}$, *R* radius of the atom, *m* mass of the electron
- From classical EM theory, we know that an oscillating charge will emit radiation with frequency identical to the oscillation frequency v as given above

The plum-pudding model predicts unique oscillation frequency

- Radiation with frequency identical to the oscillation frequency.
- Hence light emitted from the atom in the plumpudding model is predicted to have exactly one unique frequency as given in the previous slide.
- This prediction has been falsified because observationally, light spectra from all atoms (such as the simplest atom, hydrogen,) have sets of discrete spectral lines correspond to many different frequencies (already discussed earlier).

Experimental verdict on the plum pudding model

- Theoretically one expect the deviation angle of a scattered particle by the plum-pudding atom to be small: $\Theta = \sqrt{N}\theta_{ave} \sim 1^{\circ}$
- This is a prediction of the model that can be checked experimentally
- Rutherford was the first one to carry out such experiment



alpha particle is deflected by an angle θ as it passes through a Thomson-model atom. The coordinates *r* and ϕ locate the alpha particle while it is inside the atom.

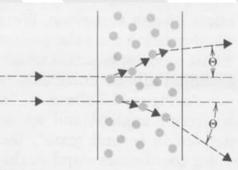


FIGURE 6.6 A microscopic representation of the scattering. Some individual scatterings tend to increase Θ , while others tend to decrease Θ .

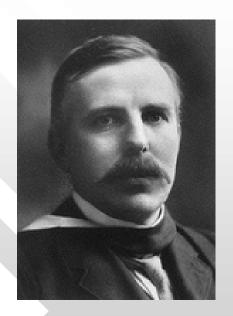
Ernest Rutherford

British physicist Ernest Rutherford, winner of the 1908 Nobel Prize in chemistry, pioneered the field of nuclear physics with his research and development of the nuclear theory of atomic structure

Born in New Zealand, teachers to many physicists who later become Nobel prize laureates

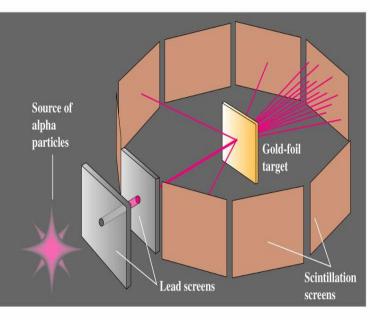
Rutherford stated that an atom consists largely of empty space, with an electrically positive nucleus in the center and electrically negative electrons orbiting the nucleus. By bombarding nitrogen gas with *alpha particles* (nuclear particles emitted through radioactivity), Rutherford engineered the transformation of an atom of nitrogen into both an atom of oxygen and an atom of hydrogen.

This experiment was an early stimulus to the development of nuclear energy, a form of energy in which nuclear transformation and disintegration release extraordinary power.



Rutherford's experimental setup

- Alpha particles from source is used to be scattered by atoms from the thin foil made of gold
- The scattered alpha particles are detected by the background screen



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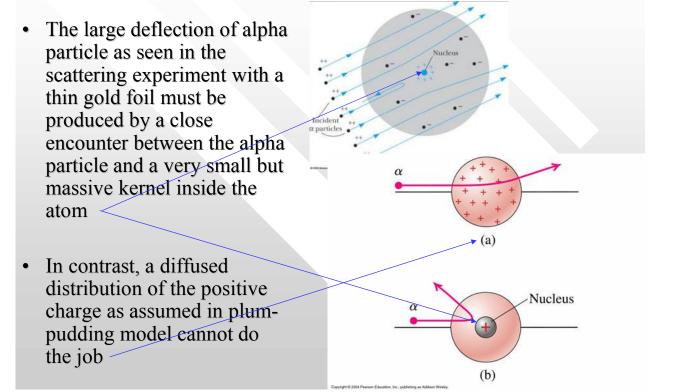
"...fire a 15 inch artillery shell at a tissue paper and it came back and hit you"

- In the scattering experiment Rutherford saw some electrons being bounced back at 180 degree.
- He said this is like firing "a 15-inch shell at a piece of a tissue paper and it came back and hit you"
- Hence Thompson plum-pudding model fails in the light of these experimental result

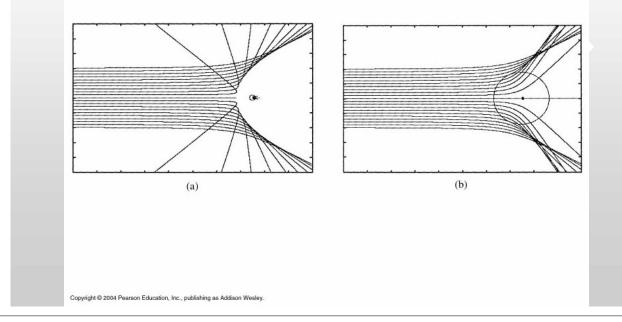
So, is the plum pudding model utterly useless?

- So the plum pudding model does not work as its predictions fail to fit the experimental data as well as other observations
- Nevertheless it's a perfectly sensible scientific theory because:
- It is a mathematical model built on sound and rigorous physical arguments
- It predicts some physical phenomenon with definiteness
- It can be verified or falsified with experiments
- It also serves as a prototype to the next model which is built on the experience gained from the failure of this model

How to interpret the Rutherford scattering experiment?



Comparing model with nucleus concentrated at a point-like nucleus and model with nucleus that has large size



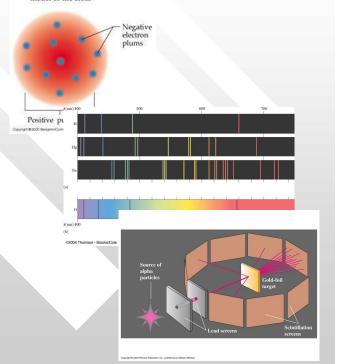
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Recap the atomic model building story Thompson plum pudding model of the atom

- Plum-pudding model by Thompson
- It fails to explain the emission and absorption line spectrum from atoms because it predicts only a single emission frequency

$$v = \left(\frac{1}{2\pi}\right)\sqrt{\frac{k}{m}}$$

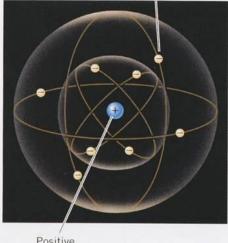
Most importantly it fails to explain the back-scattering of alpha particle seen in Rutherford's scattering experiment because the model predicts only $\Theta = \sqrt{N}\theta_{ave} \sim 1^{\circ}$



The Rutherford model

- (planetary model) Rutherford put forward an
- model to explain the result of the scattering experiment: the Rutherford model
- An atom consists of a very small nucleus of charge +Zecontaining almost all of the mass of the atom; this nucleus is surrounded by a swarm of Zelectrons
- The atom is largely comprised of empty space
- $R_{atom} \sim 10^{-10} \text{m}$ $R_{nucleus} \sim 10^{-13} 10^{-15} \text{m}$

Negative electron



Positive nucleus

Figure 30.1 In the nuclear atom a small positively charged nucleus is surrounded at relatively large distances by a number of electrons.

Infrared catastrophe: insufficiency of the Rutherford model

- According to classical EM, the Rutherford model for atom (a classical model) has a fatal flaw: it predicts the collapse of the atom within 10⁻¹⁰ s
- A accelerated electron will radiate EM radiation, hence causing the orbiting electron to loss energy and consequently spiral inward and impact on the nucleus

Rutherford model also can't explain the discrete spectrum

• The Rutherford model also cannot explain the pattern of discrete spectral lines as the radiation predicted by Rutherford model is a continuous burst.

Radiated light of

/ cycles/s

So how to fix up the problem? NEILS BOHR COMES TO THE RESCUE

- Niels Bohr (1885 to 1962) is best known for the investigations of atomic structure and also for work on radiation, which won him the 1922 Nobel Prize for physics
- He was sometimes dubbed "the God Father" in the physicist community
- http://www-gap.dcs.stand.ac.uk/~history/Mathematicians/ Bohr_Niels.html

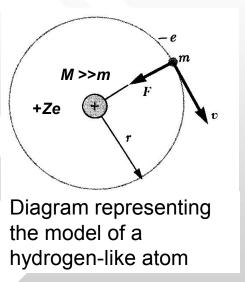


To fix up the infrared catastrophe ...

Neils Bohr put forward a model which is a hybrid of the Rutherford model with the wave nature of electron taken into account

Bohr's model of hydrogen-like atom

- We shall consider a simple atom consists of a nucleus with charge Ze and mass of $M_{nucleus} >> m_e$, such that
- $(m_e/M_{nucleus})$ can be ignored.
- The nucleus is surrounded by only a single electron
- We will assume the centre of the circular motion of the electron coincides with the centre of the nucleus
- We term such type of simple system: hydrogen-like atoms
- For example, hydrogen atom corresponds to Z = 1; a singly ionised Helium atom He⁺ corresponds to Z = 2 etc



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Bohr's postulate, 1913

- Postulate No.1: Mechanical stability (classical mechanics)
- An electron in an atom moves in a circular orbit about the nucleus under Coulomb attraction obeying the law of classical mechanics

Coulomb's attraction = centripetal force

$$\frac{1}{4\pi\varepsilon_0} \frac{(Ze)e}{r^2} = \frac{m_e v^2}{r}$$

Assumption: the mass of the nucleus is infinitely heavy compared to the electron's 30

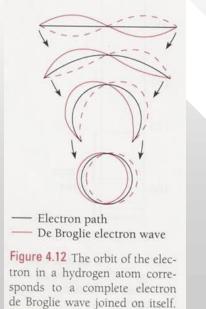
+Ze

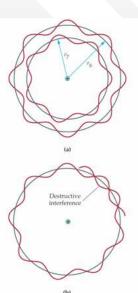
Postulate 2: condition for orbit stability

 Instead of the infinite orbit which could be possible in classical mechanics (c.f the orbits of satellites), it is only possible for an electron to move in an orbit that contains an integral number of de Broglie wavelengths,

•
$$n\lambda_n = 2\pi r_n, n = 1, 2, 3...$$

Bohr's 2nd postulate means that *n* de Broglie wavelengths must fit into the circumference of an orbit





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Electron that don't form standing

wave

- Since the electron must form standing waves in the orbits, the the orbits of the electron for each *n* is quantised
- Orbits with the perimeter that do not conform to the quantisation condition cannot persist
- All this simply means: all orbits of the electron in the atom must be quantised, and orbit that is not quantised is not allowed (hence can't exist)

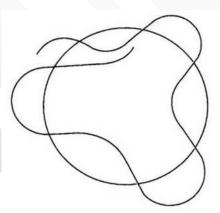
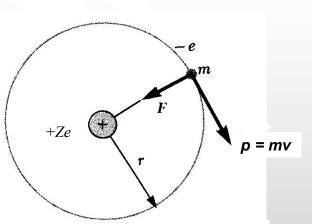


Figure 4.14 A fractional number of wavelengths cannot persist because destructive interference will occur.

Quantisation of angular momentum

- As a result of the orbit quantisation, the angular momentum of the orbiting electron is also quantised:
- $L = (m_e v) r = pr$ (definition)
- $n\lambda = 2\pi r$ (orbit quantisation)
- Combining both:
- $p = h/\lambda = nh/2\pi r$
- $L = m_e vr = p r = nh/2\pi$



Angular momentum of the electron,

 $L = p \ge r$. It is a vector quantity with its direction pointing to the direction perpendicular to the plane defined by p and r

Third postulate

- Despite the fact that it is constantly accelerating, an electron moving in such an allowed orbit does not radiate EM energy (hence total energy remains constant)
- As far as the stability of atoms is concerned, classical physics is invalid here
- My Comment: At the quantum scale (inside the atoms) some of the classical EM predictions fail (e.g. an accelerating charge radiates EM wave)

Quantisation of velocity and radius

- Combining the quantisation of angular momentum and the equation of mechanical stability we arrive at the result that:
- the allowed radius and velocity at a given orbit are also quantised:

$$r_n = 4\pi\varepsilon_0 \frac{n^2\hbar^2}{m_e Z e^2} \qquad v_n = \frac{1}{4\pi\varepsilon_0} \frac{Z e^2}{n\hbar}$$

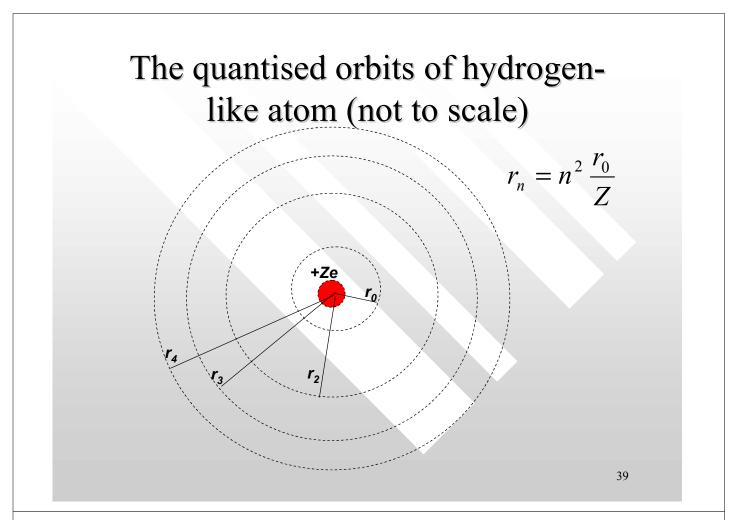
Some mathematical steps leading to
quantisation of orbits,
$$r_n = 4\pi\varepsilon_0 \frac{n^2\hbar^2}{m_e Ze^2}$$

 $m_e vr = \frac{n\hbar}{2\pi}$ (Eq.1)
 $\frac{1}{4\pi\varepsilon_0} \frac{(Ze)e}{r^2} = \frac{m_e v^2}{r} \Rightarrow v^2 = \frac{Ze^2}{4\pi\varepsilon_0 m_e} \frac{1}{r}$ (Eq. 2)
 \Rightarrow (Eq.2) \Rightarrow (Eq.1)²,
 \Rightarrow (m_evr)² = (nh/2\pi)²
 \Rightarrow LHS: $m_e^2 r^2 v^2 = m_e^2 r^2$ (Ze² / $4\pi\varepsilon_0 m_e r$)
 $= m_e r Ze^2 / 4\pi\varepsilon_0 = RHS = (nh/2\pi)^2$
 $r = n^2(h/2\pi)^2 4\pi\varepsilon_0 / Ze^2 m_e = r_n$,
 $n = 1,2,3...$ 37

Prove it yourself the quantisation of the electron velocity

$$v_n = \frac{1}{4\pi\varepsilon_0} \frac{Ze^2}{n\hbar}$$

using Eq.(1) and Eq.(2)



Important comments

- The smallest orbit charaterised by
- Z = 1, n=1 is the ground state orbit of the hydrogen

$$r_0 = \frac{4\pi\varepsilon_0 \hbar^2}{m_e e^2} = 0.5 \overset{0}{A}$$

- It's called the Bohr's radius = the typical size of an atom
- In general, the radius of an hydrogen-like ion/atom with charge Ze in the nucleus is expressed in terms of the Bohr's radius as

$$r_n = n^2 \frac{r_0}{Z}$$

- Note also that the ground state velocity of the electron in the hydrogen atom is $v_0 = 2.2 \times 10^6$ m/s << c
- non-relativistic

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• In Bohr's model for hydrogen-like atoms, an electron (mass *m*) revolves in a circle around a nucleus with positive charges *Ze*. How is the electron's velocity related to the radius *r* of its orbit?

• **A.**
$$v = \frac{1}{4\pi\varepsilon_0} \frac{Ze^2}{mr}$$
 B. $v = \frac{1}{4\pi\varepsilon_0} \frac{Ze^2}{mr^2}$ **C.** $v = \frac{1}{4\pi\varepsilon_0} \frac{Ze}{mr^2}$

- $\mathbf{D} \cdot v^2 = \frac{1}{4\pi\varepsilon_0} \frac{Ze^2}{mr}$ E. Non of the above
- Solution: I expect you to be able to derive it from scratch without memorisation
- ANS: D, Schaum's series 3000 solved problems, Q39.13, pg 722 modified

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Strongly recommending the Physics 2000 interactive physics webpage by the University of Colorado

For example the page http://www.colorado.edu/physics/2000/quantu mzone/bohr.html provides a very interesting explanation and simulation on atom and Bohr model in

particular.

Please visit this page if you go online

Recap

• The hydrogen-like atom's radii are quantised according to:

$$r_n = n^2 \frac{r_0}{Z}$$

- The quantisation is a direct consequence of the postulate that electron wave forms stationary states (standing waves) at the allowed orbits
- The smallest orbit or hydrogen, the Bohr's radius

$$r_0 = \frac{4\pi\varepsilon_0 \hbar^2}{m_e e^2} = 0.5 \overset{0}{A}$$

Postulate 4

• Similar to Einstein's postulate of the energy of a photon

EM radiation is emitted if an electron initially moving in an orbit of total energy E_i , discontinuously changes it motion so that it moves in an orbit of total energy $E_f(E_i > E_f)$. The frequency of the emitted radiation,

$$\nu = (E_i - E_f)/h;$$
$$E_i > E_f$$

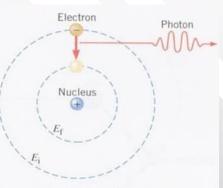
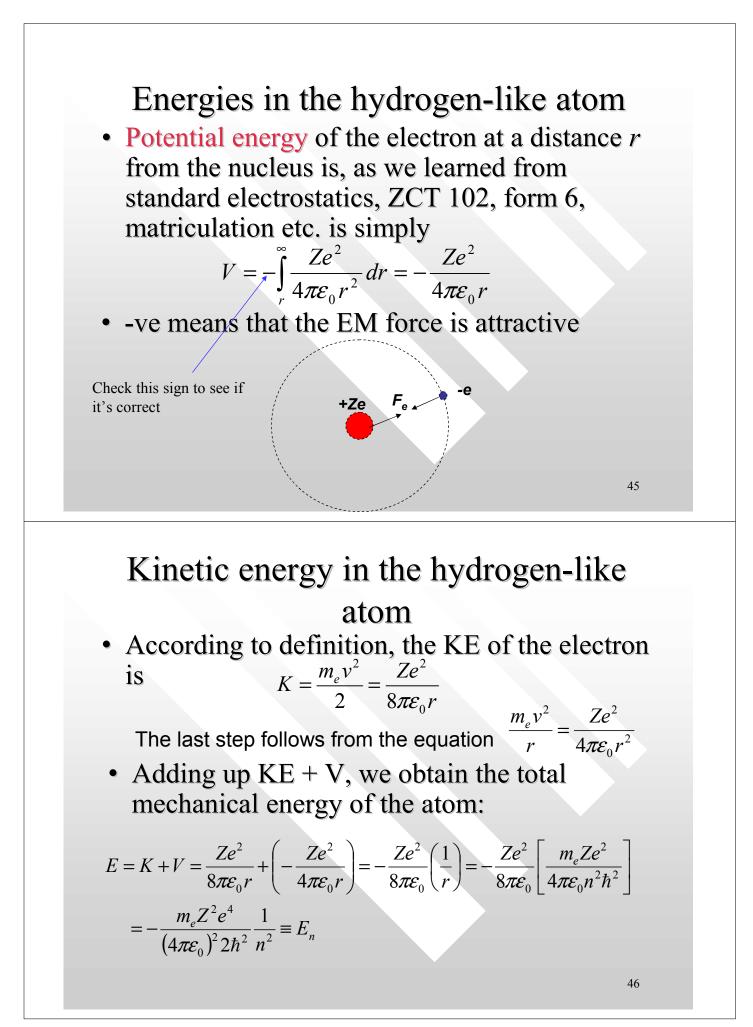


Figure 30.5 In the Bohr model, a photon is emitted when the electron drops from a larger, higher-energy orbit (energy $= E_i$) to a smaller, lower-energy orbit (energy $= E_f$).



The ground state energy

• For the hydrogen atom (Z = 1), the ground state energy (which is characterised by n = 1)

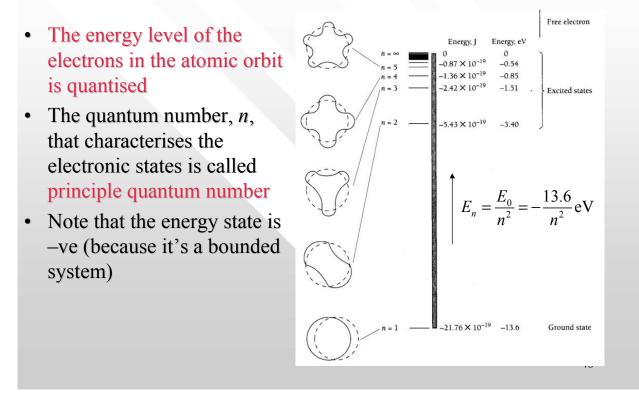
$$E_0 \equiv E_n (n=1) = -\frac{m_e e^4}{(4\pi\epsilon_0)^2 2\hbar^2} = -13.6\text{eV}$$

In general the energy level of a hydrogen like atom with Ze nucleus charges can be expressed in terms of

$$E_n = \frac{Z^2 E_0}{n^2} = -\frac{13.6Z^2}{n^2} \,\mathrm{eV}$$

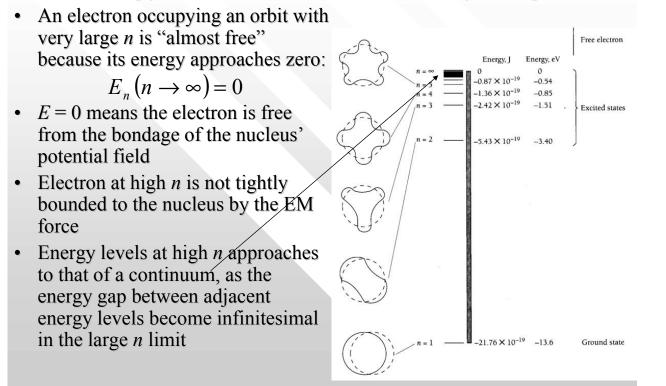
Quantisation of energy levels

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Energy of the electron at very large *n*

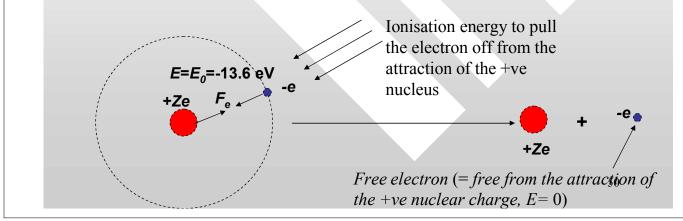


Ionisation energy of the hydrogen atom

• The energy input required to remove the electron from its ground state to infinity (ie. to totally remove the electron from the bound of the nucleus) is simply

$$E_{ionisation} = E_{\infty} - E_0 = -E_0 = 13.6 \text{eV}$$

• this is the ionisation energy of hydrogen

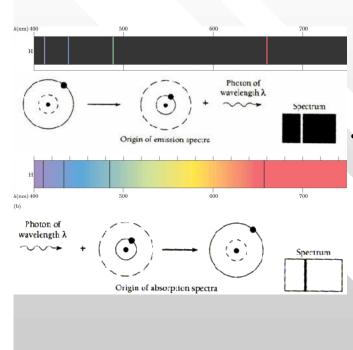


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Two important quantities to remember

- As a practical rule, it is strongly advisable to remember the two very important values
- (i) the Bohr radius, $r_0 = 0.53$ A and
- (ii) the ground state energy of the hydrogen atom, $E_0 = -13.6 \text{ eV}$

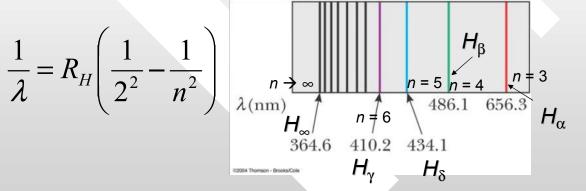
Bohr's 4th postulate explains the line spectrum



- When atoms are excited to an energy state above its ground state, they shall radiate out energy (in forms of photon) within at the time scale of $\sim 10^{-8}$ s upon their de-excitations to lower energy states –emission spectrum explained
 - When a beam of light with a range of wavelength sees an atom, the few particular wavelengths that matches the allowed energy gaps of the atom will be absorbed, leaving behind other unabsorbed wavelengthsto become the bright background in the absorption spectrum. Hence absorption spectrum explained

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Balmer series and the empirical emission spectrum equation Since 1860 – 1898 Balmer have found an empirical formula that correctly predicted the wavelength of four visible lines of hydrogen:



where $n = 3,4,5,...,R_H$ is called the Rydberg constant, experimentally measured to be $R_H = 1.0973732 \times 10^7 \text{ m}^{-1}_{_{53}}$

Example

• For example, for the H_{β} (486.1 nm) line, n = 4 in the empirical formula

$$\frac{1}{\lambda} = R_H \left(\frac{1}{2^2} - \frac{1}{n^2} \right)$$

• According to the empirical formula the wavelength of the hydrogen beta line is

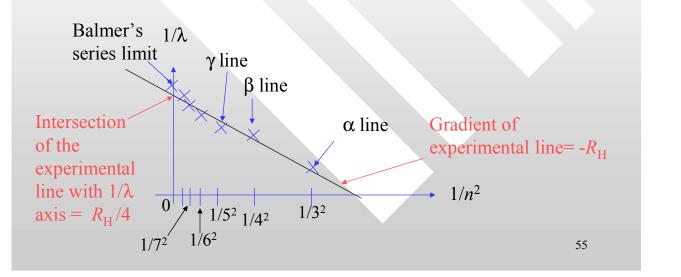
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$$\frac{1}{\lambda_{\beta}} = R_{H} \left(\frac{1}{2^{2}} - \frac{1}{4^{2}} \right) = R_{H} \left(\frac{3}{16} \right) = \frac{3(1.0973732 \times 10^{7} \,\mathrm{m}^{-1})}{16}$$
$$\implies \lambda_{\alpha} = 486 \,\mathrm{nm}$$

• which is consistent with the observed value

Experimental measurement of the Rydberg constant, $R_{\rm H}$

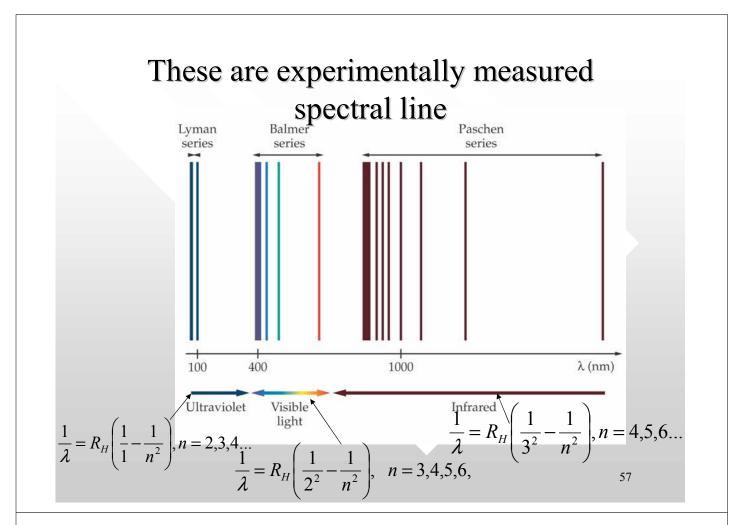
One measures the wavelengths of the α , β , γ , ...lines (corresponding to $n = 3, 4, 5, ...\infty$) in Balmer's empirical formula $\frac{1}{\lambda} = R_H \left(\frac{1}{2^2} - \frac{1}{n^2}\right)$ Then plot $1/\lambda$ as a function of $1/n^2$. Note that here $n \ge 3$.



Other spectra series

- Apart from the Balmer series others spectral series are also discovered: Lyman, Paschen and Brackett series
- The wavelengths of these spectral lines are also given by the similar empirical equation as

$$\frac{1}{\lambda} = R_{H} \left(\frac{1}{1} - \frac{1}{n^{2}} \right), \quad n = 2, 3, 4, \dots$$
Lyman series, ultraviolet region
$$\frac{1}{\lambda} = R_{H} \left(\frac{1}{3^{2}} - \frac{1}{n^{2}} \right), \quad n = 4, 5, 6, \dots$$
Paschen series, infrared region
$$\frac{1}{\lambda} = R_{H} \left(\frac{1}{4^{2}} - \frac{1}{n^{2}} \right), \quad n = 5, 6, 7, \dots$$
Brackett series, infrared region



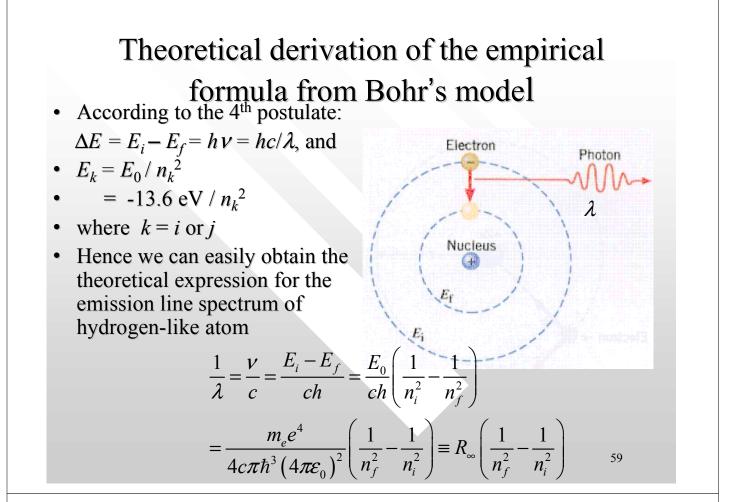
The empirical formula needs a theoretical explanation

 $\frac{1}{\lambda} = R_H \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right)$

is an empirical formula with R_H measured to be $R_H = 1.0973732 \times 10^7 \text{ m}^{-1}$.

Can the Bohr model provide a sound theoretical explanation to the form of this formula and the numerical value of R_H in terms of known physical constants?

The answer is: YES



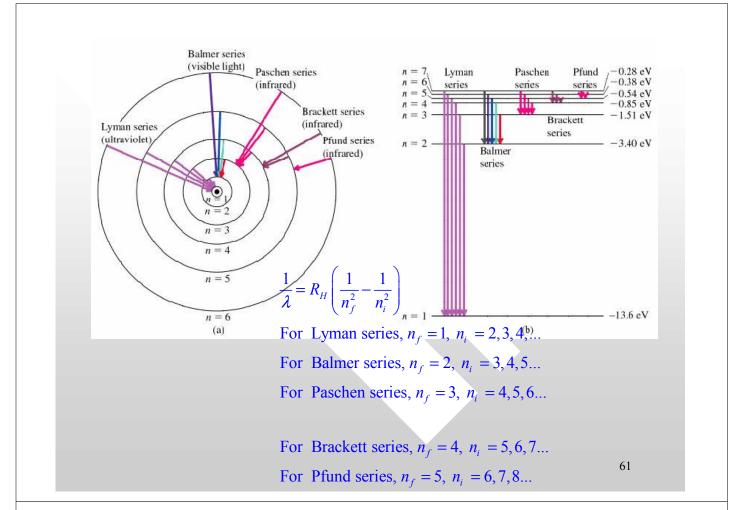
The theoretical Rydberg constant

$$R_{\infty} \equiv \frac{m_e e^4}{4c\pi\hbar^3 (4\pi\epsilon_0)^2} = 1.0984119 \times 10^7 \,\mathrm{m}^{-1}$$

• The theoretical Rydberg constant, R_{∞} , agrees with the experimental one up a precision of less than 1%

$$R_{H} = 1.0973732 \times 10^{7} \,\mathrm{m}^{-1}$$

This is a remarkable experimental verification of the correctness of the Bohr model



Real life example of atomic emission

 AURORA are caused by streams of fast photons and electrons from the sun that excite atoms in the upper atmosphere. The green hues of an auroral display come from oxygen



Example

- Suppose that, as a result of a collision, the electron in a hydrogen atom is raised to the second excited state (n = 3).
- What is (i) the energy and (ii) wavelength of the photon emitted if the electron makes a direct transition to the ground state?
- What are the energies and the wavelengths of the two photons emitted if, instead, the electron makes a transition to the first excited state (*n*=2) and from there a subsequent transition to the ground state?

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Make use of $E_k = E_0 / n_k^2 = -13.6 \text{ eV} / n_k^2$

The energy of the proton emitted in the transition from the n = 3 to the n = 1 state is

$$\Delta E = E_3 - E_1 = -13.6 \left(\frac{1}{3^2} - \frac{1}{1^2}\right) eV = 12.1 eV$$

the wavelength of this photon is

$$\lambda = \frac{c}{v} = \frac{ch}{\Delta E} = \frac{1242eV \cdot nm}{12.1eV} = 102nm$$

Likewise the energies of the two photons emitted in the transitions from $n = 3 \rightarrow n = 2$ and $n = 2 \rightarrow n = 1$ are, respectively,

$$\Delta E = E_3 - E_2 = -13.6 \left(\frac{1}{3^2} - \frac{1}{2^2}\right) = 1.89 \text{eV}$$
 with wavelength

$$\Delta E = E_2 - E_1 = -13.6 \left(\frac{1}{2^2} - \frac{1}{1^2} \right) = 10.2 \text{eV}$$
 with wavelength

$$h = 3$$

$$\Delta E = E_3 - E_1$$

$$\Delta E = E_2 - E_1$$

$$n = 1, \text{ ground state}$$

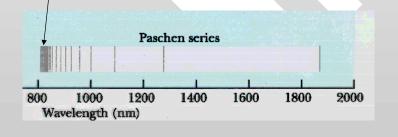
$$\lambda = \frac{ch}{\Delta E} = \frac{1242eV \cdot nm}{1.89eV} = 657 \text{ m}$$

$$\lambda = \frac{ch}{\Delta E} = \frac{1242eV \cdot nm}{10.2eV_{64}} = 121\text{nm}$$

m

Example

- The series limit of the Paschen $(n_f = 3)$ is 820.1 nm
- The series limit of a given spectral series is the shortest photon wavelength for that series
- The series limit of a spectral series is the wavelength corresponds to $n_i \rightarrow \infty$
- What are two longest wavelengths of the Paschen series?



Solution

- Note that the Rydberg constant is not provided
- But by definition the series limit and the Rydberg constant is closely related
- We got to make use of the series limit to solve that problem
- By referring to the definition of the series limit,

$$\frac{1}{\lambda} = R_H \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right) \xrightarrow{n_i \to \infty} \frac{1}{\lambda_\infty} = \frac{R_H}{n_f^2}$$

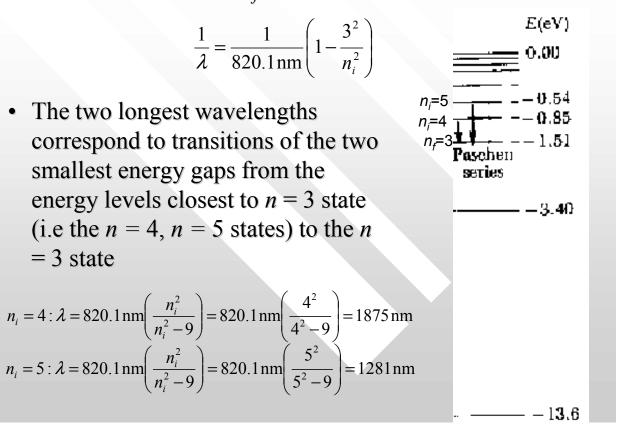
• Hence we can substitute $R_H = n_f^2 / \lambda_{\infty}$ into

$$\frac{1}{\lambda} = R_H \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right)$$

• and express it in terms of the series limit as $\frac{1}{\lambda} = \frac{1}{\lambda_{\infty}} \left(1 - \frac{n_f^2}{n_i^2} \right)$

•
$$n_i = 4, 5, 6...; n_f = 3$$

• For Paschen series, $n_f = 3$, $\lambda_{\infty} = 820.1$ nm



Example

- Given the ground state energy of hydrogen atom -13.6 eV, what is the longest wavelength in the hydrogen's Balmer series?
- Solution:

$$\Delta E = E_i - E_f = -13.6 \text{ eV} (1/n_i^2 - 1/n_f^2) = hc/\lambda$$

• Balmer series: $n_f = 2$. Hence, in terms of 13.6 eV the wavelengths in Balmer series is given by

$$\lambda_{Balmer} = \frac{hc}{13.6\text{eV}\left(\frac{1}{4} - \frac{1}{n_i^2}\right)} = \frac{1240\text{eV} \cdot \text{nm}}{13.6\text{eV}\left(\frac{1}{4} - \frac{1}{n_i^2}\right)} = \frac{91\text{nm}}{\left(\frac{1}{4} - \frac{1}{n_i^2}\right)}, \quad n_i = 3, 4, 5...$$

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$$\lambda_{Balmer} = \frac{91 \text{nm}}{\left(\frac{1}{4} - \frac{1}{n_i^2}\right)}, \ n_i = 3, 4, 5...$$

- longest wavelength corresponds to the transition from the $n_i = 3$ states to the $n_f = 2$ states
- Hence $\lambda_{Balmer,max} = \frac{91 \text{nm}}{\left(\frac{1}{4} \frac{1}{3^2}\right)} = 655.2 \text{nm}$
 - This is the red H_{α} line in the hydrogen's Balmer series
 - Can you calculate the shortest wavelength (the series limit) for the Balmer series? Ans = 364 nm

PYQ 2.18 Final Exam 2003/04

- Which of the following statements are true?
- I.. the ground states are states with lowest energy
- II. ionisation energy is the energy required to raise an electron from ground state to free state
- III. Balmer series is the lines in the spectrum of atomic hydrogen that corresponds to the transitions to the n = 1 state from higher energy states
- **A.** I,IV **B.** I,II, IV **C.** I, III,IV
- **D.** I, II **E.** II,III
- ANS: D, My own question
- (note: this is an obvious typo error with the statement IV missing. In any case, only statement I, II are true.)

PYQ 1.5 KSCP 2003/04

- An electron collides with a hydrogen atom in its ground state and excites it to a state of n =3. How much energy was given to the hydrogen atom in this collision?
- **A.** -12.1 eV **B.** 12.1 eV **C.** -13.6 eV
- **D.** 13.6 eV **E.** Non of the above
- Solution:

$$\Delta E = E_3 - E_0 = \frac{E_0}{3^2} - E_0 = \frac{(-13.6\text{eV})}{3^2} - (-13.6\text{eV}) = 12.1\text{eV}$$

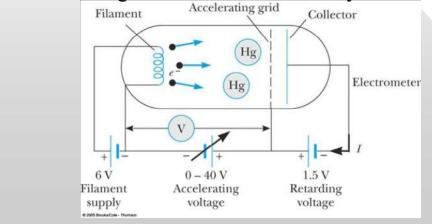
• ANS: B, Modern Technical Physics, Beiser, Example 25.6, pg. 786

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Frank-Hertz experiment The famous experiment that shows the excitation of atoms to

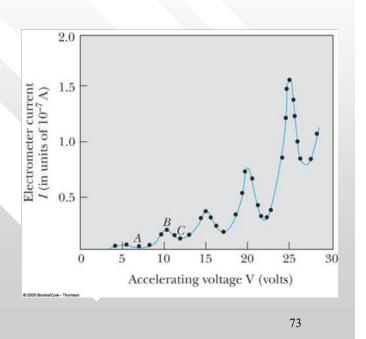
- The famous experiment that shows the excitation of atoms to discrete energy levels and is consistent with the results suggested by line spectra
- Mercury vapour is bombarded with electron accelerated under the potential V (between the grid and the filament)
- A small potential V_0 between the grid and collecting plate prevents electrons having energies less than a certain minimum from contributing to the current measured by ammeter



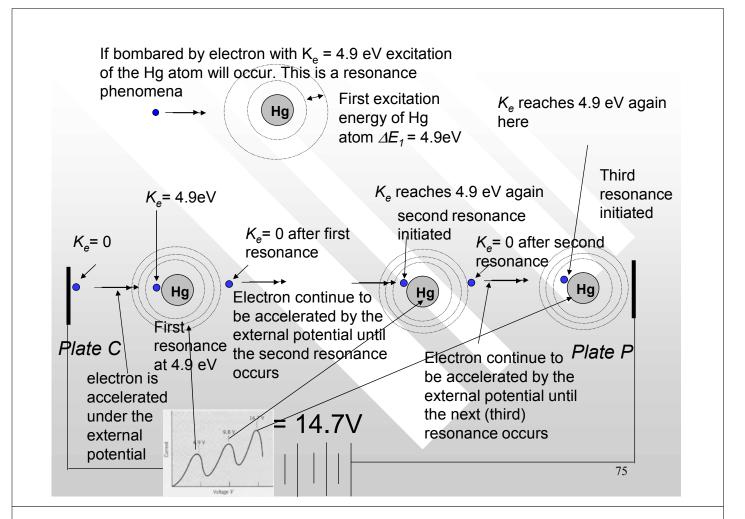
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The electrons that arrive at the anode peaks at equal voltage intervals of 4.9 V

- As V increases, the current measured also increases
- The measured current drops at multiples of a critical potential
- V = 4.9 V, 9.8 V, 14.7 V



- **Interpretation** As a result of inelastic collisions between the accelerated electrons of KE 4.9 eV with the Hg atom, the Hg atoms are excited to an energy level above its ground state
- At this critical point, the energy of the accelerating electron equals to • that of the energy gap between the ground state and the excited state
- This is a resonance phenomena, hence current increases abruptly
- After inelastically exciting the atom, the original (the bombarding) • electron move off with too little energy to overcome the small retarding potential and reach the plate
- As the accelerating potential is raised further, the plate current again increases, since the electrons now have enough energy to reach the plate
- Eventually another sharp drop (at 9.8 V) in the current occurs because, again, the electron has collected just the same energy to excite the same energy level in the other atoms



- The higher critical potentials result from two or more inelastic collisions and are multiple of the lowest (4.9 V)
- The excited mercury atom will then deexcite by radiating out a photon of exactly the energy (4.9 eV) which is also detected in the Frank-Hertz experiment
- The critical potential verifies the existence of atomic levels

Bohr's correspondence principle

- The predictions of the quantum theory for the behaviour of any physical system must correspond to the prediction of classical physics in the limit in which the quantum number specifying the state of the system becomes very large:
- lim quantum theory = classical theory $n \to \infty$
- At large *n* limit, the Bohr model must reduce to a "classical atom" which obeys classical theory

In other words...

• The laws of quantum physics are valid in the atomic domain; while the laws of classical physics is valid in the classical domain; where the two domains overlaps, both sets of laws must give the same result.

PYQ 20 Test II 2003/04

- Which of the following statements are correct?
- I Frank-Hertz experiment shows that atoms are excited to discrete energy levels
- II Frank-Hertz experimental result is consistent with the results suggested by the line spectra

III The predictions of the quantum theory for the behaviour of any physical system must correspond to the prediction of classical physics in the limit in which the quantum number specifying the state of the system becomes very large

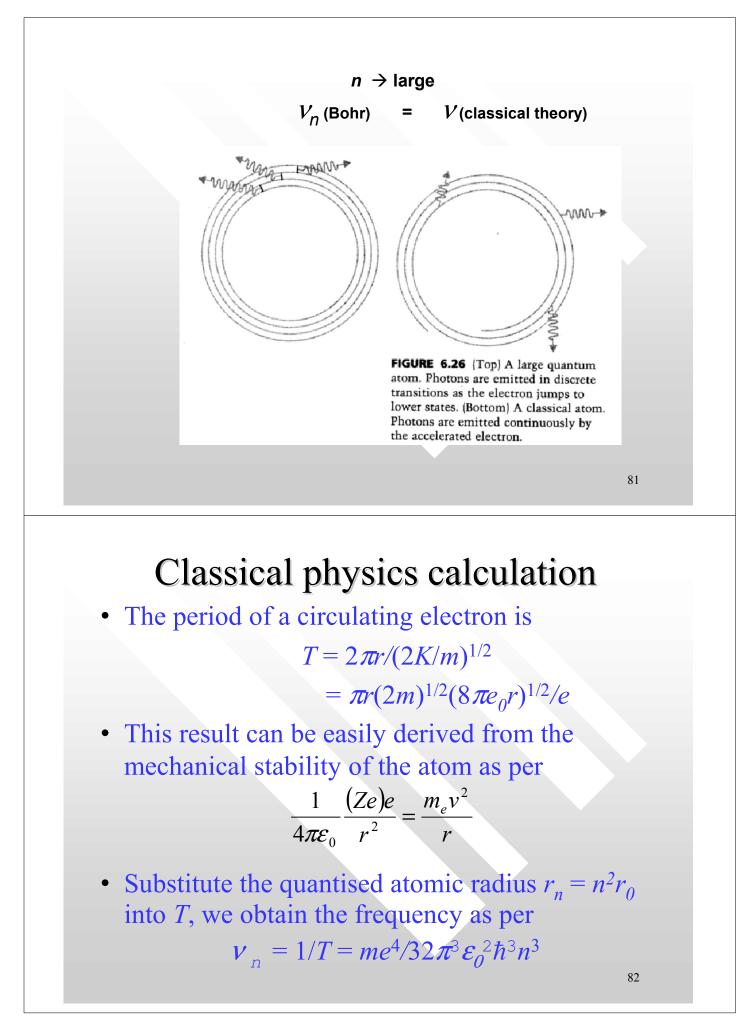
- **IV**The structure of atoms can be probed by using electromagnetic radiation
- A. II,III B. I, II,IV C. II, III, IV
- D. I,II, III, IV E. Non of the above
- ANS:D, My own questions

Example (Read it yourself)

- Classical EM predicts that an electron in a circular motion will radiate EM wave at the same frequency
- According to the correspondence principle, the Bohr model must also reproduce this result in the large *n* limit

More quantitatively

- In the limit, $n = 10^3 10^4$, the Bohr atom would have a size of 10^{-3} m
- This is a large quantum atom which is in classical domain
- The prediction for the photon emitted during transition around the $n = 10^3 - 10^4$ states should equals to that predicted by classical EM theory.



Based on Bohr's theory

• Now, for an electron in the Bohr atom at energy level $n = 10^3 - 10^4$, the frequency of an radiated photon when electron makes a transition from the *n* state to *n*-1 state is given by

Where we have made use of

 $E_n / h = E_0 / n^2 h = (-me^4/64\pi^3 \varepsilon_0^2 \hbar^3 n^2).$

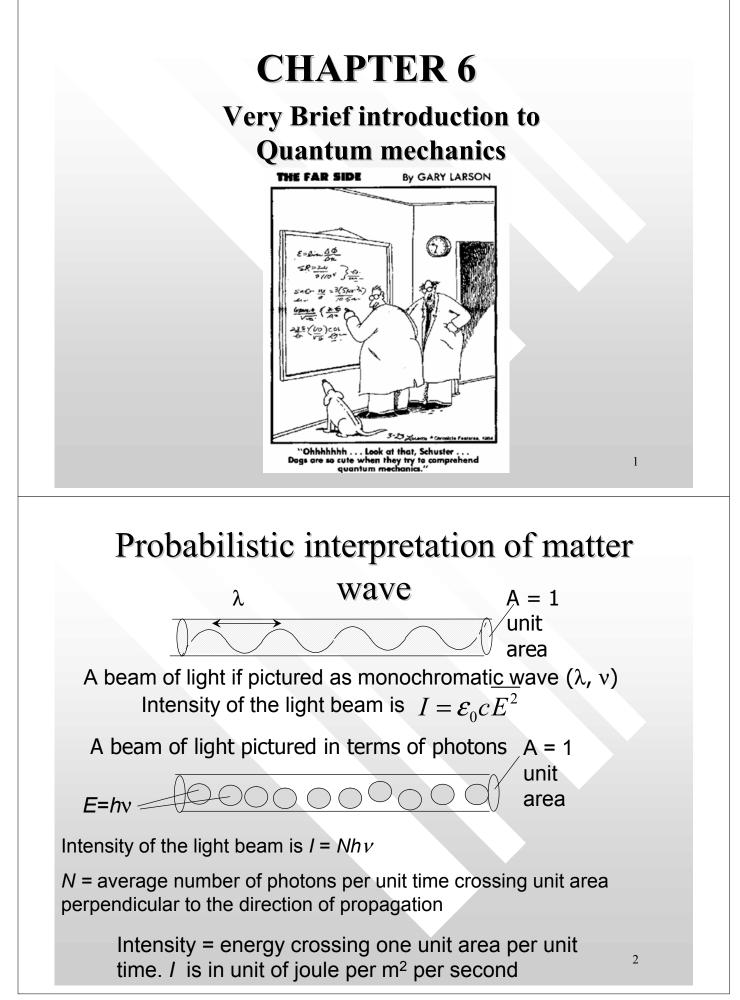
• In the limit of large *n*,

 $v \approx (me^{4}/64\pi^{3}\varepsilon_{0}^{2}\hbar^{3})[2n/n^{4}]$ = $(me^{4}/32\pi^{3}\varepsilon_{0}^{2}\hbar^{3})[1/n^{3}]$

Classical result and Quantum calculation meets at $n \rightarrow \infty$

• Hence, in the region of large *n*, where classical and quantum physics overlap, the classical prediction and that of the quantum one is identical

 $v_{classical} = v_{Bohr} = (me^4/32\pi^3\varepsilon_0^2\hbar^3)[1/n^3]$



Probability of observing a photon

- Consider a beam of light
- In wave picture, $E = E_0 \sin(kx \omega t)$, electric field in radiation
- Intensity of radiation in wave picture is

$$I = \varepsilon_0 c E^2$$

- On the other hand, in the photon picture, I = Nhv
- Correspondence principle: what is explained in the wave picture has to be consistent with what is explained in the photon picture in the limit N→infinity:

$$I = \mathcal{E}_0 c E^2 = Nh v$$

3

4

Statistical interpretation of radiation

- The probability of observing a photon at a point in unit time is proportional to N _____
- However, since $Nh\nu = \varepsilon_0 c \overline{E^2} \propto \overline{E^2}$
- the probability of observing a photon must also
- This means that the probability of observing a photon at any point in space is proportional to the square of the averaged electric field strength at that point

 $Prob(\mathbf{r}) \propto F^2$

Square of the mean of the square of the wave field amplitude

What is the physical interpretation of matter wave?

• we will call the mathematical representation of the de Broglie's wave / matter wave associated with a given particle (or an physical entity) as

The wave function, Ψ

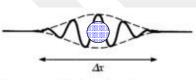


FIGURE 6.14 An idealized wave packet localized in space over a region Δx is the perposition of many waves of different amplitudes and frequencies.

- We wish to answer the following questions:
- Where is exactly the particle located within Δx ? the locality of a particle becomes fuzzy when it's represented by its matter wave. We can no more tell for sure where it is exactly located.
- Recall that in the case of conventional wave physics, $|\text{field amplitude}|^2$ is proportional to the intensity of the wave). Now, what does $|\Psi|^2$ physically mean?

Probabilistic interpretation of (the square of) matter wave

- As seen in the case of radiation field, |electric field's amplitude|² is proportional to the probability of finding a photon
- In exact analogy to the statistical interpretation of the radiation field,
- $P(x) = |\Psi|^2$ is interpreted as the probability density of observing a material particle
- More quantitatively,
- Probability for a particle to be found between point a and b is

$$p(a \le x \le b) = \int_{a}^{b} P(x) dx = \int_{a}^{b} |\Psi(x,t)|^2 dx$$

 $p_{ab} = \int_{a}^{b} |\Psi(x,t)|^{2} dx \text{ is the probability to find the}$ particle between *a* and *b*• It value is given by the area under the curve of probability density between *a* and *b* $\int |\Psi|^{2} \int \int |\Psi|^{2} \int |\Psi|^{2}$

Expectation value

• Any physical observable in quantum mechanics, *O* (which is a function of position, *x*), when measured repeatedly, will yield an expectation value of given by

$$\left\langle O\right\rangle = \frac{\int_{-\infty}^{\infty} \Psi O \Psi^* dx}{\int_{-\infty}^{\infty} \Psi \Psi^* dx} = \frac{\int_{-\infty}^{\infty} O |\Psi|^2 dx}{\int_{-\infty}^{\infty} \Psi \Psi^* dx}$$

- Example, O can be the potential energy, position, etc.
- (Note: the above statement is not applicable to energy and linear momentum because they cannot be express explicitly as a function of *x* due to uncertainty principle)...

Example of expectation value: average position measured for a quantum particle

• If the position of a quantum particle is measured repeatedly with the same initial conditions, the averaged value of the position measured is given by

$$\langle x \rangle = \frac{\int_{-\infty}^{\infty} x |\Psi|^2 dx}{1} = \int_{-\infty}^{\infty} x |\Psi|^2 dx$$

Example

- A particle limited to the *x* axis has the wave function Ψ = *ax* between *x*=0 and *x*=1; Ψ = 0 else where.
- (a) Find the probability that the particle can be found between *x*=0.45 and *x*=0.55.
- (b) Find the expectation value <*x*> of the particle's position

Solution

• (a) the probability is

$$\int_{-\infty}^{\infty} |\Psi|^2 dx = \int_{0.45}^{0.55\infty} x^2 dx = a^2 \left[\frac{x^3}{3}\right]_{0.45}^{0.55} = 0.0251a^2$$

• (b) The expectation value is

$$\langle x \rangle = \int_{-\infty}^{\infty} x |\Psi|^2 dx = \int_{0}^{1} x^3 dx = a^2 \left[\frac{x^3}{4}\right]_{0}^{1} = \frac{a^2}{4}$$

Max Born and probabilistic interpretation

- Hence, a particle's wave function gives rise to a *probabilistic interpretation* of the position of a particle
- Max Born in 1926



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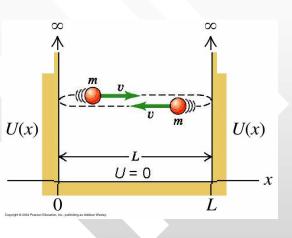
German-British physicist who worked on the mathematical basis for <u>quantum mechanics</u>. Born's most important contribution was his suggestion that the <u>absolute square</u> of the wavefunction in the <u>Schrödinger equation</u> was a measure of the probability of finding the particle at a given location. Born shared the 1954 Nobel Prize in physics with <u>Bethe</u>

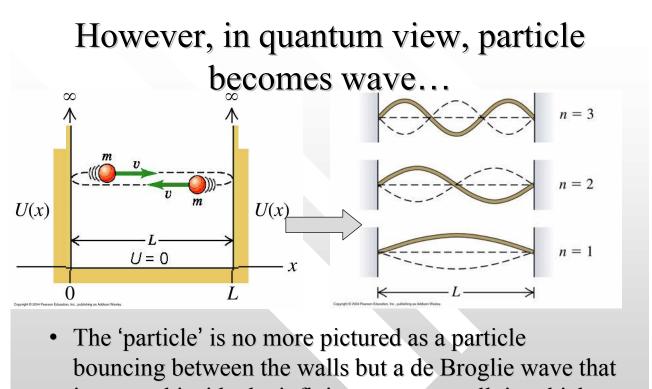
PYQ 2.7, Final Exam 2003/04

- A large value of the probability density of an atomic electron at a certain place and time signifies that the electron
- A. is likely to be found there
- B. is certain to be found there
- C. has a great deal of energy there
- D. has a great deal of charge
- E. is unlikely to be found there
- ANS:A, Modern physical technique, Beiser, MCP 25, pg. 802

Particle in in an infinite well (sometimes called particle in a box)

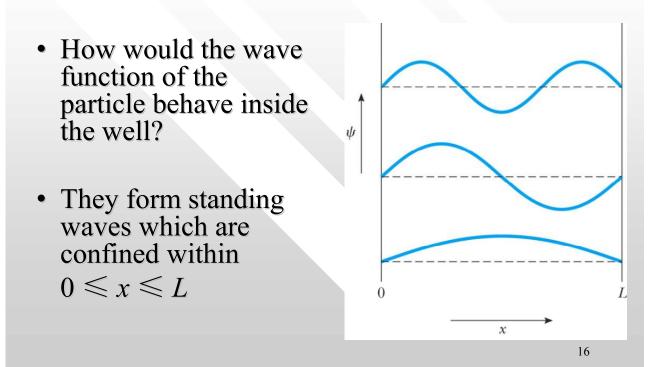
- Imagine that we put particle (e.g. an electron) into an "infinite well" with width *L* (e.g. a potential trap with sufficiently high barrier)
- In other words, the particle is confined within 0 < x < L
- In Newtonian view the particle is traveling along a straight line bouncing between two rigid walls





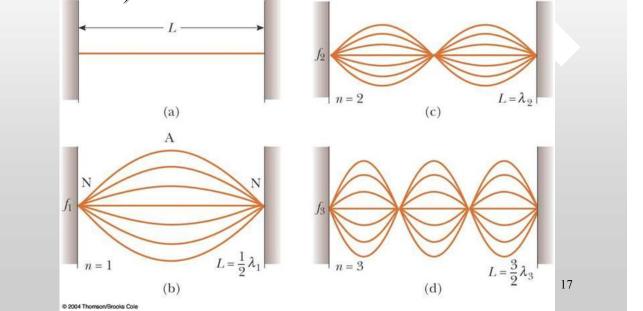
is trapped inside the infinite quantum well, in which they form standing waves

Particle forms standing wave within the infinite well



Standing wave in general

- Shown below are standing waves which ends are fixed at x = 0 and x = L
- For standing wave, the speed is constant, $(v = \lambda f = constant)$



Mathematical description of standing waves

• In general, the equation that describes a standing wave (with a constant width *L*) is simply:

$$L = n\lambda_n/2$$

 $n = 1, 2, 3, \dots$ (positive, discrete integer)

- *n* characterises the "mode" of the standing wave
- n = 1 mode is called the 'fundamental' or the first harmonic
- n = 2 is called the second harmonics, etc.
- λ_n are the wavelengths associated with the *n*-th mode standing waves
- The lengths of λ_n is "quantised" as it can take only discrete values according to $\lambda_n = 2L/n$

Energy of the particle in the box

Recall that

$$V(x) = \begin{cases} \infty, & x \le 0, x \ge L \\ 0, & 0 < x < L \end{cases}$$

- For such a free particle that forms standing waves in the box, it has no potential energy
- It has all of its mechanical energy in the form of kinetic energy only
- Hence, for the region 0 < x < L, we write the total energy of the particle as

$$E = K + V = p^2/2m + 0 = p^2/2m$$

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Energies of the particle are quantised

 Due to the quantisation of the standing wave (which comes in the form of λ_n = 2L/n), the momentum of the particle must also be quantised due to de Broglie's postulate:

$$p \rightarrow p_n = \frac{h}{\lambda_n} = \frac{nh}{2L}$$

It follows that the total energy of the particle is also quantised: $E \rightarrow E_n = \frac{p_n^2}{2m} = n^2 \frac{\pi^2 \hbar^2}{2mL^2}$

$$E_n = \frac{p_n^2}{2m} = n^2 \frac{h^2}{8mL^2} = n^2 \frac{\pi^2 \hbar^2}{2mL^2}$$

The *n* = 1 state is a characteristic state called the ground state = the state with lowest possible energy (also called zero-point energy)

$$E_n(n=1) \equiv E_0 = \frac{\pi^2 \hbar^2}{2mL^2}$$

Ground state is usually used as the reference state when we refer to ``excited states'' (n = 2, 3 or higher)

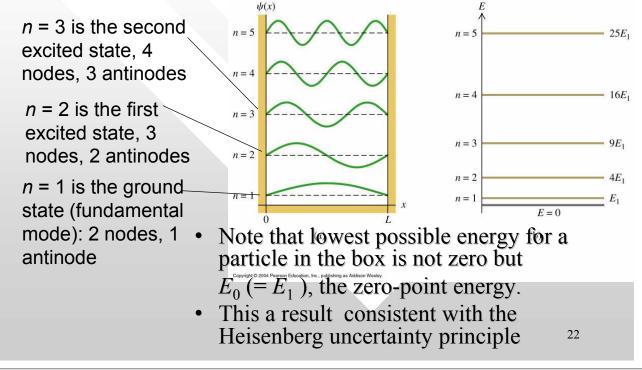
The total energy of the *n*-th state can be expressed in term of the ground state energy as

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$$E_n = n^2 E_0$$
 (*n* = 1,2,3,4...)

The higher *n* the larger is the energy level

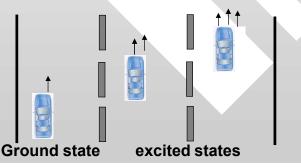
- Some terminology
- n = 1 corresponds to the ground state
- n = 2 corresponds to the first excited state, etc



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Simple analogy

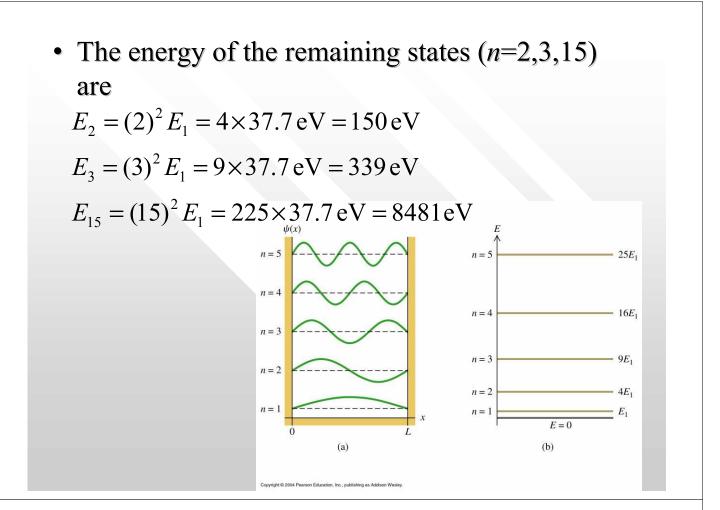
• Cars moving in the right lane on the highway are in 'excited states' as they must travel faster (at least according to the traffic rules). Cars travelling in the left lane are in the ``ground state" as they can move with a relaxingly lower speed. Cars in the excited states must finally resume to the ground state (i.e. back to the left lane) when they slow down



Example on energy levels

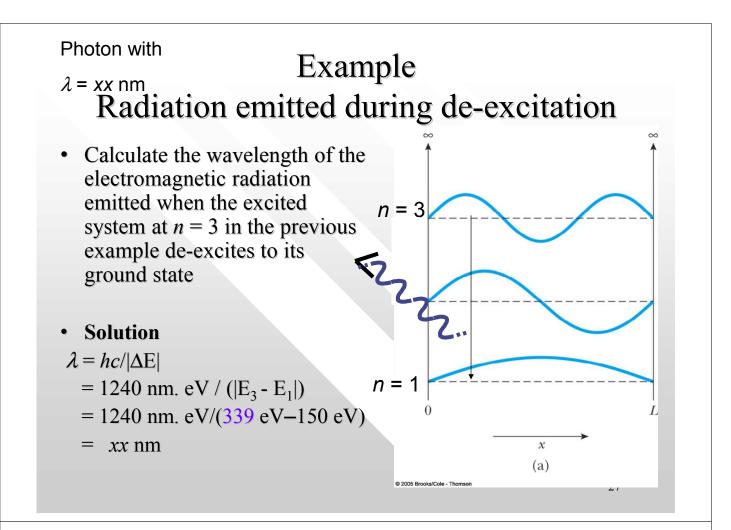
- Consider an electron confined by electrical force to an infinitely deep potential well whose length *L* is 100 pm, which is roughly one atomic diameter. What are the energies of its three lowest allowed states and of the state with *n* = 15?
- SOLUTION
- For n = 1, the ground state, we have

$$E_1 = (1)^2 \frac{h^2}{8m_e L^2} = \frac{(6.63 \times 10^{-34} \,\mathrm{Js})^2}{(9.1 \times 10^{-31} \,\mathrm{kg})(100 \times 10^{-12} \,\mathrm{m})^2} = 6.3 \times 10^{-18} \,\mathrm{J} = 37.7 \,\mathrm{eV}$$



Question continued

- When electron makes a transition from the *n* = 3 excited state back to the ground state, does the energy of the system increase or decrease?
- Solution:
- The energy of the system decreases as energy drops from 339 eV to 150 eV
- The lost amount $|\Delta E| = E_3 E_1 = 339 \text{ eV} 150$ eV is radiated away in the form of electromagnetic wave with wavelength λ obeying $\Delta E = hc/\lambda$



Example

A macroscopic particle's quantum state

 Consider a 1 microgram speck of dust moving back and forth between two rigid walls separated by 0.1 mm. It moves so slowly that it takes 100 s for the particle to cross this gap.
 What quantum number describes this motion?

Solution

• The energy of the particle is

$$E(=K) = \frac{1}{2}mv^{2} = \frac{1}{2}(1 \times 10^{-9} \text{kg}) \times (1 \times 10^{-6} \text{ m/s})^{2} = 5 \times 10^{-22} \text{ J}$$

• Solving for *n* in $E_n = n^2 \frac{\pi^2 \hbar^2}{2mL^2}$

• yields
$$n = \frac{L}{h}\sqrt{8mE} \approx 3 \times 10^{14}$$

- This is a very large number
- It is experimentally impossible to distinguish between the $n = 3 \ge 10^{14}$ and $n = 1 + (3 \ge 10^{14})$ states, so that the quantized nature of this motion would never reveal itself
- The quantum states of a macroscopic particle cannot be experimentally discerned (as seen in previous example)
- Effectively its quantum states appear as a continuum



allowed energies in classical system – appear continuous (such as energy carried by a wave; total mechanical energy of an orbiting planet, etc.) $\Delta E \approx 5 \times 10^{-22} / 10^{14}$ =1.67 × 10^{-36} = 10^{-17} eV

 $E(n=10^{14}) = 5x10^{-22}J$

is too tiny to the discerned

descret energies in quantised system – discrete (such as energy levels in an atom, energies carried by a photon)

PYQ 4(a) Final Exam 2003/04

- An electron is contained in a one-dimensional box of width 0.100 nm. Using the particle-in-abox model,
- (i) Calculate the n = 1 energy level and n = 4energy level for the electron in eV.
- (ii) Find the wavelength of the photon (in nm) in making transitions that will eventually get it from the the n = 4 to n = 1 state
- Serway solution manual 2, Q33, pg. 380, modified

- 4a(i) In the particle-in-a-box model, standing wave is formed in the box of dimension L: $\lambda_n = \frac{2L}{2}$
- The energy of the particle in the box is given by

$$K_{n} = E_{n} = \frac{p_{n}^{2}}{2m_{e}} = \frac{(h/\lambda_{n})^{2}}{2m_{e}} = \frac{n^{2}h^{2}}{8m_{e}L^{2}} = \frac{n^{2}\pi^{2}\hbar^{2}}{2m_{e}L^{2}}$$
$$E_{1} = \frac{\pi^{2}\hbar^{2}}{2m_{e}L^{2}} = 37.7 \text{ eV} \qquad E_{4} = 4^{2}E_{1} = 603 \text{ eV}$$

- 4a(ii)
- The wavelength of the photon going from n = 4 to n =1 is $\lambda = hc/(E_6 - E_1)$
- = 1240 eV nm/(603 37.7) eV = 2.2 nm

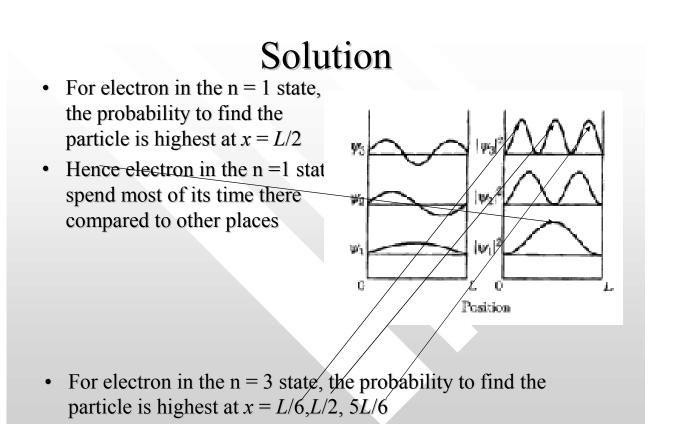
Example on the probabilistic interpretation:

Where in the well the particle spend most of its time?

- The particle spend most of its time in places where its probability to be found is largest
- Find, for the n = 1 and for n =3 quantum states respectively, the points where the electron is most likely to be found

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• Hence electron in the n =3 state spend most of its time at this three places

Boundary conditions and normalisation of the wave function in the infinite well

- Due to the probabilistic interpretation of the wave function, the probability density P(x) = |Ψ|² must be such that
- $P(x) = |\Psi|^2 > 0$ for 0 < x < L
- The particle has no where to be found at the boundary as well as outside the well, i.e P(x) = |Ψ|² = 0 for x ≤ 0 and x ≥ L

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• The probability density is zero at the boundaries

- Inside the well, the particle is bouncing back and forth between the walls
- It is obvious that it must exist within somewhere within the well
- This means:

$$\int_{-\infty}^{\infty} P(x) dx = \int_{0}^{L} |\Psi|^{2} dx = 1$$

$$\int_{-\infty}^{\infty} P(x) dx = \int_{0}^{L} |\Psi|^2 dx = 1$$

- is called the normalisation condition of the wave function
- It represents the physical fact that the particle is contained inside the well and the integrated possibility to find it inside the well must be 1
- The normalisation condition will be used to determine the normalisaton constant when we solve for the wave function in the Schrodinder equation

See if you could answer this question

Can you list down the main differences between the particle-in-a-box system (infinite square well) and the Bohr's hydrogen like atom? E.g. their energies level, their quantum number, their energy gap as a function of *n*, the sign of the energies, the potential etc.

Schrodinger Equation



Schrödinger, Erwin (1887-1961), Austrian physicist and Nobel laureate. Schrödinger formulated the theory of wave mechanics, which describes the behavior of the tiny particles that make up matter in terms of waves. Schrödinger formulated the Schrödinger wave equation to describe the behavior of electrons (tiny, negatively charged particles) in atoms. For this achievement, he was awarded the 1933 Nobel Prize in physics with British physicist <u>Paul Dirac</u>

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What is the general equation that governs the evolution and behaviour of the wave function?

- Consider a particle subjected to some timeindependent but space-dependent potential *V*(*x*) within some boundaries
- The behaviour of a particle subjected to a timeindependent potential is governed by the famous (1-D, time independent, non relativistic) Schrodinger equation:

$$\frac{\hbar^2}{2m}\frac{\partial^2\psi(x)}{\partial x^2} + (E - V)\psi(x) = 0$$

How to derive the T.I.S.E

- 1) Energy must be conserved: E = K + U
- 2) Must be consistent with de Brolie hypothesis that $p = h/\lambda$
- 3) Mathematically well-behaved and sensible (e.g. finite, single valued, linear so that superposition prevails, conserved in probability etc.)
- Read the msword notes or text books for more technical details (which we will skip here)

Energy of the particle

• The kinetic energy of a particle subjected to potential V(x) is E_{K}



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- *E* is conserved if there is no net change in the total mechanical energy between the particle and the surrounding (Recall that this is just the definition of total mechanical energy)
- It is essential to relate the de Broglie wavelength to the energies of the particle:

$$\lambda = h / p = h / \sqrt{[2m(E-V)]}$$

• Note that, as $V \rightarrow 0$, the above equation reduces to the no-potential case (as we have discussed earlier) 42

 $\lambda = h / p \rightarrow h / \sqrt{[2mE]}$, where E = K only

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Infinite potential revisited

- Armed with the T.I.S.E we now revisit the particle in the infinite well
- By using appropriate boundary condition to the T.I.S.E, the solution of T.I.S.E for the wave function Ψ should reproduces the quantisation of energy level as have been deduced earlier,

i.e.
$$E_n = \frac{n^2 \pi^2 \hbar^2}{2mL^2}$$

In the next slide we will need to do some mathematics to solve for $\Psi(x)$ in the second order differential equation of TISE to recover this result. This is a more formal ψ_{ay} compared to the previous standing waves argument which is more qualitative

Why do we need to solve the Shrodinger equation?

- The potential V(x) represents the environmental influence on the particle
- Knowledge of the solution to the T.I.S.E, i.e. $\psi(x)$ allows us to obtain essential physical information of the particle (which is subjected to the influence of the external potential V(x)), e.g the probability of its existence in certain space interval, its momentum, energies etc.

Take a classical example: A particle that are subjected to a gravity field $U(x) = GMm/r^2$ is governed by the Newton equations of motion,

$$-\frac{GMm}{r^2} = m\frac{d^2r}{dt^2}$$

• Solution of this equation of motion allows us to predict, e.g. the position of the object *m* as a function of time, r = r(t), its instantaneous momentum, energies, etc.

S.E. is the quantum equivalent of the Newton's law of motion

- The equivalent of "Newton laws of motion" for quantum particles = Shroedinger equation
- Solving for the wave function in the S.E. allows us to extract all possible physical information about the particle (energy, expectation values for position, momentum, etc.)

The infinite well in the light of TISE

$$V(x) = \begin{cases} \infty, & x \le 0, x \ge L \\ 0, & 0 < x < L \end{cases}$$

Plug the potential function V(x) into the T.I.S.E

$$\frac{\hbar^2}{2m}\frac{\partial^2\psi(x)}{\partial x^2} + (E - V)\psi(x) = 0$$

Within 0 < x < L, V(x) = 0, hence the TISE becomes

$$\frac{\partial^2 \psi(x)}{\partial x^2} = -\frac{2m}{\hbar^2} E \psi(x) \equiv -B^2 \psi(x)$$

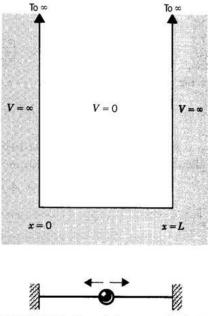


FIGURE 5.3 A particle moves freely in the one-dimensional region $0 \le x \le L$, but is excluded completely from x < 0 and x > L.

The behavior of the particle inside the box is governed by the equation

$$\frac{\partial^2 \psi(x)}{\partial x^2} = -B^2 \psi(x)$$

$$B^2 = \frac{2mE}{\hbar^2}$$

This term contain the information of the energies of the particle, which in terms governs the behaviour (manifested in terms of its mathematical solution) of $\psi(x)$ inside the well. Note that in a fixed quantum state *n*, *B* is a constant because *E* is conserved.

However, if the particle jumps to a state $n' \neq n, E$ takes on other values. In this case, *E* is not conserved because there is an net change in the total energy of the system due to interactions with external environment (e.g. the particle is excited by external photon)

If you still recall the elementary mathematics of second order differential equations, you will recognise that the solution to the above TISE is simply

$\psi(x) = A\sin Bx + C\cos Bx$

Where A, C are constants to be determined by ultilising the boundary conditions $_{47}$ pertaining to the infinite well system

You can prove that indeed

$$\psi(x) = A\sin Bx + C\cos Bx \tag{EQ 1}$$

is the solution to the TISE $\frac{\partial^2 \psi(x)}{\partial x^2} = -B^2 \psi(x)$ (EQ 2)

- I will show the steps in the following:
- Mathematically, to show that EQ 1 is a solution to EQ 2, we just need to show that when EQ1 is plugged into the LHS of EQ. 2, the resultant expression is the same as the expression to the RHS of EQ. 2.

Plug

$$\psi(x) = A \sin Bx + C \cos Bx \text{ into the LHS of EQ 2:}$$

 $\frac{\partial^2 \psi(x)}{\partial x^2} = \frac{\partial^2}{\partial x^2} [A \sin Bx + C \cos Bx]$
 $= \frac{\partial}{\partial x} [BA \cos Bx - BC \sin Bx]$
 $= -B^2 A \sin Bx - B^2 C \cos Bx$
 $= -B^2 [A \sin Bx + C \cos Bx]$
 $= -B^2 [\psi(x) = \text{RHS of EQ2}$

Proven that EQ1 is indeed the solution to EQ2

Boundary conditions

- Next, we would like to solve for the constants A, C in the solution \u03c8(x), as well as the constraint that is imposed on the constant B
- We know that the wave function forms nodes at the boundaries. Translate this boundary conditions into mathematical terms, this simply means

$$\psi(x=0)=\psi(x=L)=0$$

• First,

• Plug
$$\psi(x = 0) = 0$$
 into
 $\psi = A\sin Bx + C\cos Bx$, we obtain
 $\psi(x=0) = 0 = A\sin 0 + C\cos 0 = 0$

- i.e, C = 0
- Hence the solution is reduced to
 ψ(x) = AsinBx

• Next we apply the second boundary condition

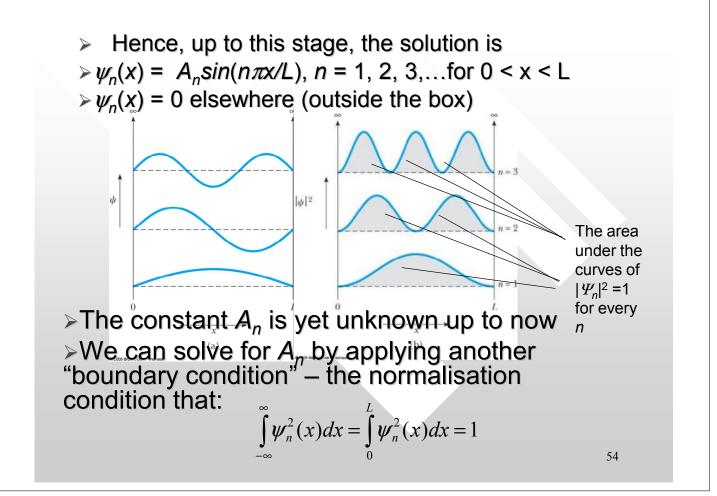
 $\psi(x=L)=0=A\sin(BL)$

- Only either A or sin(BL) must be zero but not both
- A cannot be zero else this would mean $\psi(x)$ is zero everywhere inside the box, conflicting the fact that the particle must exist inside the box
- The upshot is: A cannot be zero

- This means it must be $\sin BL = 0$, or in other words
- $B = n \pi / L \equiv B_n, n = 1, 2, 3, ...$
- *n* is used to characterise the quantum states of $\psi_n(x)$
- B is characterised by the positive integer n, hence we use B_n instead of B
- The relationship $B_n = n\pi/L$ translates into the familiar quantisation of energy condition:

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•
$$(B_n = n\pi/L)^2 \rightarrow B_n^2 = \frac{2mE_n}{\hbar^2} = \frac{n^2\pi^2}{L^2} \Longrightarrow E_n = n^2 \frac{\pi^2\hbar^2}{2mL^2}$$



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Solve for A_n with normalisation $\int_{-\infty}^{\infty} \psi_n^2(x) dx = \int_{0}^{L} \psi_n^2(x) dx = A_n^2 \int_{0}^{L} \sin^2(\frac{n\pi x}{L}) dx = \frac{A_n^2 L}{2} = 1$ thus $A_n = \sqrt{\frac{2}{L}}$

• We hence arrive at the final solution that

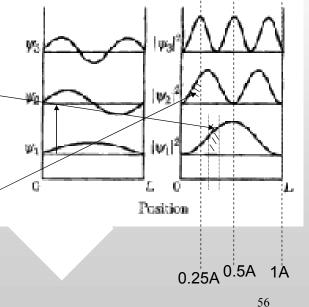
 $\gg \psi_n(x) = (2/L)^{1/2} sin(n\pi x/L), n = 1, 2, 3,...$ for 0 < x < L

 $\gg \psi_n(x) = 0$ elsewhere (i.e. outside the box)

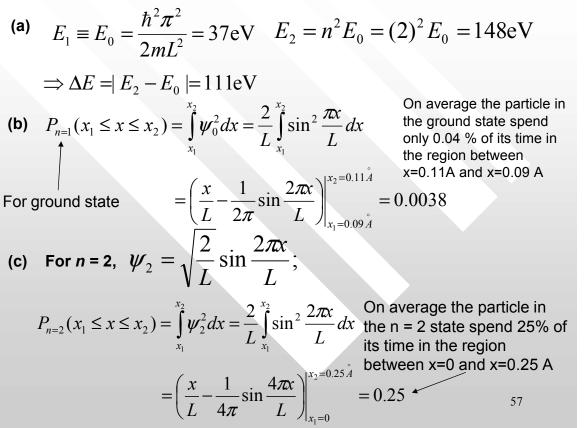
Example

- An electron is trapped in a onedimensional region of length $L = 1.0 \times 10^{-10}$ m.
- (a) How much energy must be supplied to excite the electron from the ground state to the first state?
- (b) In the ground state, what is the probability of finding the electron in the region from $x = 0.090 \times 10^{-10} \text{ m to } 0.110 \times 10^{-10} \text{ m}?$
- (c) In the first excited state, what is the probability of finding the electron between

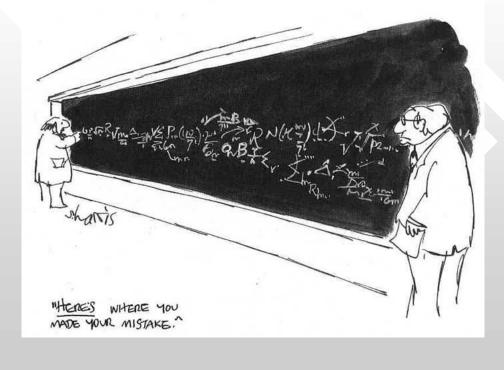
$$x = 0$$
 and $x = 0.250 \times 10^{-10}$ m?



Solutions

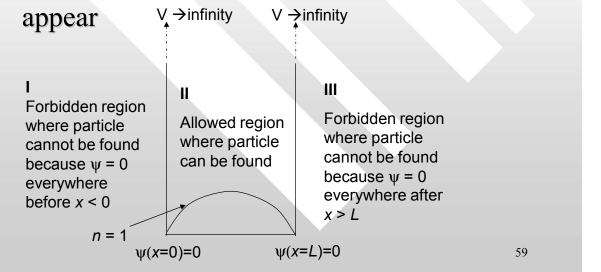


The nightmare of a lengthy calculation



Quantum tunneling

• In the infinite quantum well, there are regions where the particle is "forbidden" to

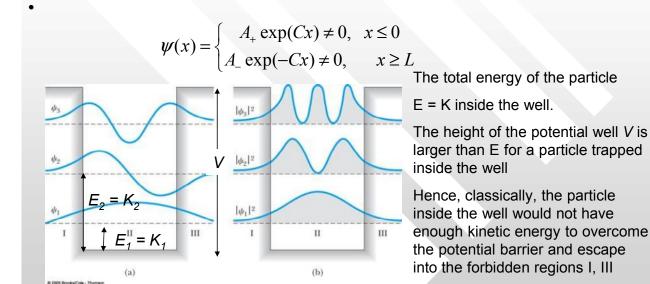


Finite quantum well

• The fact that y is 0 everywhere x $\leq 0, x \geq L$ is because of the I Π III infiniteness of the potential, $V \rightarrow \infty$ • If V has only finite height, the Usolution to the TISE will be E modified such that a non-zero value of y can exist beyond the boundaries at $\tilde{x} = 0$ and $x = \tilde{L}$ 0 L In this case, the pertaining boundaries conditions are x $\psi_{I}(x=0) = \psi_{II}(x=0), \psi_{II}(x=L) = \psi_{III}(x=L)$ $\frac{d\psi_I}{dx}\Big|_{x=0} = \frac{d\psi_{II}}{dx}\Big|_{x=0}, \frac{d\psi_{II}}{dx}\Big|_{x=0} = \frac{d\psi_{III}}{dx}\Big|_{x=0}$ 60

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- For such finite well, the wave function is not vanished at the boundaries, and may extent into the region I, III which is not allowed in the infinite potential limit
- Such ψ that penetrates beyond the classically forbidden regions diminishes very fast (exponentially) once x extents beyond x = 0 and x = L
- The mathematical solution for the wave function in the "classically forbidden" regions are



However, in QM, there is a slight chance to find the particle outside the well due to the quantum tunneling effect

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• The quantum tunnelling effect allows a confined particle within a finite potential well to penetrate through the classically impenetrable potential wall After many many Hard times of banging Hard and and the wall high high wall. wall, Е Е V V Quantum tunneling effect 62

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Why tunneling phenomena can happen

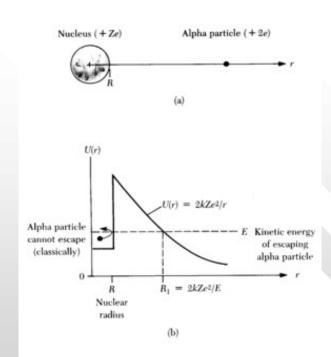
- It's due to the continuity requirement of the wave function at the boundaries when solving the T.I.S.E
- The wave function cannot just "die off" suddenly at the boundaries of a finite potential well
- The wave function can only diminishes in an exponential manner which then allow the wave function to extent slightly beyond the boundaries

$$\psi(x) = \begin{cases} A_+ \exp(Cx) \neq 0, & x \le 0\\ A_- \exp(-Cx) \neq 0, & x \ge L \end{cases}$$

- The quantum tunneling effect is a manifestation of the wave nature of particle, which is in turns governed by the T.I.S.E.
- In classical physics, particles are just particles, hence never display such tunneling effect

Quantum tunneling effect





Real example of tunneling phenomena: alpha decay

Figure 6.7 (a) Alpha decay of a radioactive nucleus. (b) The potential energy seen by an alpha particle emitted with energy E. R is the nuclear radius, about 10^{-14} m or 10 fm. Alpha particles tunneling through the potential barrier between R and R_1 escape the nucleus to be detected as radioactive decay products.

Real example of tunneling phenomena: Atomic force microscope

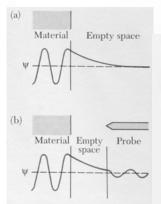


Figure 3 (a) The wavefunction of an electron in the surface of the material to be studied. The wavefunction extends beyond the surface into the empty region. (b) The sharp tip of a conducting probe is brought close to the surface. The wavefunction of a surface electron penetrates into the tip, so that the electron can "tunnel" from surface to tip.

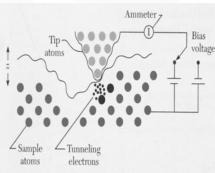


FIGURE A Highly schematic diagram of the scanning tunneling microscope process. Electrons, represented in the figure as small dots, tunnel across the gap between the atoms of the tip and sample. A feedback system that keeps the tunneling current constant causes the tip to move up and down tracing out the contours of the sample atoms.

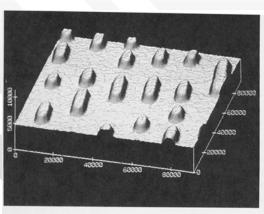


FIGURE D An atomic force microscope scan of a stamper used to mold compact disks. The numbers given are in nm. The bumps on this metallic mold stamp out 60 nm-deep holes in tracks that are 1.6 μ m apart in the optical disks. *Photo courtesy of Digital Instruments*.

TUTORIAL PROBLEM SET SESSI 2007/08 SEMESTER II

TUTORIAL 1 SPECIAL RELATIVITY (BASED ON UNDERSTANDING PHYSICS, CUMMINGS et al, John Wiley and Sons)

SEC. 38-2 ORIGINS OF SPECIAL RELATIVITY 1. Chasing Light.

What fraction of the speed of light does each of the following speeds *v* represent? That is, what is the value of the ratio v/c? (a) A typical rate of continental drift, 3 cm/y. (b) A high way speed limit of 100 km/h. (c) A supersonic plane flying at Mach 2.5 = 3100 km/h. (d) The Earth in orbit around the Sun at 30 km/s. (e) What conclusion(s) do you draw about the need for special relativity to describe and analyze most everyday phenomena? (Note: Some everyday phenomena can be derived from relativity. For example, magnetism can be described as arising from electrostatics plus special relativity applied to the slow-moving charges in wires.) ($v/c = 3.16 \times 10^{-18}$.; $v/c = 9.26 \times 10^{-8}$.; $v/c = 2.87 \times 10^{-6}$.; $v/c = 10^{-4}$.)

SEC. 38-3 . THE PRINCIPLE OF RELATIVITY 3. Examples of the Principles of Relativity

Identical experiments are carried out (1) in a high-speed train moving at constant speed along a horizontal track with the shades drawn and (2) in a closed freight container on the platform as the train passes. Copy the following list and mark with a "yes" quantities that will necessarily be the same as measured in the two frames. Mark with a "no" quantities that are not necessarily the same as measured in the two frames. (a) The time it takes for light to travel one meter in a vacuum; (b) the kinetic energy of an electron accelerated from rest through a voltage difference of one million volts; (c) the time for half the number of radioactive particles at rest to decay; (d) the mass of a proton; (e) the structure of DNA for an amoeba; (f) Newton's Second Law of Motion: F = ma; (g) the value of the downward acceleration of gravity g.

SEC. 38-4. LOCATING EVENTS WITH AN INTELLIGENT OBSERVER 6. Eruption from the Sun

You see a sudden eruption on the surface of the Sun. From solar theory you predict that the eruption emitted a pulse of particles that is moving toward the Earth at one- eighth the speed of light. How long do you have to seek shelter from the radiation that will be emitted when the particle pulse hits the Earth? Take the light-travel time from the Sun to the Earth to be 8 minutes. (56 minutes)

SEC. 38-5 LABORATORY AND ROCKET LATTICEWORKS OF CLOCKS 10. Where and When?

Two firecrackers explode at the same place in the laboratory and are separated by a time of 12 years. (a) What is the spatial distance between these two events in a rocket in which the events are separated in time by 13 years? (b) What is the relative speed of the rocket and laboratory frames? Express your answer as a fraction of the speed of light. $(4.7 \times 10^{16} \text{ meters.}; a)$ little more than one-third the speed of light)

13. Fast-Moving Muons

The half-life of stationary muons is mea sured to be 1.6 microseconds. Half of any initial number of station ary muons decays in one half-life. Cosmic rays colliding with atoms in the upper atmosphere of the Earth create muons, some of which move downward toward the Earth's surface. The mean lifetime of high-speed muons in one such burst is measured to be 16 microseconds. (a) Find the speed of these muons relative to the Earth. (b) Moving at this speed, how far will the muons move in one half-life? (c) How far would this pulse move in one half-life if there were no relativistic time stretching? (d) In the relativistic case, how far will the pulse move in 10 half-lives? (e) An initial pulse consisting of 10⁸ muons is created at a distance above the Earth's surface given in part (d). How many will remain at the Earth's surface? Assume that the pulse moves vertically downward and none are lost to collisions. (Ninety-nine percent of the Earth's atmosphere lies below 40 km altitude.)

 $\left(\frac{v}{c} = 0.995.; 4.8 \times 10^3 \text{ meters.}; 480 \text{ meters}; 48 \text{ kilom eters.}; 9.8 \times 10^4\right)$

15. Living a Thousand Years in One Year

Living a Thousand Years in One Year. You wish to make a round trip from Earth in a spaceship, traveling at constant speed in a straight line for 6 months on your watch and then returning at the same constant speed. You

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wish, further, to find Earth to be 1000 years older on your return. (a) What is the value of your constant speed with respect to Earth? (b) How much do you age during the trip? (c) Does it matter whether or not you travel in a straight line? For example, could you travel in a huge circle that loops back to Earth? (v/c = 0.9999995.; one year)

SEC 38-8 . CAUSE AND EFFECT 17. Relations between Events

The table shows the t and x coordinates of three events as observed in the laboratory frame. Laboratory Coordinates of Three Events

	t	x
Event	years	light-years
Event 1	2	1
Event 2	7	4
Event 3	5	6

On a piece of paper list vertically every pair of these events: (1,2), (1, 3), (2, 3). (a) Next to each pair write "timelike," "light-like," or "space-like" for the relationship between those two events. (b) Next to each pair, write "Yes" if it is possible for one of the events to cause the other event and "No" if a cause and effect relation between them is not possible. (For full benefit of this exercise construct and analyze your own tables.)

ANS: (1,2) timelike yes; (1,3) spacelike no; (2,3) lightlike yes

22. Proton Crosses Galaxy

Find the energy of a proton that crosses our galaxy (diameter 100 000 light-years) in one minute of its own time. $(5.27 \times 10^{10} mc^2)$

38-10 MOMENTUM AND ENERGY

23. Converting Mass to Energy

The values of the masses in the reaction $p + {}^{19}F \rightarrow \alpha + {}^{16}O$ have been determined by a mass spectrometer to have the values: m(p) = 1.00782, m(F) = 18.998405, $m(\alpha) = 4.002603u$, m(O) = 15.994915u. Here u is the atomic mass unit (Section 1.7). How much energy is released in this reaction? Express your answer in both kilograms and MeV. $(1.4467 \times 10^{-29} \text{ kilogram}; 1.3020 \times 10^{-12} \text{ joules})$

27. Powerful Proton

A proton exits an accelerator with a kinetic energy equal to N times its rest energy. Find expressions for its (a)

speed and (b) momentum.
$$\left(\frac{\lfloor N(N+2) \rfloor^{1/2}}{N+1}c.; p = \lfloor N(N+2) \rfloor^{1/2} mc.\right)$$

30. A Box of Light

Estimate the power in kilowatts used to light a city of 8 million inhabitants. If all this light generated during one hour in the evening could be captured and put in a box, how much would the mass of the box increase? (16 million kilowatts; 0.64 g)

SEC. 38-11 . THE LORENTZ TRANSFORMATION

32. Really Simultaneous?

(a) Two events occur at the same time in the laboratory frame and at the laboratory coordinates ($x_1 = 10$ km, $y_1 = 4$ km, $z_1 = 6$ km) and ($x_2 = 10$ km, $y_2 = 7$ km, $z_2 = -10$ km). Will these two events be simultaneous in a rocket frame moving with speed v= 0.8c in the x direction in the laboratory frame? Explain your answer. (b) Three events occur at the same time in the laboratory frame and at the laboratory coordinates (x_0, y_1, z_1), (x_0, y_2, z_2) and (x_0, y_1, z_3)

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where x_0 has the same value for all three events. Will these three events be simultaneous in a rocket frame moving with speed v in the laboratory x direction? Explain your answer. (c) Use your results of parts (a) and (b) to make a general statement about simultaneity of events in laboratory and rocket frames.

ANS: (a) simultaneous—in the rocket frame ($\Delta t' = 0$); (b) events are *simultaneous* in both the laboratory and rocket frames for the pair of events in part (a) and for all three pair of events in part (b);

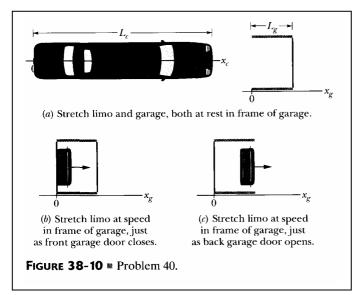
38-12 LORENTZ CONTRACTION 36. Electron Shrinks Distance

An evacuated tube at rest in the /laboratory has a length 3.00 m as measured in the laboratory. An electron moves at speed v = 0.999 987c in the laboratory along the axis of this evacuated tube. What is the length of the tube measured in the rest frame of the electron? (1.53 cm)

39. Traveling to the Galactic Center

(a) Can a person, in principle, /travel from Earth to the center of our galaxy, which is 23 000 ly distant, in one lifetime? Explain using either length contraction or time dilation arguments. (b) What constant speed with respect to the galaxy is required to make the trip in 30 y of the traveler's life time? (Yes; v/c = 0.99999915)

40. Limo in the Garage



Carman has just purchased the world's longest stretch limo, which has proper length L = 30.0 m. Part (a) of Figure 38-10 shows the limo parked at rest in front of a garage of proper length $L_g = 6.00$ m, which has front and back doors. Looking at the limo parked in front of the garage, Carman says there is no way that the limo can fit into the garage. "Au con traire!" shouts Garageman, "Under the right circumstances the limo can fit into the garage with both garage doors closed and room to spare!" Garageman envisions a fast-moving limo that takes up exactly one-third of the proper length of the garage. Part (b) of Figure 38-10 shows the speeding limo just as the front garage door closes behind it as recorded in the garage frame. Part (c) of Figure 38-10 shows the limo just as the back garage door opens in front of it as recorded in the garage frame. Find the sped of the

limo with respect to the garage required for this scenario to take place. (v = 0.99778c.)

SEC 38-13 RELETIVITY OF VELOCITIES 42. Separating Galaxies.

Galaxy A is measured to be receding from us on Earth with a speed of 0.3c. Galaxy B, located in precisely the opposite direction, is also receding from us at the same speed. What recessional velocity will an observer on galaxy A measure (a) for our galaxy, and (b) for galaxy B? (0.3c., -0/55c)

44. Transit Time

An unpowered spaceship whose rest length 350 meters has a speed 0.82c with respect to Earth. A micrometeorite, also with speed of 0.82c with respect to Earth, passes spaceship on an antiparallel track that is moving in the opposite direction. How long does it take the micrometeorite to pass spaceship as measured on the ship? $(1.2 \times 10^{-6} \text{ second.})$

TUTORIAL 2

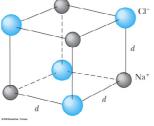
Black Body, Photoelectricity, Compton Scattering, X-rays, Pair-production/annihilation

1. The total intensity I(T) radiated from a blackbody (at all wavelengths λ) is equal to the integral over all wavelengths. $0 < \lambda < \infty$, of the Planck distribution $I(\lambda, T) = \frac{2\pi hc^2}{\lambda^5 (e^{hc/\lambda k_B T} - 1)}$. (a) By changing variables to $x = hc/\lambda kT$, show that I(T) has the

form $I(T) = \sigma T^4$, where σ is a constant independent of temperature. This result is called **Stefan's fourth-power law**, after the Austrian physicist Josef Stefan. (b) Given that $\int_0^\infty \frac{x^3 dx}{e^x - 1} = \pi^4 / 15$, show that the Stefan-Boltzmann Constant

σ is $σ = \frac{2π^5 k^4}{15h^3 c^2}$. (c) Evaluate σ numerically, and find the total power radiated from a red-hot (T = 1000 K) steel hail of radius 1 cm. (Such a ball is well approximated as a blackbody.) (Taylor, Problem 4.4, pg. 141,) **ANS: (c)** 71 W

- 2. If Planck constant were smaller than it is, would quantum phenomena be more or less conspicuous than they are now? (Beiser, Ex. 1, pg. 89)
- 3. The diameter of an atomic nucleus is about 10×10^{-15} m. Suppose you wanted to study the diffraction of photons by nuclei. What energy of photons would you choose? (Krane, Q.1, pg. 94)
- 4. Electric current is charge flowing per unit time. If we increase the kinetic energy of the electron by increasing the energy of the photons, shouldn't the current increase, because the charge flows more rapidly? Why doesn't it? (Krane, Q.6, pg. 94)
- 5. What would be the effects on a photoelectric effect if we were to double the frequency of the incident light? If we were to double the wavelength? If we were to double the intensity? (Krane, Q.7, pg. 94)
- 6. The Compton-scattering formula suggests that objects viewed from different angles should reflect light of different wavelengths. Why don't we observe a change in colour of objects as we change the viewing angle? (Krane, Q.16, pg. 95)
- 7. You have a monoenergetic source of X-rays of energy 84 keV, but for an experiment you need 70 keV X-rays. How would you convert the X-ray energy from 84 to 70 keV? (Krane, Q.16, pg. 95)
- 8. Show that a photon cannot transfer all of its energy to a free electron. (*Hint*: Note that energy and linear momentum must be conserved.) (Serway, Moses and Moyer, P27. pg. 103)
- 9. The determination of Avogadro's number with x—rays. X-rays. X-rays from a molybdenum (0.626 A) are incident on a NaCl crystal, which has the atomic arrangement shown in Figure below. If NaCl has a density of 2.17 g/cm³ and the n=1 diffraction maximum from planes separated by d is found at $\theta = 6.41^{\circ}$, compute Avogadro's number. (*Hint:* First determine d. Using Figure P3.39, determine the number of NaCl molecules per primitive cell and set the mass per unit volume of the primitive cell equal to the density. (Serway, Moses and Moyer, P39, pg./ 104)



ANS: $N_A = 6.13 \times 10^{23}$ /mole

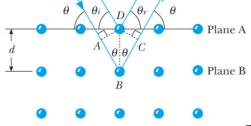
10. Two light sources are used in a photoelectric experiment to determine the work function for a particular metal surface. When green light from a mercury lamp (λ = 546.1 nm) is used, a retarding potential of 1.70 V reduces the photocurrent to zero. (a) Based on this measurement, what is the work function for this metal? (b) What

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stopping potential would be observed when using the yellow light from a helium discharge tube ($\lambda = 587.5$ nm)? (Serway, Moses and Moyer. P42, pg 104)

ANS: (a) 0.571 eV; (b) 1.54 V

11. Monochromatic X rays are incident on a crystal in the geometry of Figure below.



The first-order Bragg peak is observed when the angle of incidence is 34.0°. The crystal spacing is known to be 0.347 nm. (a) What is the wavelength of the X rays? (b) Now consider a set of crystal planes that makes an angle of 45° with the surface of the crystal (as in the Figure). For X rays of the same wavelength, find the angle of incidence measured from the surface of the crystal that produces the first-order Bragg peak. At what angle from the surface does the emerging beam appear in this case? (Krane, P3, pg 95)

- 12. The universe is filled with thermal radiation, which has a bla at an effective temperature of 2.7 K. What is the peak wavelength of this radiation? What is the energy (in eV) of a quanta at the peak wavelength? In what region of the electromagnetic spectrum is this peak wavelength? (Krane. P 20, pg 96)
- 13. Light from the sun arrives at the earth an average of 1.5×10^{11} m away, at the rate of 1.4×10^{13} W/m of area perpendicular to the direction of the light. Assume that sunlight is monochromatic with a frequency of 5×10^{14} Hz. *(a)* How many photons fall per second on each square meter of Earth's surface directly facing the sun? *(b)* What is the power output of the sun, and how many photons per second does it emit? *(c)* How many photons per cubic meter are there near the earth? (Beiser, Ex. 9, pg. 90)

ANS: (a) 4.2×10^{21} ; (b) 4.2×10^{26} Watt; 1.2×10^{45} photon per second (c) 1.4×10^{13} photon/m³

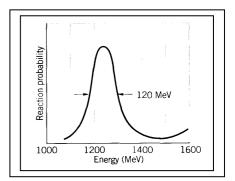
14. 1.5 mW of 400-nm light is directed at a photoelectric cell. If 0.10 percent of the incident photons produce photoelectrons, find the current in the cell. (Beiser, Ex. 15, pg. 90)

ANS: 0.48 μA

- 15. (a) Find the change in wavelength of 80-pm x-rays that are scattered 120° by a target, (b) Find the angle between the directions of the recoil electron and the incident photon. (c) Find the energy of the recoil electron. (Beiser, Ex. 34, pg. 90)
 ANS: (a) 3.64 pm (b) 29.3° (c) 674 eV
- 16. A photon of frequency v is scattered by an electron initially at rest. Verify that the maximum kinetic energy of the recoil electron is $KE_{max} = (2h^2v^2/mc^2) / (1+2hv/mc^2)$ (Beiser, Ex. 35, pg. 90)
- 17. Show that, regardless of its initial energy, a photon cannot undergo Compton scattering through an angle of more than 60° and still be able to produce an electron-positron pair. (*Hint:* Start by expressing the Compton wavelength of the electron in terms of the maximum photon wavelength needed for pair production.) (Beiser, Ex. 41, pg. 91)
- 18. (a) Verily that the minimum energy a photon must have to create an electron-positron pair in the presence of a stationary nucleus of mass *M* is 2mc²/(l + m/M), where *m* is the electron rest mass. (b) Find the minimum energy needed for pair production in the presence of a proton. (Beiser, Ex. 42, pg. 91)
 ANS: (b) 1.023 MeV
- 19. Why is it in a pair annihilation the resultant photons cannot be singly produced?

TUTORIAL 3 Wave properties of particles

- 1. Suppose we cover one slit in the two-slit experiment with a very thin sheet of fluorescent material that emits a photon of light whenever an electron passes through. We then fire electrons one at a time at the double slit; whether or not we see a flash of light tells us which slit the electron went through. What effect does this have on the interference pattern? Why? (*Suggestion: Read Chap. 1, Feynman Lectures on Physics Vol. 3*) (Krane, Q13, pg. 131,)
- 2. The speed of an electron is measured to within an uncertainty of 2.0×10^4 m/s. What is the size of the smallest region of space in which the electron can be confined? (Krane, P14, pg. 133)
- 3. A pi meson (pion) and a proton can briefly join together to form a Δ particle. A measurement of the energy of the π p system (see Figure) shows a peak at 1236 MeV, corresponding to the rest energy of the Δ particle, with an experimental spread of 120 MeV. What is the lifetime of the Δ ? (Krane, P17, pg. 133)



- 4. A proton or a neutron can sometimes "violate" conservation of energy emitting and then reabsorbing a pi meson, which has a mass of 135 MeV/ c^2 . This is possible as long as the pi meson is reabsorbed within a short enough time Δt consistent with the uncertainty principle. (a) Consider $p \rightarrow p + \pi$. By what amount ΔE is energy conservation violated? (ignore any kinetic energies.) (b) For how long a time Δt can the pi meson exist? (c) Assuming pi meson to travel at very nearly the speed of light, how far from the proton can it go? (This procedure gives us an estimate of the range of the nuclear force, because we believe that protons and neutron are held together in the nucleus by exchanging pi mesons.) (Krane, P22, pg. 133)
- 5. Show that the formula for low-energy electron diffraction (LEED), when electrons are incident perpendicular to a crystal surface, may be written as $\sin \phi = \frac{nhc}{d(2m_ec^2K)^{1/2}}$, where *n* is the order of the maximum, *d*

is the atomic spacing, m_e is the electron mass, K is the electron's kinetic energy, and ϕ is the angle between the incident and diffracted beams, (b) Calculate the atomic spacing in a crystal that has consecutive diffraction maxima at $\phi = 24.1^{\circ}$ and $\phi = 54.9^{\circ}$ for 100-eV electrons. (Serway, M & M, P 14, pg. 188) **ANS:** 33×10⁻¹⁰ m for $n=1,33\times10^{-10}$ m for n=2)

- 6. A woman on a ladder drops small pellets toward a spot on the floor, (a) Show that, according to the uncertainty principle, the miss distance must be at least $\Delta x = \left(\frac{\hbar}{2m}\right)^{1/2} \left(\frac{H}{2g}\right)^{1/4}$, where *H* is the initial height of each pellet above the floor and *m* is the mass of each pellet, (b) If H = 2.0 m and m = 0.50 g, what is Δx ? (Serway & M & M, P 21, pg. 188) **ANS: (b)** $\Delta x_{total} = 5.2 \times 10^{-16}$ m
- 7. An excited nucleus with a lifetime of 0.100 ns emits a γ ray of energy 2.00 MeV. Can the energy width (uncertainty in energy, ΔE) of this 2.00-MeV γ emission line be directly measured if the best gamma detectors can measure energies to ±5 eV? (Serway & M & M, P 25, pg. 188)

- Find the de Broglie wavelength of a 1.00-MeV proton. Is a relativistic calculation needed? (Beiser, Ex. 6, pg. 117) ANS: 2.86x10⁻¹⁴ m; No need.
- 9. Show that the de Broglie wavelength of a particle of mass *m* and kinetic energy KE is given by

$$\lambda = \frac{nc}{\sqrt{KE(KE + 2mc^2)}}$$
 (Beiser, Ex. 10, pg. 117)

- 10. What effect on the scattering angle in the Davisson-Germer experiment does increasing the electron energy have? (Beiser, Ex. 23, pg. 117)
- 11. A beam of 50-keV electrons is directed at a crystal and diffracted electrons are found at an angle of 50° relative to the original beam. What is the spacing of the atomic planes of the crystal? A relativistic calculation is needed for λ . (Beiser, Ex. 26, pg. 117) **ANS:** 3.0 pm
- 12. The lowest energy possible for a certain particle trapped in a certain box is 1.00 eV. (*a*) What are the next two higher energies the particle can have? (*b*) If the particle is an electron, how wide is the box? (Beiser, Ex. 29, pg. 118)

ANS: (a) 4 eV, 9 eV; (b) 45 fm

- 13. Discuss the prohibition of E = 0 for a particle trapped in a box L wide in terms of the uncertainty principle. How does the minimum momentum of such a particle compare with the momentum uncertainty required by the uncertainty principle if we take $\Delta x = L$? (Beiser, Ex. 30, pg. 118)
- 14. (a) How much time is needed to measure the kinetic energy of an electron whose speed is 10.0 m/s with an uncertainty of no more than 0.100 percent? How far will the electron have travelled in this period of time? (b) Make the same calculations for a 1.00-g insect whose speed is the same. What do these sets of figures indicate? (Beiser, Ex. 34, pg. 118)

ANS: (a) 1.2 ms, 1.2 cm; (b) $9.5 \ge 10^{-29} = 10^{-28} = 10^{-$

- How accurately can the position of a proton with v << c. be determined without giving it more than 1.00 keV of kinetic energy? (Beiser, Ex. 35, pg. 118). ANS: 0.144 pm
- 16. (a) Find the magnitude of the momentum of a particle in a box in its *n*th state. (b) The minimum change in the particles momentum that a measurement can cause corresponds to a change of ±1 in the quantum number *n*. If Δx = L. show that Δp Δx≥ ħ/2. (Beiser, Ex. 36, pg. 118)

ANS: (a) *nh*/2*L*; (b) *h*/2*L*;

TUTORIAL 4 Atomic models

- 1. How is the quantization of the energy in the hydrogen atom similar to the quantization of the systems discussed in the 1-D infinite quantum well? How is it different? Do the quantizations originate from similar causes? (Krane, Q8, pg. 201)
- 2. In both the Rutherford theory and the Bohr theory, we used the classical expression for the kinetic energy. Estimate the velocity of an electron in the Bohr atom and of an alpha particle in a typical scattering experiment, and decide if the use of the classical formula is justified. (Krane, Q14, pg. 201)
- 3. The lifetimes of the levels in a hydrogen atom are of the order of 10⁻⁸ s. Find the energy uncertainty of the first excited state and compare it with the energy of the state. (Krane, P29, pg. 204)
- 4. A long time ago, in a galaxy far, far away, electric charge had not yet been invented, and atoms were held together by gravitational forces. Compute the Bohr radius and the n=2 to n=1 transition energy in a gravitationally hound hydrogen atom. (Krane, P33, pg. 204)
- 5. The **fine structure constant** is defined as $\alpha = e^2/2\varepsilon_o hc$. This quantity got its name because it first appeared in a theory by the German physicist Arnold Sommerfeld that tried to explain the line structure in spectral lines (multiple lines close together instead of single lines) by assuming that elliptical as well as circular orbits are possible in the Bohr model. Sommerfeld's approach was on the wrong track, but α has nevertheless turned out to be a useful quantity in atomic physics, (*a*) Show that $\alpha = v_1/c$, where v_1 is the velocity of the electron in the ground state of the Bohr atom, (*b*) Show that the value of α is very close to 1/137 and is a pure number with no dimensions. Because the magnetic behavior of a moving charge depends on its velocity, the small value of α is representative of the relative magnitudes of the magnetic and electric aspects of electron behavior in an atom (*c*) Show that $\alpha a_0 = \lambda_c / 2\pi$, where a_0 is the radius of the ground-state Bohr orbit and λ_c is the Compton wavelength of the electron. (Beiser Ex. 9, pg. 158)
- 6. Show that the energy of the photon emitted when a hydrogen atom makes a transition from state *n* to state *n* 1 is, when n is very large, $\Delta E \cong \alpha^2 (mc^2/n^3)$ where α is the fine structure constant. (Krane, P38, pg. 205)
- Can the electron in the ground state of the hydrogen atom absorb a photon of energy (a) less than 13.6 eV and (b) greater than 13.6 eV? (c) What is the minimum photon energy that can be absorbed by the ground state of the hydrogen atom? (Serway, M & M, Q3, pg. 145)

ANS: (a) Yes (b) No (c) 10.2 eV

8. Four possible transitions for a hydrogen atom are listed here.

(A) $n_i = 2; n_f = 5$ (B) $n_i = 5; n_f = 3$ (C) $n_i = 7; n_f = 4$ (D) $n_i = 4; n_f = 7$

- (a) Which transition emits the photons having the shortest wavelength?
- (b) For which transition does the atom gain the most energy? (c) For which transition(s; does the atom lose energy? (Serway, M & M. Q11, pg. 145)

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9. An electron initially in the n = 3 state of a one-electron atom of mass M at rest undergoes a transition to the n = 1 ground state. (a) Show that tile recoil speed of the atom from emission of a photon is given approximately by v=8hR/9M. (b) Calculate the percent of the 3 → 1 transition energy that is carried off by the recoiling atom if the atom is deuterium. (Serway, M & M. Q29, pg. 148)

ANS: (b) 3.23×10^{-8} %

10. *The Auger process*. An electron in chromium makes a transition from the n = 2 state to the n = 1 state with out emitting a photon. Instead, the excess energy is transferred to an outer electron (in the n = 4 state), which is ejected by the atom. (This is called an Auger process, and the ejected electron is referred to as an Auger electron.) Use the Bohr theory to find the kinetic energy of the Auger electron. (Serway, M & M. Q28, pg. 148)

ANS: 5.385 keV

- 11. In a hot star, a multiply ionized atom with a single remaining electron produces a series of spectral lines as described by the Bohr model. The series corresponds to electronic transitions that terminate in the same final state. The longest and shortest wavelengths of the series are 63.3 nm and 22.8 nm, respectively. (*a*) What is the ion? (*b*) Find the wave lengths of the next three spectral lines nearest to the line of longest wavelength. (Serway, M & M. Q44, pg. 150) ANS: (a) O⁷⁺; (b) 41.0 nm, 33.8 nm, 30.4 nm
- Find the frequency of revolution of the electron in the classical model of the hydrogen atom. In what region of the spectrum are electromagnetic waves of this frequency? (Beiser, Ex. 4, pg. 157) ANS: 6.6×10¹⁵ Hz, ultraviolet

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- 13. What is the shortest wavelength present in the Bracken series of spectral lines? (Beiser, Ex.5, pg. 158)ANS: 1459 nm
- 14. A beam of 13.0-eV electrons is used to bombard gaseous hydrogen. What series of wavelengths will be emitted? (Beiser Ex. 16, pg. 158). **ANS:** Excited to the n = 4 level but no higher
- 15. The longest wavelength in the Lyman series is 121.5 nm and the shortest wavelength in the Balmer series is 364.6 nm. Use the figures to find the longest wavelength of light that could ionize hydrogen. (Beiser, Ex. 23, pg. 158) **ANS:** 91.13 cm
- 16. When an excited atom emits a photon, the linear momentum of the photon must be balanced by the recoil momentum of the atom. As a result, some of the excitation energy of the atom goes into the kinetic energy of its recoil. (a) Modify $E_i E_f = hv$ to include this effect, (b) Find the ratio between the recoil energy and the photon energy for the $n = 3 \rightarrow n \rightarrow 2$ transition in hydrogen, for which $E_f E_i = 1.9$ eV. Is the effect a major one? A nonrelativistic calculation is sufficient here. (Beiser, Ex. 27, pg. 158) ANS: (a)

$$E_f - E_i = h \nu \left(1 + \frac{1}{2} \left(1 + \frac{Mc^2}{h\nu} \right)^{-1} \right)$$

(b) $1.0 \ge 10^{-9}$; nonrelativistic is sufficient

TUTORIAL 5 Introductory Quantum Mechanics

1. Which of the following wave functions cannot be solutions of Schrodinger's equation for all values of x? Why not? (a) $\psi = A \sec x$; (b) $\psi = A \tan x$; (c) $\psi = A e^{x^2}$; (d) $\psi = A e^{-x^2}$ (Beiser, Ex. 3, pg. 197)

ANS: only (d) could be a solution

2. The wave function of a certain particle is $\psi = A \cos^2 x$ for $\pi/2 < x < \pi/2$. (*a*) Find the value of *A*. (*b*) Find the probability that the panicle be found between x = 0 and $x = \pi/4$ (Beiser, Ex. 5, pg. 197)

ANS: (a)
$$\sqrt{\frac{8}{3}}$$
; (b) 0.462

- The expectation value ⟨x⟩ of a particle trapped in a box a wide is a/2 (0≤x≤a), which means that its average position is the middle of the box. Find the expectation value ⟨x²⟩_n in the stationary state n. What is the behaviour of ⟨x²⟩_n as n becomes infinity. Is this consistent with classical physics? (Beiser, Ex. 17, pg. 198). ANS: a²((1/3)-(1/2)π²n²).
- 4. Find the probability that a particle in a box *L* wide can be found between x = 0 and x = L/n when it is in the *n*th state. (Beiser, Ex. 19, pg. 198)

ANS: 1/*n*.

- 5. What is the physical meaning of $\int_{-\infty}^{\infty} |\psi|^2 dx = 1 \psi dx = 1$? (Krane, Q3, pg/ 168)
- 6. What are the dimensions of $\psi(x)$? (Krane, Q4, pg. 168) ANS: \sqrt{L} .
- 7. What happens to the probability density in the infinite well when n → ∞? Is this consistent with classical physics? (Krane, Q6, pg. 168)
- 8. How would the solution to the one-dimensional infinite potential energy well be different if the potential energy were not zero for 0≤x≤L but instead had a constant value U₀. What would be the energies of the excited states? What would be the wavelengths of the standing de Broglie waves? Sketch the behavior of the lowest two wave functions. (Krane, Q6, pg. 168)
- 9. A particle in an infinite well is in the ground state with an energy of 1.26 eV. How much energy must be added to the particle to reach the second excited state (n = 3)? The third excited state (n = 4)? (Krane, P4, pg. 170)
- 10. An electron is trapped in a one-dimensional well of width 0.132 nm. The electron is in the n = 10 state. (*a*) What is the energy of the electron? (*b*) What is the uncertainty in its momentum? (*c*) What is the uncertainty in its position? How do these results change as $n \rightarrow \infty$? Is this consistent with classical behavior? (Krane, P9, pg. 170)
- 11. Consider a particle moving in a one-dimensional box with walls at x = -L/2 and x = +L/2. (a) Write the wave functions and probability densities for the states n = 1, n = 2, and n = 3. (b) Sketch the wave function and probability densities. (Hint: Make an analogy to the case of a particle in a box with walls at x = 0 and x = L) (Serway, M & M, P11, pg. 228)

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12. A particle of mass *m* is placed in a one-dimensional box of length *L*. The box is so small that the particle's motion is relativistic, so that $E = p^2/2m$ is not valid. (*a*) Derive an expression for the energy levels of the particle using the relativistic energy-momentum relation and the quantization of momentum that derives from confinement. (*b*) If the particle is an electron in a box of length $L = 1.00 \times 10^{-12}$ m, find its lowest possible kinetic energy. By what percent is the nonrelativistic formula for the energy in error? (Serway, M & M, P14, pg. 228)

ANS: (a)
$$K_n = \left[\left(\frac{nhc}{2L} \right)^2 + \left(mc^2 \right)^2 \right]^{1/2} - mc^2$$
; (b) 0.29 MeV, 29% too big

PAST YEAR TESTS, QUIZZES AND EXAM QUESTIONS (2003/04 – 2006/07)

PAST YEAR TESTS, QUIZZES AND EXAM QUESTIONS (2003/04 – 2006/07)

SESSI 03/04/TEST1

- **I(T)** Photon carries momentum
- **II(F)** The Compton shift $\Delta \lambda$ is greater for higher-energy photons
- **III(F)** The Compton shift $\Delta \lambda$ is smaller for lower-energy photons

A. I only	B. I, II	C. II, III
D. I,III	E. I,II, III	

ANS:A, Machlup, pg. 497

14. Which of the following statements correctly describe the following experiments? I(T) Photoelectricity exhibits particle nature of light

II(F) Electron diffraction exhibits wave nature of light

III (T) Compton effect exhibits particle nature of electron

IV(T) Compton effect exhibits particle nature of light

iv(i) compton ence	t exilibits particle nature	or ngin
A. II,III	B. I, II,III	C. II, III, IV

D. I,III, IV E. I,II, III,IV

ANS:D, My own questions

- 15. Which of the following statements correctly describe light?
 - **I(T)** According to Einstein, the energy in an electromagnetic beam is concentrated in discrete bundles called photon
 - II(T) According to the classical Maxwell theory of radiation, light is described as electromagnetic wave
 - **III (F)** The energy of the photon is proportional to the root-mean-square of the amplitude of the electromagnetic fields
 - IV (*) The intensity of a beam of light is proportional to the root-mean-square of the amplitude of the electromagnetic fields

A. II,III	B. I, II,IV	C. II, III, IV
D. I,III, IV	E. I,II, III,IV	

ANS:C (Free mark will be given for this question because statement IV may appear confusing and illstated).

(*) Rigorously speaking, statement IV is correct because the "root-mean-square of the amplitude" is equal to the square of the amplitude. The amplitude is a constant independent of time and space, hence whether you average its square over a complete period or simply squaring it without taking its

"average" the answer is still the same. Mathematically this is stated as $\langle E_0^2 \rangle = \frac{1}{T} \int_{0}^{T} E_0^2 dt = E_0^2$.

My own questions

16. Which of the following statements correctly describe photoelectricity?

- **I(T)** If the frequency is unchanged the number of electrons ejected depends on the incident intensity **II(F)** If the frequency is unchanged the kinetic energies of electrons ejected depends on the incident
- intensity III (T) In photoeletricity the fundamental event is the interaction of a single quantum of light with a
- **III (1)** In photoeletricity the fundamental event is the interaction of a single quantum of light with a single particle of matter

IV(T)	Electrons are	ejected imm	nediately w	hen photoe	lectricity	occurs
A. II,II	I	B. I, II,I	Π	C. II,	III, IV	

D. I,III, IV E. I,II, III,IV

ANS:D, Christman's pocket companion, pg. 302-303

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17.	 17. Which of the following statements correctly describe Compton scattering? I(T) The Compton effect has to be treated relativistically II(T) The Compton effect is significant only when the incident wavelength of the light used is comparable to the Compton wavelength of the electron 			
	III(T)	The maximum	change in wavelength	is given by $\Delta \lambda_{\text{max}} = 2\lambda_C$, where λ_C is the Compton
	IV (F)	wavelength of The Compton e		or electrons bounded to atoms than for free electrons
	A. 11,11 D. 1,111		B. I, II,III E. I,II, III,IV	С. II, III, IV
	ANS:B	, partly Christm	an's pocket companic	on, pg. 305, partly own question
18.	I(F) II(T) III(T)	The Davisson- In the Davisson interatomic spa At the quantum	•	erifies the particle nature of electromagnetic wave the wavelength of the electron is comparable to the re like waves

A. II,III	B. I, II,III	C. II, III, IV
D. I,III, IV	E. I,II, III,IV	

ANS:C, My own question

19. An increase in the voltage applied to an x-ray tube causes an increase in the x-rays'

- I(F) wavelength
- II(F) speed
- III(T) energy IV (T) frequency

A. III,IV B. I, II,III C. II, III, IV D. L,III, IV E. L,II, III,IV

ANS:A, Arthur Beiser, Modern technical physics, Q 7, pg. 801

- 20. The description of a particle in terms of matter waves is legitimate because **I(F)** It is based on common sense
 - **II(F)** The analogy with electromagnetic waves is plausible
 - **III(T)** The analogy with electromagnetic waves is p. **III(T)** theory and experiment agree

 A. III only
 B. I, II
 C. II, III

 D. I,III
 E. I,II, III

ANS:A, Arthur Beiser, Modern technical physics, Q 9, pg. 801

Data

speed of light in free space, $c = 3.00 \text{ x} 10^8 \text{ m s}^{-1}$

elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$

the Planck constant, $h = 6.63 \times 10^{-34} \text{ J s}$

unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$

rest mass of electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$

SESSI 03/04/TEST1 rest mass of proton, $m_p = 1.67 \ge 10^{-27} \text{ kg}$

SESSI 03/04/TEST2

ZCT 104/3E Modern Physics Semester Test II, Sessi 2003/04 Duration: 1 hour

Data

speed of light in free space, $c = 3.00 \times 10^8 \text{ m s}^{-1}$ elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$ the Planck constant, $h = 6.63 \times 10^{-37} \text{ Js}$ unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$ rest mass of electron, $m_c = 9.11 \times 10^{-31} \text{ kg}$ rest mass of proton, $m_m = 1.67 \times 10^{-27} \text{ kg}$

Answer all questions

1. A particle of mass m is confined to a one-dimensional box of length L. The particle's momentum is given by

D. $n\hbar/2L$

 A. h/2L
 B. nh/2L
 C. ħ/2L

 E. Non of the above
 ANS: B. Ronald and William, O10.20, pg. 92

2. The energy of the particle in Q1 is given by

A.
$$n^2 \frac{\hbar^2}{8m\pi L^2}$$
 B. $n^2 \frac{\hbar^2}{8mL^2}$ **C.** $n^2 \frac{\pi^2 \hbar^2}{2mL^2}$ **D.** $n^2 \frac{\hbar^2}{2mL^2}$

E. Non of the above ANS: B, Ronald and William, Q10.20, pg. 92

3. What is the ionisation energy of the hydrogen atom?

A. infinity	B. 0	C13.6 eV	D. 13.6 eV
E. Non of the abov	e		
ANS: D, Modern	Technical Phys	ics, Beiser, pg. 786	

4. What is the ground state energy of the hydrogen atom?

A. infinity	B. 0	C. -13.6 eV	D. 13.6 eV
E. Non of the above	/e		
ANS: C, Modern	Technical Phys	ics, Beiser, pg. 786	

5. An electron collides with a hydrogen atom in its ground state and excites it to a state of n = 3. How much energy was given to the hydrogen atom in this collision?

 A. -12.1 eV
 B. 12.1 eV
 C. -13.6 eV
 D. 13.6 eV

 E. Non of the above
 ANS: B, Modern Technical Physics, Beiser, Example 25.6, pg. 786

6. Which of the following transitions in a hydrogen atom emits the photon of lowest frequency?

A. n = 3 to n = 4**B.** n = 2 to n = 1**C.** n = 8 to n = 2**D.** n = 6 to n = 2**E.** Non of the above **ANS: D, Modern Technical Physics, Beiser, Q40, pg. 802, modified**

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7. In Bohr's model for hydrogen-like atoms, an electron (mass *m*) revolves in a circle around a nucleus with positive charges *Ze*. How is the electron's velocity related to the radius *r* of its orbit?

A.
$$v = \frac{1}{4\pi\varepsilon_0} \frac{Ze^2}{mr}$$
 B. $v = \frac{1}{4\pi\varepsilon_0} \frac{Ze^2}{mr^2}$ **C.** $v = \frac{1}{4\pi\varepsilon_0} \frac{Ze}{mr^2}$ **D.** $v^2 = \frac{1}{4\pi\varepsilon_0} \frac{Ze^2}{mr}$

ANS: D, Schaum's series 3000 solved problems, Q39.13, pg 722 modified

8. How is the total energy of the electron in Question 7 related the radius of its orbit?

A.
$$E = \frac{1}{4\pi\varepsilon_0} \frac{Ze^2}{2r}$$

B. $E = \frac{1}{4\pi\varepsilon_0} \frac{Ze}{2r}$
C. $E = -\frac{1}{4\pi\varepsilon_0} \frac{Ze}{2r}$
D. $E = -\frac{1}{4\pi\varepsilon_0} \frac{Ze^2}{2r}$

E. Non of the above ANS: D, Schaum's 3000 solved problems, Q39.14, pg. 722

9. The quantum number n of the lowest energy state of a hydrogen atom

A. is 0B. is 1C. depends on the orbit sizeD. depends on the electron speedE. Non of the aboveANS: B, Modern Technical Physics, Beiser, Q23, pg. 802

10. The electron of a ground state hydrogen atom

A. has left the atom
highest energyB. is at rest
E. Non of the aboveC. is in its orbit of lowest energy
E. Non of the aboveD. is in its orbit of
t of highest energyANS: C, Modern Technical Physics, Beiser, Q16, pg. 801

11. A proton and an electron, far apart and at rest initially, combine to form a hydrogen atom in the ground state, A single photon is emitted in this process. What is its wavelength?

A. 13.6 nm B. 20 nm C. 91 nm D. infinity E. Non of the above ANS: C, Modern Technical Physics, Beiser, Q30, pg. 804

12. The wave function of a particle trapped in an infinite quantum well of width L is given by

$$\psi_n = A_n \sin \frac{n\pi x}{L}$$
. Determine the normalisation constant A_n .
A. $\sqrt{\frac{L}{2}}$ B. $\frac{2}{L}$ C. $\sqrt{\frac{2n}{L}}$ D. $\sqrt{\frac{2}{L}}$ E. Non of the above
ANS: D, my own question

13. Where does the particle in Question 12 spend most of its time while in the ground state? **A.** around x = 0 **B.** around x = L **C.** around x = L/2 **D.** around x = L/4 **E.** Non of the above **ANS:C. My own question**

SESSI 03/04/TEST2

14. How many different photons can be emitted by hydrogen atoms that undergoes transitions to the ground states from the n = 5 states?

A. 3 B. 6 C. 10 D. 15 E. Non of the above ANS: C, Ronald and William, Q11.8, pg. 109

- 15. Which of the following statements are true about an electron trapped on the *x*-axis by infinite potential energy barriers at x = 0 and x = L?
 - I(T) Inside the trap the coordinate-dependent part of the wave function ψ satisfy the Schrödinger equation
 - **II(T)** ψ obeys the boundary conditions $\psi(0) = 0$ and $\psi(L) = 0$
 - III (F) The probability to locate the electron is everywhere the same inside the well

IV(T) Outside the trap, $\psi = 0$

A. II,III B. I, II,III C. II, III, IV D. I, II, IV only E. Non of the above

ANS:D, Christman's pocket companion, Item 40.3, pg. 312

16. Which of the following statements are true?

I(T)	The energy of a particle trapped inside	e an finite quantum well is quantised		
II(T)	The energy of a particle trapped inside an infinite quantum well is quantised			
III (F) The lowest energy of a particle trapped in an infinite quantum well is zero				
A. II,I	II B. I, II,III	C. II, III		
D. I, II	E. Non of the above			
ANS:D my own question				

17. Which of the following statement(s) is (are) true?

- I(T) The plum pudding model cannot explains the backscattering of alpha particles from thin gold foils
- **II(T)** Rutherford model assumes that an atom consists of a tiny but positively charged nucleus surrounded by electrons at a relatively large distance
- **III(T)** In the Bohr model, an electron in a stationary state emits no radiation
- IV(T) In the Bohr model, electrons bound in an atom can only occupy orbits for which the angular momentum is quantised

A. III,IV	B. I, II.III	C. I, II, III.IV	D. I,II
E. Non of the ab	ove		
ANS:C,Giancoli	, Summery on pg 972		

18. Which of the following statement(s) is (are) true?

- I(F) Bohr's theory worked well for one electron ions as well as for multi-electron atoms
- **II(F)** Bohr's model is plagued by the infrared catastrophe
- **III(F)** In the Bohr model, n = 1 corresponds to the first excited state
 - IV(T) Rutherford model cannot explain the stability of atomic orbit

A. III,IV	B. I, II.III	C. I, II, III.IV	D. I,II
E. Non of the ab	ove		
ANS:E, My owr	question		

19. Which of the following statements are correct?

I(F) Balmer series corresponds to the spectral lines emitted when the electron in a hydrogen atom makes transitions from higher states to the n = 1 state

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- **II(F)** Lyman series corresponds to the spectral lines emitted when the electron in a hydrogen atom makes transitions from higher states to the n = 2 state
- **II(T)** Paschen series corresponds to the spectral lines emitted when the electron in a hydrogen atom makes transitions from higher states to the n = 3 state

A. II,III B. I, II,III C. II, III D. III only E. Non of the above ANS:D, My own questions

20. Which of the following statements are correct?

- I(T) Frank-Hertz experiment shows that atoms are excited to discrete energy levels
- II(T) Frank-Hertz experimental result is consistent with the results suggested by the line spectra
- III (T) The predictions of the quantum theory for the behaviour of any physical system must correspond to the prediction of classical physics in the limit in which the quantum number specifying the state of the system becomes very large
- IV(T) The structure of atoms can be probed by using electromagnetic radiation

A. II,III B. I, II,IV C. II, III, IV

D. I,II, III, IV E. Non of the above

ANS:D, My own questions

SESSI 03/04/FINAL

UNIVERSITI SAINS MALAYSIA

Second Semester Examination Academic Session 2003/2004

February/March 2004

ZCT 104E/3 - Physics IV (Modern Physics) [Fizik IV (Fizik Moden)]

Duration: 3 hours [Masa: 3 jam]

Please check that the examination paper consists of **SIXTEEN** pages of printed material before you begin the examination.

[Sila pastikan bahawa kertas peperiksaan ini mengandungi ENAM BELAS muka surat yang bercetak sebelum anda memulakan peperiksaan ini.]

<u>Instruction</u>: Answer any **FOUR (4)** questions. Students are allowed to answer all questions in Bahasa Malaysia or in English.

[<u>Arahan</u>: Jawab mana-mana **EMPAT** soalan. Pelajar dibenarkan menjawab semua soalan sama ada dalam Bahasa Malaysia atau Bahasa Inggeris.]

- 2 -

Data

speed of light in free space, $c = 3.00 \text{ x} 10^8 \text{ m s}^{-1}$

permeability of free space, $\mu_0 = 4\pi \text{ x } 10^{-7} \text{ H m}^{-1}$

permittivity of free space, $\varepsilon_0 = 8.85 \text{ x } 10^{-12} \text{ F m}^{-1}$

elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$

the Planck constant, $h = 6.63 \times 10^{-34} \text{ J s}$

unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$

rest mass of electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$

rest mass of proton, $m_{\rm p} = 1.67 \text{ x } 10^{-27} \text{ kg}$

molar gas constant, = 8.31 J K⁻¹ mol⁻¹

the Avogadro constant, $N_{\rm A} = 6.02 \text{ x } 10^{23} \text{ mol}^{-1}$

gravitational constant, $G = 6.67 \times 10-11 \text{ N m}^2 \text{ kg}^{-2}$

acceleration of free fall, $g = 9.81 \text{ m s}^{-2}$

[ZCT 104E]

Question 1. (25 marks)

1.1 A spaceship of proper length L_p takes t seconds to pass an Earth observer. What is its speed as measured by the Earth observer according to classical physics? [Sebuah kapal angkasa yang panjang proper-nya L_p mengambil masa t untuk bergerak melalui seorang pemerhati di Bumi. Mengikut fizik klasik, apakah kelajuannya yang terukur oleh pemerhati di Bumi itu?]

- 3 -

A.
$$L_p/t$$
 B. $\frac{cL_p/t}{\sqrt{c^2 + (L_p/t)^2}}$ **C.** c **D.** L_p

E. Non of the above [Tiada dalam pilihan di atas]

ANS: A, Serway solution manual 2, Q9A, pg. 336

1.2 In Question 1, what is its speed as measured by the Earth observer according to special relativity? [Dalam soalan 1, apakah kelajuan yang terukur oleh pemerhati di Bumi mengikut teori kerelatifan khas?]

A.
$$L_p/t$$
 B. $\frac{cL_p/t}{\sqrt{c^2 + (L_p/t)^2}}$ **C.** c **D.** L_p

E. Non of the above [*Tiada dalam pilihan di atas*]

ANS: B, Serway solution manual 2, Q9A, pg. 336

1.3 What is the momentum of a proton if its total energy is twice its rest energy? [Apakah momentum bagi suatu proton jika jumlah tenaganya adalah dua kali tenaga rehatnya?]

A. 1620 Ns **B.** 1 MeV/*c* **C.** 938 MeV/*c* **D.** 2 MeV/*c*

E. 1620 MeV/c

ANS: E, Serway solution manual 2, Q21, pg. 339

1.4 The power output of the Sun is 3.8×10²⁶ W. How much rest mass is converted to kinetic energy in the Sun each second?
 [Output kuasa Matahari ialah 3.8×10²⁶ W. Berapakah jisim rehat yang ditukarkan kepada tenaga kinetik setiap saat di dalam Matahari?]

A. 4.2×10^9 kg **B.** 1.3×10^{17} kg **C.** 3.6×10^8 kg

....3/-

[ZCT 104E]

D. 6.6×10^{10} kg **E.** 4.2×10^8 kg

ANS: A, Serway solution manual 2, Q37, pg. 340

What is the value of hc/e in unit of $nm \cdot eV$ 1.5 [Apakah nilai hc/e dalam unit $nm \cdot eV$?]

> A. 1.240 **B.** 1240×10^{-6} **C.** 1240 **D.** 1240×10^{-9}

E. 1240×10^{-3}

ANS: C, my own question [note: typo: the quantity should read hc instead of hc/e]

By what factor is the mass of an electron accelerated to the speed of 0.999*c* larger 1.6 than its rest mass? [Berapa besarnya factor jisim satu elektron yang dipecutkan kepada kelajuan 0.999c berbanding dengan jisim rehatnya?]

A. 31.6 **B.** 0.03 **C.** 0.04 **D.** 22.3 **E.** 1.0

ANS: D, my own question

- The rest mass of a photon 1.7 [Jisim rehat foton]
 - A. is zero
 - [ialah sifar] **B**. is the same as that of an electron [sama dengan jisim elektron] C. depends on its frequency [bergantung kepada frekuensinva] **D.** depends on its energy [bergantung kepada tenaganya] E. Non of the above [Tiada dalam pilihan di atas]

ANS: A, Modern physical technique, Beiser, MCP 6, pg. 801

- Determine the vacuum wavelength corresponding to a γ -ray energy of 10^{19} eV 1.8 [Tentukan jarak gelombang vakum bagi sinar γ yang bersepadanan dengan tenaga 10¹⁹ eV]
 - **A.** 1.24×10^{-9} pm
 - **B.** 1.24×10^{-16} pm

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- C. 1.24×10^{-25} nm **D.** 1.24×10^{-16} nm
- E. 1.24×10^{-25} nm

ANS: D, Schaum's 3000 solved problems, O38.3, pg. 708

- To produce an x-ray quantum energy of 10⁻¹⁵ J electrons must be accelerated 19 through a potential difference of about [Untuk menghasilkan sinar-x dengan tenaga kuantum 10⁻¹⁵ J suatu elektron mesti dipecutkan melalui satu beza keupayaan yang nilainya lebih kurang l
 - A. 4 kV
 - **B.** 6 kV
 - **C.** 8 kV
 - **D.** 9 kV E. 10 kV

ANS: B, OCR ADVANCED SUBSIDIARY GCE PHYSICS B (PDF), Q10, pg. 36

Ouestion 1.10–1.12 [Soalan 1.10-1.12]

- **A.** 10⁻⁴ m **B.** 10⁻⁷ m **C.** 10^{-10} m **D.** 10⁻¹² m **E.** 10⁻¹⁵ m
- 1.10 Which of the values in the list above is the best estimate of the radius of an atom? [Nilai yang manakah dalam senarai di atas memberikan anggaran yang paling baik untuk radius satu atom?]

ANS: C, OCR ADVANCED PHYSICS B (PDF), Q1, pg. 74

1.11 Which of the values in the list above is the best estimate of the wavelength of visible light? [Nilai yang manakan dalam senarai di atas memberikan anggaran yang paling baik untuk jarak gelombang cahaya ternampak?]

ANS: B, OCR ADVANCED PHYSICS B (PDF), Q1, pg. 74

1.12 Which of the values in the list above is the best estimate of the wavelength of a 1.5 MeV electron?

[Nilai yang manakan dalam senarai di atas memberikan anggaran yang paling baik untuk jarak gelombang bagi elektron 1.5 MeV?]

ANS: D, OCR ADVANCED PHYSICS B (PDF), Q1, pg. 74

1.13 What is the momentum of a single photon of red light ($\nu = 400 \times 10^{12}$ Hz) moving through free space?

[Apakah momentum foton cahaya merah ($v = 400 \times 10^{12}$ Hz) yang bergerak melalui ruang bebas?]

A. 8.8×10⁻²⁷ kg m/s **B**. 6 keV **C**. 1240 eV/c **D**. 1.65 eV/c **E**. 2.4 eV/c

ANS: D, Schaum's 3000 solved problems, Q8.12, pg. 709

1.14 What potential difference must be applied to stop the fastest photoelectrons emitted by a nickel surface under the action of ultraviolet light of wavelength 2000 Å? The work function of nickel is 5.00 eV.

[Apakah beza keupayaan yang mesti dikenakan untuk menghentikan fotoelektron paling pantas yang dipancarkan dari permukaan nikel di bawah tindakan cahaya ultraungu yang jarak gelombangnya 2000 Å? Fungsi kerja nikel ialah 5.00 eV.]

A. 1.0 kV **B**. 1.2 kV **C**. 2.0 V **D**. 1.0 V **E**. 1.2 V

ANS: E, Schaum's 3000 solved problems, Q38.18, pg. 710

- 1.15 Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I. The assumption of the Ether frame is inconsistent with the experimental observation

[Tanggapan rangka Ether adalah tidak konsisten dengan pemerhatian eksperimen]

- II. The speed of light is constant [Kelajuan cahaya adalah malar]
- III. Maxwell theory of electromagnetic radiation is inconsistent with the notion of the Ether frame [Teori sinaran keelektromagnetan Maxwell adalah tidak konsisten dengan tanggapan rangka Ether]

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IV Special relativity is inconsistent with the notion of the Ether frame *[Kerelatifan Khas adalah tidak konsistent dengan tanggapan rangka Ether]*

A. III,IV **B.** I, II, III **C.** I, II, III,IV

D. I, II **E.** I, II,IV

ANS: E, my own question

- 1.16 Which of the following statements are true about light? [Yang manakah kenyataan berikut adalah benar berkenaan dengan cahaya?]
 - I. It propagates at the speed of $c = 3 \times 10^8$ m/s in all medium [Cahaya tersebar pada kelajuan $c = 3 \times 10^8$ m/s dalam semua jenis medium]
 - II. It's an electromagnetic wave according to the Maxwell theory [Cahaya ialah gelombang elektromagnetik mengikut teori Maxwell]
 - **III.** It's a photon according to Einstein [Cahaya ialah foton menurut Einstein]
 - **IV.** It always manifests both characteristics of wave and particle simultaneously in a given experiment [Cahaya sentiasa memperlihatkan kedua-dua ciri gelombang dan kezarahan secara serentak dalam sesuatu eksperimen]
 - **A.** I,IV **B.** II, III,IV **C.** I, II, III,IV
 - **D.** I, II **E.** II,III

ANS: E, my own question

- 1.17 Which of the following statements are true about Lorentz transformation? [Yang manakah kenyataan berikut adalah benar berkenaan dengan transformasi Lorentz?]
 - I. It relates the space-time coordinates of one inertial frame to the other [*Ia menghubung-kaitkan koordinat-koordinat ruang-masa suatu rangka inersia dengan koordinat-koordinat ruang-masa rangka inersia lain*]
 - II. It is the generalisation of Galilean transformation [*Ia merupakan generalisasi transformasi Galilean*]
 - III. It constitutes one of the Einstein's special relativity postulates

[Ia merupakan salah satu postulat teori kerelatifan khas Einstein]

- IV. Its derivation is based on the constancy of the speed of light postulate [Ia diterbitkan berdasarkan postulat kemalaran kelajuan cahaya]
- **A.** I,IV **B.** I,II, IV **C.** I, II, III,IV
- D. I, II E. II,III
- ANS: B, my own question
- 1.18 The expression of linear momentum has to be modified in the relativistic limit in order to

[Ekspresi momentum linear kena dimodifikasikan pada limit relativistik supaya]

- I. preserve the consistency between the Lorentz transformation and conservation of linear momentum *[konsistensi antara transformasi Lorentz dengan keabadian momentum linear terpelihara]*
- **II.** preserve the consistency between the Galilean transformation and conservation of linear momentum *[konsistensi antara transformasi Galilean dengan keabadian momentum linear terpelihara]*
- III. preserve the consistency between special relativity with Newtonian mechanics [konsistensi antara kerelatifan khas dengan mekanik Newton terpelihara]
- IV. preserve the consistency between the Lorentz transformation and Galilean transformation [konsistensi antara transformasi Lorentz dengan transformasi Galilean terpelihara]
- A. I only B. I,II, IV C. I, III,IV D. III,IV E. IV only

ANS: A, my own question

Question 2. (25 marks) [Soalan 2 (25 markah)]

2.1 What is the kinetic energy of the fastest photoelectrons emitted by a copper surface, of work function 4.4 eV when illuminated by visible light 0f 700 nm? [Apakah tenaga kinetik fotoelektron paling pantas yang dipancarkan oleh permukaan kuprum, yang fungsi kerjanya 4.4 eV, semasa disinari cahaya

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ternampak 700 nm?]

A. 1.17 eV
B. 6.17 eV
C. 1.17 eV
D. 1.0 eV
E. non of the above [*Tiada dalam pilihan di atas*]

ANS: E, Schaum's 3000 solved problems, Q38.21, pg. 710

2.2 Suppose that a beam of 0.2-MeV photon is scattered by the electrons in a carbon target. What is the wavelength of those photon scattered through an angle of 90°? [Katakan satu bim foton 0.2 MeV diserakkan oleh elektron di dalam sasaran karbon. Apakah jarak gelombang bagi foton yang diserakkan melalui satu sudut 90°?]

A. 0.00620 nm B. 0.00863 nm C. 0.01106 nm D. 0.00243 nm E. non of the above *[Tiada dalam pilihan di atas]* ANS: B, Schaum's 3000 solved problems, Q38.31, pg. 712

2.3 Determine the cut-off wavelength of x-rays produced by 50-keV electrons in a x-ray vacuum tube? [Tentukan jarak gelombang penggal bagi sinar-x yang dihasilkan oleh elektron 50 keV dalam satu tiub sinar-x vakum.]

A. 0.000248 Å
B. 2.48 Å
C. 248 Å
D. 0.248 Å
E. non of the above [*Tiada dalam pilihan di atas]*

ANS: D, Schaum's 3000 solved problems, Q38.39, pg. 714

A lamp emits light of frequency 5.0×10¹⁵ Hz at a power of 25 W. The number of photons given off per seconds is
 [Suatu lampu memancarkan cahaya berfrekuensi 5.0×10¹⁵ Hz pada kuasa 25 W. Bilangan foton yang dihasilkan per saat ialah]

A. 1.3×10^{-19} **B.** 8.3×10^{-17} **C.** 7.5×10^{18} **D.** 1.9×10^{50}

E. 2.9×10^{13} ANS:C , Modern physical technique, Beiser, MCP 34, pg. 802, modified

- 2.5 Which of the following transitions in a hydrogen atom emits the photon of lowest frequency? [Dalam senarai di bawah, peralihan yang manakah memancarkan foton frekuensi terendah di dalam atom hidrogen?]
 - A. n = 1 to n = 2 B. n = 2 to n = 1 C. n = 2 to n = 6

 D. n = 6 to n = 2 E. n = infinitely large to n = 1 [n = sebesar tak terhingga ke n = 1]

ANS:D, Modern physical technique, Beiser, MCP 40, pg. 802

- 2.6 The speed of an electron whose de Broglie wavelength is 1.0×10^{-10} m is [Kelajuan satu elektron yang jarak gelombang de Broglie-nya 1.0×10^{-10} m ialah
-]

A. 6.6×10^{-24} m/s **B.** 3.8×10^3 m/s **C.** 7.3×10^6 m/s

D. 1.0×10^{10} m/s **E.** 6.6×10^2 m/s ANS:C, Modern physical technique, Beiser, MCP 36, pg. 802

2.7 A large value of the probability density of an atomic electron at a certain place and time signifies that the electron

[Nilai yang besar bagi ketumpatan kebarangkalian suatu elektron atom pada sesuatu tempat dan masa menunjukkan elektron itu]

- A. is likely to be found there [agak mungkin dijumpai di sana]
- **B.** is certain to be found there *[pasti dijumpai di sana]*
- C. has a great deal of energy there [mempunyai banyak tenaga di sana]
- **D.** has a great deal of charge *[mempunyai banyak cas]*
- **E.** is unlikely to be found there

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[tidak berapa mungkin dijumpai di sana]

ANS:A, Modern physical technique, Beiser, MCP 25, pg. 802

- 2.8 Ionisation energy of hydrogen is 13.5 eV. What is the shortest wavelength in the Lyman series of hydrogen atom? [Tenaga pengionan hidrogen ialah 13.5 eV. Apakah jarak gelombang terpendek dalam siri Lyman hidrogen?]
 - **A.** 364 nm **B.** 121 nm **C.** 91 nm **D.** 819 nm

E. 103 nm ANS:C, my own question

2.9 If the momentum of a particle is doubled, its wavelength is multiplied ______ times [Jika momentum suatu zarah digandakan dua, jarak gelombangnya digandakan ______kali]

A. 1 B. 2 C. 1/2 D. 8 E. 0

ANS: C, Machlup, Review question 7, pg. 522, modified

- 2.10 A standing wave cannot have less than _____ antinode. In quantum mechanics, that fundamental mode would be called the ______. [Suatu gelombang pegun tidak boleh mempuyai kurang daripada ______antinod. Dalam mekanik kuantum, mod asas ini dinamakan ______.]
 - A. 1, first excited state [keadaan teruja pertama] [keadaan dasar]
 - C. 2, first excited state [keadaan teruja pertama] [keadaan dasar]
 - E. 0, ground state [keadaan dasar]
 ANS: B, Machlup, Review question 9, pg. 522, modified
- 2.11 Assume that the uncertainty in the position of a particle is equal to its de Broglie wavelength. What is the minimal uncertainty in its velocity, v_x ? [Anggapkan bahawa ketidakpastian dalam kedudukan suatu zarah adalah sama dengan jarak gelombang de Broglie-nya. Apakah ketidakpastian minimum dalam halajunya v_x ?]

A. $v_x/4\pi$ **B.** $v_x/2\pi$ **C.** $v_x/8\pi$ **D.** v_x

E. v_x/π

ANS: A, Schaum's 3000 solved problems, Q38.66, pg. 718

2.12 If the ionisation energy for a hydrogen atom is 13.6 eV, what is the energy of the level with quantum number n = 3?[Jika tenaga pengionan satu atom hidrogen ialah 13.6 eV, apakah tenaga untuk paras yang bernombor kuantum n = 3?]

A. 1.51 eV	B. 3.4 eV	C. 12.1 eV
D. -1.51 eV	E. -3.4 eV	

ANS: D, Schaum's 3000 solved problems, Q39.6, pg. 720

- 2.13 What is the zero-point energy of an electron trapped in an infinite potential well
 - of size L = 0.5 Å

[Apakah tenaga titik-sifar bagi elektron yang terperangkap di dalam suatu telaga

keupayaan infinit yang saiznya L = 0.5 A]

A. 7.5×10^{-9} eV **B.** 11.7×10^{-6} eV **C.** 0.30×10^{-6} eV

D. 13.6 eV **E.** 65×10^{-6} eV

ANS: 150 eV. Free marks will be given for this question since there is no correct answer in the options.

- 2.14 A moving body is described by the wave function ψ at a certain time and place; ψ^2 is proportional to the body's [Suatu jasad bergerak diperihalkan oleh fungsi gelombang ψ pada suatu masa dan tempat tertentu; ψ^2 adalah berkadar dengan]
 - A. electric field [medan elektrik]
 B. speed [kelajuan]
 C. energy [tenaga]
 D. probability of being found [kebarangkalian untuk dijumpai]
 E. mass [jisim]

ANS:D, Modern physical technique, Beiser, MCP 11, pg. 801

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2.16

2.15 The continuous x-ray spectrum produced in an x-ray tube can be explained by [Keselanjaran spektrum sinar-x yang dihasilkan dalam suatu tiub sinar-x dapat diterangkan oleh]

	-		
І. П. Ш. IV.	Classical Electroma [Teori klasik gelomi Pair production [Penghalisan pasan Bremsstrahlung [Bremsstrahlung] Diffraction [Belauan]	bang keelektroma	•
A. I,IV	B. I,II, IV	C. I, III,IV	D. I, III
E. II,III ANS: D, Planck consta [Pemalar Pla			
I.	is a universal const	ant	
II.	<i>[ialah satu pemalar</i> is the same for all r		
ш	[adalah sama bagi : is different for diffe		1]
	[adalah tidak sama	bagi logam yang	berlainan]
IV.	characterises the qu [mencirikan skala k		
A. I,IV	B. I,II, IV	C. I, III,IV	D. I, III
E. 11,111			

ANS: B, Machlup, Review question 8, pg. 496, modified

- 2.17 A neon sign produces [Suatu lampu neon menghasilkan]
 - I. a line spectrum [suatu spektrum garis]
 II. an emission spectrum [suatu spektrum pancaran]
 III. an absorption spectrum [suatu spektrum penyerapan]
 IV. photons [foton]

A. I,IV **B.** I,II, IV **C.** I, III,IV **D.** I, III

E. II,III

ANS:B, Modern physical technique, Beiser, MCP 20, pg. 801, modified

- 2.18 Which of the following statements are true? [Kenyataan berikut yang manakah benar?]
 - I.. the ground states are states with lowest energy [keadaan asas adalah keadaan dengan tenaga yang paling rendah]
 - II. ionisation energy is the energy required to raise an electron from ground state to free state [tenaga pengionan adalah tenaga yang diperlukan untuk menaikan suatu elektron dari keadaan asas ke keadaan bebas]
 - **III**. Balmer series is the lines in the spectrum of atomic hydrogen that corresponds to the transitions to the n = 1 state from higher energy states [Balmer siri adalah garis-garis spectrum atom hidrogen yang bersepadanan dengan peralihan dari paras-paras tenaga yang lebih tinggi ke paras n = 1]

A. I,IV **B.** I,II, IV **C.** I, III,IV **D.** I, II

E. II,III

ANS: D, My own question (note: this is an obvious typo error with the statement IV missing. In any case, only statement I, II are true.)

Question 3. (25 marks)

[Soalan 3. (25 markah)]

(a) Lithium, beryllium and mercury have work functions of 2.3 eV, 3.9 eV and 4.5 eV, respectively. If a 400-nm light is incident on each of these metals, determine

[Fungsi kerja Lithium, beryllium dan raksa adalah 2.3 eV, 3.9 eV dan 4.5 eV masing-masing. Jika cahaya 400 nm ditujukan ke atas setiap satu logam itu, tentukan]

- (i) which metals exhibit the photoelectric effect, and [logam yang manakah memperlihatkan kesan fotoelectrik, dan]
- (ii) the maximum kinetic energy for the photoelectron in each case (in eV)

[tenaga kinetik maksimum untuk fotoelektron dalam setiap kes itu (dalam unit eV)]

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	Serway solution manual 2, Q21, pg. 357
(b)	Molybdenum has a work function of 4.2 eV.

- [Fungsi kerja Molybdenum ialah 4.2 eV.]
 - (i) Find the cut-off wavelength (in nm) and threshold frequency for the photoelectric effect. [Carikan jarak gelombang penggal (dalam unit nm) dan frekuensi ambang untuk kesan fotoelektrik]
 - (ii) Calculate the stopping potential if the incident radiation has a wavelength of 180 nm.
 [Hitungkan keupayaan penghenti jika sinaran tuju mempunyai jarak gelombang 180 nm.]

Serway solution manual 2, Q16, pg. 356

(c) A 0.0016-nm photon scatters from a free electron. For what scattering angle of the photon do the recoiling electron and the scattered photon have the same kinetic energy? [Suatu foton 0.0016 nm diserakkan oleh elektron bebas. Apakah sudut serakan foton supaya elektron yang tersentak dan foton yand terserak itu mempunyai tenaga kinetik yang sama?]

Serway solution manual 2, Q35, pg. 358

Solution:

Q3a(i) The energy of a 400 nm photon is $E = hc/\lambda = 3.11 \text{ eV}$ [2 mark]

The effect will occur only in lithium* [2 marks, with or without explanation]

Q3a(ii)

For lithium, $K_{max} = h_V - W_0 = 3.11 \text{ eV} - 2.30 \text{ eV} = 0.81 \text{ eV}^*$ [3 marks]

[Note*: for Q3a(i,ii), the full 2+2+3 marks only for the unique answer set {lithium, $K_{max} = 0.81 \text{ eV}$ }. Minus 2 marks for any extra answer set involving other metals]

Q3b(i)

Cut-off frequency = $\lambda_{cutoff} = hc/W_0$ = 1240 nm eV / 4.2 eV = **295 nm** Cut-off frequency (or threshold frequency)= $v_{cutoff} = c/\lambda = 1.01 \times 10^{15}$ Hz [3 + 3 marks]

Q3b(ii)

Stopping potential $V_{stop} = (hc/\lambda - W_0) / e = (1240 \text{ nm.eV}/180 \text{ nm} - 4.2 \text{ eV})/e = 2.7 \text{ V}$

[3 marks]

Q3c

The energy of the incoming photon is $E_i = hc/\lambda = 0.775 \text{ MeV}$ [3 mark]

Since the outgoing photon and the electron each have half of this energy in kinetic form, $E_o = hc/\lambda' = 0.775 \text{ MeV} / 2 = 0.388 \text{ MeV} and$ $\lambda' = hc/E_o = 1240 \text{ eV}. \text{ nm} / 0.388 \text{ MeV} = 0.0032 \text{ nm}$ The Compton shift is $\Delta \lambda = \lambda' - \lambda = (0.0032 - 0.0016) \text{ nm} = 0.0016 \text{ nm}$

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[3 marks]
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By \Delta \lambda = \lambda_c (1 - \cos \theta) = h/m_e c (1 - \cos \theta)

0.0016 \text{ nm} = 0.00243 \text{ nm} (1 - \cos \theta)

\Rightarrow \theta = 70^\circ

[3 marks]
```

Question 4. (25 marks) [Soalan 4. (25 markah]

- (a) An electron is contained in a one-dimensional box of width 0.100 nm. Using the particle-in-a-box model, [Suatu elektron terkandung di dalam satu kotak satu dimensi yang lebarnya 0.100 nm. Dengan menggunakan model zarah-dalam-satu-kotak]
 - (i) Calculate the n = 1 energy level and n = 4 energy level for the electron in eV.
 [Hitungkan paras tenaga n = 1 dan n = 4 untuk elektron itu dalam unit eV.]
 - (ii) Find the wavelength of the photon (in nm) in making transitions that will eventually get it from the the n = 4 to n = 1 state [Hitungkan jarak gelombang foton (dalam unit nm) semasa ia membuat peralihan yang membawanya dari keadaan n = 4 ke keadaan n = 1]

Serway solution manual 2, Q33, pg. 380, modified

- (b) Consider a 20-GeV electron. [Pertimbangkan suatu elektron 20 GeV.]
 - (i) What is its Lorentz factor γ ? [Apakah faktor Lorentznya?]
 - (ii) What is its de Broglie wavelength? [Apakah jarak gelombang de Broglie-nya?]
 Serway solution manual 2, Q12, pg. 376, modified

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- (c) A photon is emitted as a hydrogen atom undergoes a transition from the n = 6 state to the n = 2 state. Calculate [Suatu foton dipancarkan ketika suatu atom hidrogen melakukan satu peralihan dari keadaan n = 6 ke n = 2. Hitungkan]
 - (i) the energy [tenaga]
 (ii) the wavelength [jarak gelombang]
 (iii) the frequency [frekuensi]
 of the emitted photon
 - [foton yang dipancarkan]

Serway solution manual 2, Q47, pg. 360, modified

Solution:

Q4a(i) In the particle-in-a-box model, standing wave is formed in the box of dimension *L*: $\lambda_n = \frac{2L}{n}$ [1 marks]

The energy of the particle in the box is given by

$$K_n = E_n = \frac{p_n^2}{2m_e} = \frac{(h/\lambda_n)^2}{2m_e} = \frac{n^2 h^2}{8m_e L^2} = \frac{n^2 \pi^2 \hbar^2}{2m_e L^2}$$

[2 marks]

$$E_1 = \frac{\pi^2 \hbar^2}{2m_e L^2} = 37.7 \text{ eV}$$
[2 mark]

 $E_4 = 4^2 E_1 = 603 \text{ eV}$ [2 mark]

Q4a(ii)

The wavelength of the photon going from n = 4 to n = 1 is $\lambda = hc/(E_6 - E_7)$ = 1240 eV nm/ (603 – 37.7) eV = **2.2 nm** [2 marks]

Q4b(i)

From $E = \gamma m_e c^2$, $\gamma = E/m_e c^2 = 20 \text{ GeV}/0.51 \text{ MeV} = 39216$ [4 marks]

Q4b(ii)

Momentum p = E/c = 20 GeV/c (rest mass of electron ignored, $m_e c^2 \ll E$) $\lambda = hc/E = hc/pc = 1240 \text{ eV nm} / 20 \text{ GeV} = 6.2 \times 10^{-17} \text{ m}$ [3 marks]

O4c

For hydrogen,
$$E_n = -\frac{13.6}{n^2} eV$$

Q4c(i)
 $\Delta E_{6\to 2} = E_6 - E_2 = -13.6 \left(\frac{1}{6^2} - \frac{1}{2^2}\right) eV = 3.02 eV$

[3 marks]

O4c(ii)

 $\lambda_{6\to 2} = hc / \Delta E_{6\to 2} = 1240$ nm · eV / 3.02eV = 410 nm [3 marks]

O4c(iii)

 $v = c/\lambda = 7.32 \text{ x } 10^{14} \text{ Hz}$ [3 marks]

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UNIVERSITI SAINS MALAYSIA

KSCP Academic Session 2003/2004

April 2004

ZCT 104E/3 - Physics IV (Modern Physics) [Fizik IV (Fizik Moden)]

Duration: 3 hours [Masa: 3 jam]

Please check that the examination paper consists of ELEVEN pages of printed material before you begin the examination.

[Sila pastikan bahawa kertas peperiksaan ini mengandungi SEBLELAS muka surat vang bercetak sebelum anda memulakan peperiksaan ini.]

Instruction: Answer all FOUR (4) questions.

Students are allowed to answer all questions in Bahasa Malaysia or in English.

Please answer Question 1 in the objective answer form provided. Submit the objective answer form and the answers to the structured questions (i.e. O2 - O4) separately.

[Arahan: Jawab kesemua EMPAT soalan. Pelajar dibenarkan menjawab semua soalan sama ada dalam Bahasa Malaysia atau Bahasa Inggeris. Sila jawab Soalan 1 dalam kertas jawapan objecktif yang dibekalkan. Hantar kertas jawapan objecktif dan jawapan kepada soalan struktur (iaitu Soalan 2 – Soalan 4) berasingan.]

Data

speed of light in free space, $c = 3.00 \text{ x} 10^8 \text{ m s}^{-1}$ permeability of free space, $\mu_0 = 4\pi \times 10^{-7} \text{ H m}^{-1}$ permittivity of free space. $\varepsilon_0 = 8.85 \text{ x } 10^{-12} \text{ F m}^{-1}$ elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$ the Planck constant, $h = 6.63 \times 10^{-34} \text{ J s}$ unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$ rest mass of electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$ rest mass of proton, $m_p = 1.67 \times 10^{-27} \text{ kg}$ molar gas constant, = 8.31 J K⁻¹ mol⁻¹ the Avogadro constant, $N_{\rm A} = 6.02 \text{ x } 10^{23} \text{ mol}^{-1}$ gravitational constant, $G = 6.67 \text{ x } 10\text{-}11 \text{ N m}^2 \text{ kg}^{-2}$ acceleration of free fall, $g = 9.81 \text{ m s}^{-2}$

Q1. [25 marks]

- 1.1 What were the consequences of the negative result of the Michelson-Morley experiment? [Antara berikut yang manakah akibat keputusan negatif eksperimen Michelson-Morley?]
 - I. It render untenable the hypothesis of the ether [*Ia menjadikan hipotesis ether tidak dapat dipertahankan*]
 - II. It suggests the speed of light in the free space is the same everywhere, regardless of any motion of source or observer [Ia mencadangkan bahawa laju cahaya dalam ruang bebas adalah sama di mana-mana sahaja, tidak kira sama ada punca cahaya atau pemerhati mempunyai sebarang pergerkan]
 - **III.** It implies the existence of a unique frame of reference in which the speed of light in this frame is equal to *c* [*Ia mengimplikasikan kewujudan suatu rangka rujukan yang laju cahaya dalam rangka tersebut adalah bersamaan dengan c*]

A. III only B. I,II C. I, III D. I, II, III E. Non of the above [*Tiada dalam pilihan di atas*]

Ans: B

Murugeshan, S. Chand & Company, New Delhi, pg. 25, Q1.

- **1.2** Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I. The expression for kinetic energy of a relativistic particle is given by $\frac{1}{2}mv^2$

[Ekspresi tenaga kinetic suata zarah kerelatifan ialah $\frac{1}{2}mv^2$]

- **II.** Special theory of relativity is applicable to accelerating system [Teori kerelatifan khas boleh dipergunakan ke atas sistem yang mengalami pecutan]
- **III.** The maximal velocity ever attainable is that of light in free space [Laju maksimum yang mungkin tercapai ialah laju cahaya dalam ruang bebas]
- IV. The mass of a particle becomes infinite at the speed equal to *c* [Jisim suatu zarah menjadi infinit pada kelajuan bersamaan dengan c]

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A. II.III	B. I.II.III.IV	C. I. II. III	D. III. IV

E. Non of the above [Tiada dalam pilihan di atas]

Ans: D

Murugeshan, S. Chand & Company, New Delhi, pg. 18, Q23.(for I), pg. 26, Q5.(for II), pg. 27, Q12.(for III), pg. 27, Q14.(for IV),

- **1.3** Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I The concept of Bohr orbit violates the uncertainty principle [Konsep orbit Bohr melanggar prinsip ketidakpastian]
 - II A hydrogen atom has only a single electron [Atom hidrogen mempunyai satu elektron tunggal sahaja]
 - III The spectrum of hydrogen consists of many lines even though a hydrogen atom has only a single electron [Spektrum hidrogen terdiri daripada banyak pinggir (garisan) walaupun atom hidrogen hanya mempunyai satu elektron sahaja]
 - IV Most of an atom consists of empty space [Kebanyakan daripada isipadu suatu atom terdiri daripada ruang kosong]
 - A. I,II B. I,II,III,IV C. I, II, III D. III, IV E. Non of the above *[Tiada dalam pilihan di atas]*

Ans: D

Murugeshan, S. Chand & Company, New Delhi, pg. 86, Q13.(for I), pg. 88, Q19.(for II,III), pg. 87, Q11.(for IV)

- 1.4 Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I In the Bohr theory of the hydrogen atom, the potential energy of the orbiting electron is positive [Dalam teori atom hidrogen Bohr, tenaga keupayaan elektron yang mengorbit ialah positif]
 - II In the Bohr theory of the hydrogen atom, the kinetic energy of the orbiting electron is positive [Dalam teori atom hidrogen Bohr, tenaga kinetik elektron yang mengorbit ialah positif]
 - III In the Bohr theory of the hydrogen atom, the potential energy of the orbiting electron is negative

[Dalam teori atom hidrogen Bohr, tenaga keupayaan elektron yang mengorbit ialah negatif]

IV. In the Bohr theory of the hydrogen atom, the kinetic energy of the orbiting electron is negative [Dalam teori atom hidrogen Bohr, tenaga kinetik elektron yang mengorbit ialah negatif]

A. I,II	B. III,IV	C. I, IV	D. II, III
E. Non of t	he above [Tiada da	lam pilihan di atas]	

Ans: D

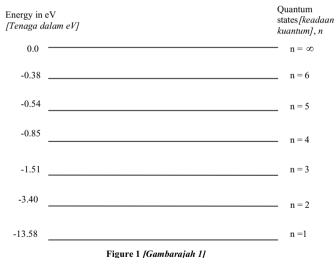
Murugeshan, S. Chand & Company, New Delhi, pg. 91, Q36

Q1.5 – Q1.7 refers to the energy diagrams shown in Figure 1.

[Soalan 1.5 - Soalan 1.7 merujuk kepada gambarajah yang terpapar di Gambarajah 1.]

Some of the energy levels of the hydrogen atom are shown (not to proportion)

[Beberapa paras tenaga atom hidrogen dipaparkan seperti berikut (tidak mematuhi nisbah)]



1.5 How much energy in eV is required to raise an electron from the ground state to the n = 5 state? (ignore selection rules) [Apakah tenaga (dalam unit eV) yang diperlukan untuk menaikkan suatu elektron dari keadaan bumi ke keadaan n = 5? (abaikan petua pilihan)]

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1.6

1.7

1.8

A. 13 E. No		B. 10.18 e [Tiada dalam p	C. 12.73 ilihan di atas]	D. 13.04
	igeshan, S. Ch		New Delhi, pg. 92, Q Savin, Schaum's serie	
electi [Apa. terpa	on makes a tra kah anggaran	ansition from state <i>jarak gelombang</i>	of photon (in nm) emi e $n = 6$ to $n = 2$? (igno (dalam unit nm) untui ari keadaan $n = 6$ ke n	re selection rules) k foton yang
A. 91 E. No		B. 122 e [Tiada dalam p	C. 94 ilihan di atas]	D. 410
Ans: My o	D wn question			
under rules) [Tera	rgoes transition) lapat berapa fo galami peraliho	This to the $n = 4$ stands to the n berbeza yang	emitted by the hydrog te from the <i>n</i> = 6 state g terpancar oleh atom = 6 dari keadaan n = 4	? (ignore selection <i>hidrogen yang</i>
A.3 E. No	B. 4 on of the above	C. 1 e [Tiada dalam p	D. 6 ilihan di atas]	
Ans: Muru		and & Company,	New Delhi, pg. 90, Q	30, modified
depei [Dald	nd on the refer	ence frame of obs utifan, pembolehc	observable(s) is (are) r server? erap yang mana adala kan pemerhati?]	
I. II. III. IV	Space Time Mass Energy			

IV. Energy

A. I,II B. I,II,III,IV C. I, II, III D. III,IV E. Non of the above /*Tiada dalam pilihan di atas*] D. III,IV

Ans: B

Murugeshan, S. Chand & Company, New Delhi, pg. 28, Q23.

- **1.9** Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - γ-rays have much shorter wavelength than x-rays [Jarak gelombang sinar γ adalah jauh lebih pendek daripada jarak gelombang sinar x]
 - **II.** The wavelength of *x*-rays in a *x*-ray tube can be controlled by varying the accelerating potential [Jarak gelombang sinar x dalam suatu tiub sinar x dapat dikawal dengan menyelaraskan beza upaya pecutan]
 - III. x-rays are electromagnetic waves [Sinar x ialah gelombang elektromagnetik]
 - IV. x-rays show diffraction pattern when passing through crystals [Sinar x memperlihatkan corak belauan semasa ia melalui hablur]

 A. I,II
 B. I,II,III,IV
 C. I, II, III
 D. III.IV

 E. Non of the above [Tiada dalam pilihan di atas]

Ans: B

Murugeshan, S. Chand & Company, New Delhi, pg. 132, Q1.(for I), pg. 132, Q3 (for II), pg. 132, Q4 (for III,IV)

- **1.10** Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I. Photoelectric effect arises due to the absorption of electrons by photons [Kesan fotoelektrik muncul kerana penyerapan elektron oleh foton]
 - **II.** Compton effect arises due to the scattering of photons by free electrons [Kesan Compton muncul kerana penyerakan foton oleh elektron bebas]
 - **III.** In the photoelectric effect, only part of the energy of the incident photon is lost in the process [Dalam kesan fotoelektrik, hanya sebahagian daripada tenaga foton tuju terlesap dalam proses tersebut]
 - IV. In the Compton effect, the photon completely disappears and all of its energy is given to the Compton electron [Dalam kesan Compton, foton hilang langsung dan kesemua tenaganya diberikan kepada elektron Compton]

A. I,II B. II,III,IV C. I, II, III D. III,IV

Ans: E [I = false; II = true; III = false; IV = false] Murugeshan, S. Chand & Company, New Delhi, pg. 134, Q13,

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- **1.11** Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I. Compton effect is experimentally observed for visible light rays [Kesan Compton boleh dicerap secara eksperimen bagi cahaya ternampak]
 - II. The presence of the unmodified line in Compton scattering can be explained in terms of Rayleigh scatterings [Kehadiran pinggir (garisan) yang tidak terubah dalam penyerakan Compton dapat diterangkan dengan penyerakan Rayleigh]
 - III. In Compton scattering, one neglects the effect of the nucleus on the x-rays [Dalam penyerakan Compton, kita mengabaikan kesan ke atas sinar x oleh nucleus]
 - A. II, III B. I, III C. I, II, III D. II only E. Non of the above *[Tiada dalam pilihan di atas]*

Ans: A

Murugeshan, S. Chand & Company, New Delhi, pg. 134, Q14 (for I), Q15 (for II), Q16 (for III),

- **1.12** Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I The energy of the quantum of light is proportional to the frequency of the wave model of light [Tenaga kuantum cahaya adalah berkadar dengan frekuensi model gelombang cahaya]
 - II In photoelectricity, the photoelectrons has as much energy as the quantum of light which causes it to be ejected [Dalam kesan fotoelektrik, fotoelektron mempunyai tenaga sebanyak tenaga kuantum cahaya yang menyebabkan fotoelektron terlenting]
 - III In photoelectricity, no time delay in the emission of photoelectrons would be expected in the quantum theory [Dalam teori kuantum, tiada tunda masa dalam pemancaran fotoelektron dijangkakan untuk kesan fotoelektrik]

A. II, IIIB. I, IIIC. I, II, IIID. I ONLYE. Non of the above [Tiada dalam pilihan di atas]

Ans: B

Murugeshan, S. Chand & Company, New Delhi, pg. 136, Q28 (for I), Q29, Q30 (for II,III)

1.13 An electron, proton and an alpha-particle have the same de Broglie wavelength. Which one moves faster? *[Elektron, proton dan zarah alpha ketiga-tiganya mempunyai jarak gelombang de Broglie yang sama. Yang manakah bergerak dengan lebih pantas?]*

A. Electron B. Proton C. Alpha-particle
D. All particles move at the same speed [kesemua zarah bergerak dengan kelajuan yang sama]
E. Non of the above [Tiada dalam pilihan di atas]

Ans: A

Murugeshan, S. Chand & Company, New Delhi, pg. 163, Q3

- **1.14** Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I. The de Broglie wavelengths of macroscopic bodies are generally too tiny to be experimentally detected [Jarak gelombang de Broglie jasad makroskopik secara amnya adalah terlalu kecil untuk dikesan secara eksperimen]
 - **II.** If Planck's constant were smaller than it is, quantum phenomena would be more conspicuous than they are now [Jika nilai pemalar Planck adalah lebih kecil daripada nilainya yang sedia ada, fenomena kuantum akan menjadi lebih sedia tercerap berbanding dengan ketercerapannya yang sedia ada]
 - III In quantum theory, the physical variables (e.g. energy, momentum) used to describe a confined electron are discrete [Dalam teori kuantum, pembolehubah fizikal (misalnya tenaga dan momentum) yang memerihalkan sesuatu elektron yang terkurung adalah diskrit

 A. II, III
 B. I ONLY
 C. I, II, III
 D. I, III

 E. Non of the above [Tiada dalam pilihan di atas]
 D. I, III

Ans: D

Murugeshan, S. Chand & Company, New Delhi, pg. 163, Q1 (for I), Q12 (for II), Q21 (for III)

1.15 Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]

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I. The experimental proof for which electron posses a wavelength $\lambda = \frac{h}{n}$

was first verified by Davisson and Germer [Pembuktian scara eksperimen bahawa elektron mempunyai jarak gelombang $\lambda = \frac{h}{p}$ pada mula-mulanya ditentukan oleh Davisson and Germer]

- II. The experimental proof of the existence of discrete energy levels in atoms involving their excitation by collision with low-energy electron was confirmed in the Frank-Hertz experiment [Pembuktian secara eksperimen kewujudan paras tenaga diskrit dalam atom yang melibatkan pengujaan mereka oleh perlanggaran dengan elektron bertenaga rendah telah dipastikan dalam eksperimen Frank-Hertz]
- III. Compton scattering experiment establishes that light behave like particles [Penyerakan Compton menetapkan bahawa cahaya berlagak seperti zarah]
- IV. Photoelectric experiment establishes that electrons behave like wave [Kesan fotoelektrik menetapkan bahawa elektron berlagak seperti gelombang]
- A. I,IIB. I,II,III,IVC. I, II, IIID. III,IVE. Non of the above [Tiada dalam pilihan di atas]

Ans: C

Serway and Moses, pg. 127 (for I), pg. 133 (for II), own options (for III,IV)

Q2. [25 marks]

(a) A man in a spaceship moving at a velocity of 0.9*c* with respect to the Earth shines a light beam in the same direction in which the spaceship is travelling.

[Seorang yang berada di dalam satu kapal angkasa yang bergerak pada halaju 0.9c relatif kepada Bumi menyinarkan satu bim cahaya ke arah yang mana kapal angkasa itu sedang bergerak.]

Compute the velocity of the light beam relative to Earth using [Hitungkan halaju bim cahaya itu relatif kepada Bumi dengan menggunakan]

(i) Galilean approach [pendekatan Galileo]

[3 marks]

(ii) Special relativity approach [pendekatan teori kerelatifan khas]

[6 marks]

Please define clearly all the symbols used in your working. [Sila nyatakan dengan jelas definasi simbol-simbol yang digunakan dalam kerja anda.] Ans

(a) O' is the moving frame travelling at v = 0.9c with respect to the Earth. Speed of the light beam as seen in the frame O' is u' = c. O is the Earth frame. We wish to find the speed of the light beam as seen from frame O, u.

(i) According to Galilean transformation, u = u' + v = c + 0.9c = 1.9c.

(ii) Use $u = \frac{u' + v}{c + 0.9c}$

$$u = \frac{u}{1 + \left(\frac{v}{c^2}\right)u'} = \frac{c}{1 + \left(\frac{0.9c}{c^2}\right)c} = c \implies v = c$$

Acosta, Q4-7, pg. 53, modified

(b) How fast does a rocket have to go for its length to be contracted to 99% of its rest length? [Berapa cepatkah suatu roket harus bergerak supaya panjangnya menyusut kepada 99% daripada panjang rehatnya?]

[5 marks]

Ans:

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$$\frac{L}{L_0} = 0.99 = \sqrt{1 - \left(\frac{v}{c}\right)^2}$$

 $\Rightarrow v = 0.141c$

Gautreau and Savin, Schaum's series modern physics, pg.21, Q. 4.1

(c) The average lifetime of μ-meson with a speed of 0.95c is measured to be 6×10⁻⁶ s. Compute the average lifetime of μ-meson in a frame in which they are at rest.
 [Hayat purata meson-μ yang bergerak dengan kelajuan 0.95c adalah

diukur sebagai 6×10⁻⁶ s. Hitungkan hayat purata meson-μ dalam rangka di mana mereka adalah rehat] [5 marks]

Ans:

Lorentz factor is
$$\gamma = \frac{1}{\sqrt{1 - \left(\frac{v}{c}\right)}} = \frac{1}{\sqrt{1 - (0.95)}} = 3.20$$

The time measured in a frame in which the μ -mesons are at rest is the proper time, Δt_0 :

 $\Delta t_0 = \Delta t / \gamma = = 6 \times 10^{-6} \text{ s}/3.2 = 1.87 \times 10^{-6} \text{ s}$

Gautreau and Savin, Schaum's series modern physics, pg.24, Q 5.1

- (d) (i) What is the rest mass of a proton in terms of MeV? [Apakah jisim rehat satu proton dalam unit MeV?] [2 marks]
 - (ii) What is the relativistic mass of a proton (in terms of MeV) whose kinetic energy is 1 GeV? [Apakah jisim kerelatifan satu proton (dalam unit MeV) yang bertenaga kerelatifan 1 GeV?]

[4 marks]

Ans:

- (i) $m_p c^2 = 1.67 \times 10^{-27} \text{kg x} (3 \times 10^8 \text{ m/s})^2 = 1.503 \times 10^{-10} \text{ J} = 1.503 \times 10^{-10} / (1.6 \times 10^{-19}) \text{ eV} = 939.4 \text{ MeV}$
- (ii) $K = (\gamma 1)m_pc^2 = 1 \text{ GeV}$ $(\gamma - 1) = 1 \text{ GeV}/m_pc^2 = 1 \text{ GeV}/939.4 \text{ MeV} = 1.06$ $\gamma = 1.06 + 1 = 2.06$ $mc^2 = \gamma m_pc^2 = 2.06 \times 939.4 \text{ MeV} = 1939.4 \text{ MeV}$

Note: Due to the inconsistency between the English and Malay version of question I would also give full mark to those who used total relativisic energy $E = \gamma m_{p}c^{2} = 1$ GeV in the calculation (instead of using $K = (\gamma - 1)m_{p}c^{2} = 1$ GeV).

Gautreau and Savin, Schaum's series modern physics, pg.55, Q 8.34, slightly modified.

Q3. [25 marks]

(a) A proton is accelerated from rest through a potential of 1 kV. Find its de Broglie wavelength.
 [Suatu proton dipecutkan dari keadaan rehat melalui satu beza keupayaan 1 keV. Hitungkan jarak gelombang de Broglienya.]

[6 marks]

Ans.

$$K = \frac{p^2}{2m_p} = \text{kinetic energy of the proton} = 1 \text{ keV.}$$
$$\lambda = \frac{h}{p} = \frac{h}{\sqrt{2m_p K}} = \frac{h}{\sqrt{2m_p K}} = \frac{6.63 \times 10^{-34} \text{ J} \cdot \text{s}}{\sqrt{2 \times 1.67 \times 10^{-27} \text{ kg} \cdot 1000 \times 1.6 \times 10^{-19} \text{ J}}} = 9.1 \times 10^{-3} \text{ Å}$$

Gautreau and Savin, Schaum's series modern physics, pg.97, Q. 10.38

(b) Determine the cutoff wavelength in Å of x-rays produced by a 50-keV electrons in a x-ray tube.

[Tentukan jarak gelombang penggal (dalam unit $\overset{\circ}{A}$) sinar x yang dihasilkan oleh elektron 50 keV dalam suatu tiub sinar x.] [5 marks]

Ans.

$$\lambda_{cutoff} = \frac{hc}{eV} = \frac{1240 \text{eV} \cdot \text{nm}}{50 \text{keV}} = 0.0248 \text{nm} = 0.24 \text{ Å}$$

Schaum's series 3000 solved problem, pg.714, Q. 38.39

(c) Determine the photon flux (in unit of number of photons per unit time per unit area) associated with a beam of monochromatic light of

wavelength 3000 Å and intensity 3×10^{-14} W/m².

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[Tentukan fluks foton (dalam unit bilangan foton per unit masa per unit luas) yang bersepadanan dengan suatu bim cahaya monokromatik

berjarak gelombang 3000 $\stackrel{o}{A}$ dan berkeamatan $3 \times 10^{-14} \text{ W/m}^2$.]

[8 marks]

Ans:

N

$$= I/\varepsilon = I \cdot \left(\frac{\lambda}{hc}\right)$$

= 3×10⁻¹⁴ W/m² × $\frac{300 \text{ nm}}{1240 \text{ eV} \cdot \text{ nm}}$
= 7.26×10⁻¹⁵ $\left(\frac{W}{\text{ eV}}\right)$ /m² = 7.26×10⁻¹⁵ (6.25×10¹⁸ / s)/m² = 45375 photon / m² · s

Gautreau and Savin, Schaum's series modern physics, pg.98, Q. 10.53

(d) Suppose that the x-component of the velocity of a 2×10⁻⁴ kg mass is measured to an accuracy of ±10⁻⁶ m/s. What is the limit of the accuracy with which we can locate the particle along the x-axis? [Andaikan bahawa komponen x halaju suatu jasad berjisim 2×10⁻⁴ kg diukur tepat kepada kejituan ±10⁻⁶ m/s. Apakah limit kejituan kedudukannya yang boleh kita pastikan sepanjang paksi-x?]

Ans.

$$\Delta p\Delta x \ge \frac{\hbar}{2}; \ p = mv;$$

$$\Delta(mv)\Delta x = m\Delta v\Delta x \ge \frac{\hbar}{2}$$

$$\Delta x \ge \frac{\hbar}{2m\Delta y} = \frac{h}{4\pi m\Delta y} = 2.63 \times 10^{-25} \,\mathrm{m}$$

Gautreau and Savin, Schaum's series modern physics, pg.98, Q. 10.53

Q4. [25 makrs]

(a) Given the ground state energy of hydrogen atom -13.6 eV, estimate the ionisation energy for He⁺.
 [Diberi bahawa tenaga keadaan bumi atom hidrogen ialah -13.6 eV, anggarkan tenaga pengionan untuk He⁺.]
 [5 marks]

Ans: Generally, the energy state of an hydrogen-like atom with Z charge in its nucleus is given by $E_n = \frac{Z^2}{n^2} E_0$, $E_0 =$ ground state energy of hydrogen atom.

Hence ionisation energy of He⁺ (with Z = 2) = E_{∞} (He⁺) - E_0 (He⁺) = 0 - $\frac{2^2}{1^2}E_0$ = -4(-13.6) eV = 54.4 eV

(b) What are the n values in the transition that produces the third longest wavelength in the Balmer series in the hydrogen atom? (ignore selection rules) [Apakah nilai-nilai n yang peralihannya menghasilkan jarak gelombang yang ketiga paling panjang dalam siri Balmer atom hidrogen? (abaikan petua pilihan)]

[4 marks]

Ans: $n = 5 \rightarrow n = 2$ Giancoli, pg. 856, Q. 50, modified.

(c) Given the Bohr radius of the hydrogen atom $r_0 = 0.5 \stackrel{o}{A}$, estimate the speed (in m/s) of the electron in the ground state orbit of the hydrogen atom.

[Diberi bahawa radius Bohr atom hidrogen ialah $r_0 = 0.5$ Å, anggarkan laju (dalam m/s) elektron dalam orbit keadaan bumi atom hidrogen.]

[8 marks]

Ans: Equating the centrepetal force required by the electron to the electrostatic force,

$$\frac{mv^2}{r} = \frac{e^2}{4\pi\varepsilon_0 r^2} \Rightarrow v_0^2 = \frac{e^2}{4\pi\varepsilon_0 mr_0} \Rightarrow v_0 = \sqrt{\frac{e^2}{4\pi\varepsilon_0 mr_0}} = 2.25 \times 10^6 \,\mathrm{m/s}$$

My own question

(d) Given the Rydberg constant
$$R = 1.0967758 \ge 10^{-3} \text{ A}^{\circ^{-1}}$$
, determine, in

Α,

- (i) the shortest, and
- (ii) the longest

wavelengths of the Lyman series of hydrogen.

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[Diberi bahawa pemalar Rydberg ialah R =
$$1.0967758 \times 10^{-3} \text{ \AA}^{\circ^{-1}}$$

Tentukan, dalam unit $\overset{\circ}{A}$, jarak gelombang yang

(i) paling pendek, dan(ii) paling panjang

dalam siri Lyman hidrogen]

[4 + 4 marks]

Ans:

(i) Wavelengths in the Lyman series are given by $n_l = 1$ $\frac{1}{\lambda} = R\left(\frac{1}{1^2} - \frac{1}{n^2}\right), n = 2,3,4...$

(ii) The longest wavelength corresponds to
$$n = 2$$
:

$$\frac{1}{\lambda_{\text{max}}} = \left(1.097 \times 10^{-3} \text{ \AA}^{-1}\right) \left(\frac{1}{1^2} - \frac{1}{2^2}\right), \text{ or } \lambda_{\text{max}} = 1215 \text{ \AA}^{-1}$$

The longest wavelength corresponds to $n \rightarrow \infty$

$$\frac{1}{\lambda_{\min}} = \left(1.097 \times 10^{-3} \text{ \AA}^{-1}\right) \left(\frac{1}{1^2} - \frac{1}{\infty^2}\right), \text{ or } \lambda_{\max} = 912 \text{ \AA}^{\circ}$$

Gautreau and Savin, Schaum's series modern physics, pg.107, Q. 11.1

ZCT 104/3E Modern Physics Semester II, Sessi 2004/05 Test I (17 Dec 2004)

Data

Speed of light in free space, $c = 3.00 \times 10^8 \text{ ms}^{-1}$ Elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$ The Planck constant, $h = 6.63 \times 10^{-34} \text{ J} \text{ s}$ Unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$ Rest mass of electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$ Rest mass of proton, $m_p = 1.67 \times 10^{-27} \text{ kg}$

- What are the major flaws in the classical model of blackbody radiation given by Rayleigh-Jeans laws? I (F) Molecular energy is quantized
 - **II (F)** Molecules emit or absorb energy in discrete irreducible packets
 - III(T) The intensity of short wavelength radiation emitted by a blackbody approaches infinity as the wavelength decreases.IV (T) Energy is continuously divisible
 - iv (i) Energy is continuously divisible

A. III, IV B. I, II,III C. II, III, IV D. I, II E. Non of the above

ANS:A, Serway, questions 1, 2, page 1313

- 2. What are the assumptions did Planck make in dealing with the problem of radiation?
 - I (T) Molecular energy is quantized
 - **II (T)** Molecules emit or absorb energy in discrete irreducible packets
 - **III(F)** The intensity of short wavelength radiation emitted by a blackbody approaches infinity as the wavelength decreases.
 - IV (F) Energy is continuously divisible

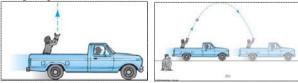
A. III, IV B. I, II,III C. II, III, IV D. I, II E. Non of the above

ANS:D, Serway, questions 1, 2, page 1313

3. An unstable high-energy particle enters a detector and leaves a track of length d before it decays. Its speed relative to the detector was v = c/2. What is its proper lifetime? That is how long would the particle have lasted before decay had it been at rest with respect to the detector?

A.
$$\frac{d}{c}$$
 B. $\frac{4d}{\sqrt{3c}}$ C. $\frac{2d}{\sqrt{3c}}$ D. $\frac{\sqrt{3d}}{c}$ E. Non of the above
RHW 7th ed. P5, pg. 1050
Solution: D

4. A ball was thrown upward by an observer in a van moving with constant speed *u* << *c*. He is observed by an observer in a rest frame attached to the ground, see figure below. Which of the following statement(s) is (are) true regarding the two inertial frames of reference?



I The ball thrown follows different path

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- II The kinematical laws of classical mechanics are valid only the moving frame (the van) but not to the rest frame attached to ground.
- III Classically Galilean transformation relates the trajectory of the ball in the rest frame with that in the moving frame.
- IV Since $u \ll c$, Lorentz transformation will fail to relate the trajectory of the ball in the rest frame with that in the moving frame.

A. II,III B. I, II,III C. II, III, IV D. I Only E. Non of the above My own question Solution: E (I, III are true)

5. What measurement(s) do two observers in relative motion always agree on? I The relativistic mass of an object II The relativistic momentum of an object III The relativistic energy of an object IV $E^2 - p^2$, where p is the magnitude of relativistic momentum and E the relativistic energy the object

A. II,III B. I, II,III C. II, III, IV D. IV Only E. Non of the above

My own question Solution: D

Free marks will be given for this question due to the typo in IV. It should actually reads: " $E^2 - c^2 p^2$, where p is the ".

Actually, the original statement is dimensionally correct in the natural unit system in which the c is taken to have a value of 1. However since we are adopting S.I. unit throughout the course we will take the original statement to be 'dimensionally wrong' as far as the ZCT 104 courses is concerned.

- 6. Which of the following statement(s) is (are) true?
 - I The upper limit of the speed of an electron is the speed of light *c*.

II As more energy E is fed into an object its momentum approaches $\frac{E}{-}$.

III There is no upper limit to the relativistic momentum of an electron. **IV** There is an upper limit to the relativistic momentum of an electron.

A. III B. I, II,III C II, IV D. IV Only E. Non of the above Serway Q12, pg. 1276 Solution: B

 The rest energy and total energy respectively, of three particles, expressed in terms of a basic amount *A* are (1) *A*, 2*A*; (2) *A*, 3*A*; (3) 3*A*, 4*A*. Without written calculation, rank the particles according to their kinetic energy, greatest first.

A. 2>1 = 3 E. 3>1 = 2 B. 1>2 = 3 C. 2>1>3 D. 2 = 1 = 3

RHW 7th ed. Q1, pg. 1050 Solution: A

8. The length of a spaceship is measured to be exactly half its rest length. By what factor do the spaceship's clocks run slow relative to clocks in the observer's frame?

A. 0.866 B. 0.745 C. 2.000 D. 0.366 E. 0.134

SESSI 04/05/TEST1 Solution: C

9. The length of a spaceship is measured to be exactly half its rest length. What is the speed parameter $\beta = v/c$ of the spaceship relative to the observer's frame?

A. 0.87 B. 2.00 C. 0.75 D. 2.73 E. 4.00 ANS: A We solve $L = L_0 \sqrt{1 - \left(\frac{\nu}{c}\right)^2} = L_0 \sqrt{1 - \beta} = \frac{L_0}{\gamma}$ for ν and then plug in: $\beta = \sqrt{1 - \left(\frac{L}{L_0}\right)^2} = \sqrt{1 - \left(\frac{1}{2}\right)^2} = 0.866.$ Resnick and Halliday, 7th edition, Problem 12, Pg. 1051

10. Consider a light pulse emitted from the origin, O, of a stationary frame S. The origin of a moving frame S', O', which overlaps with O at t = t' = 0 is moving with a constant speed *u* with respect to O. Which statement(s) correctly describe(s) the position of the wavefront of the light sphere as measured from the origins? r(r') is the distance of the wavefront from the origin O (O') at time t(t').

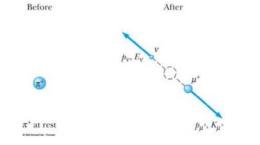
I
$$r = ct$$
 II $r' = ct'$ III $r' = r$ IV $r' = ut$

A. I,II B. I, II,III C. II, III, IV D. IV Only E. Non of the above My own question Solution: A

11. Which of the following statement(s) is (are) true regarding Lorentz transformation (LT)?
I Time dilation can be recovered from LT
II Length contraction can be recovered from LT
III Absolute simultaneity is not guaranteed by LT
IV Galilean transformation is a generalisation of LT

A. II,III B. I, II,III C. II, III, IV D. I, II E. Non of the above My own question Solution: B

Question 12-13 are based on the decay of a π meson into a muon and a massless neutrino shown in figure below. The mass of the muon is known to be $m_{\mu} = 106 \text{ MeV}/c^2$, and the kinetic energy of the muon is measured to be $K_{\mu} = 4.6 \text{ MeV}$. p_{μ} denotes the momentum of the muon.



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12. What is the momentum of the neutrino?

A.
$$\sqrt{\left(K_{\mu}+m_{\mu}c^{2}\right)^{2}-m_{\mu}^{2}c^{4}}$$

B. $\left(K_{\mu}+m_{\mu}c^{2}\right)$
C. $\sqrt{2m_{\mu}K_{\mu}}$
D. p_{μ}
E. Non of the above
Serway and Mosses. pg. 53
Solution: D

13. What is the total relativistic energy of the neutrino?

A.
$$\sqrt{(K_{\mu} + m_{\mu}c^2)^2 - m_{\mu}^2c^4}$$

B. $(K_{\mu} + m_{\mu}c^2) + \sqrt{(K_{\mu}^2 + 2K_{\mu}m_{\mu}c^2)^2}$
C. K_{μ}
D. $m_{\mu}c^2$
E. Non of the above
Serway and Mosses. pg. 52
Ans: A

Solution: $E_v = \sqrt{(p_v^2 c^2 + m_v^2 c^4)} = p_v c \ (m_v c^2 = 0)$. The momentum of neutrino, $p_v^2 = p_\mu^2$ (from Question 12 above) is related to the kinetic energy of the muon via $E_\mu = \sqrt{(p_\mu^2 c^2 + m_\mu^2 c^4)} = m_\mu c^2 + K_\mu$. Therefore the momentum of the neutrino is related to the kinetic energy of the muon via $p_v^2 c^2 = (m_\mu c^2 + K_\mu)^2 - m_\mu^2 c^4$. Taking the square root, we then have $E_v = p_v c = \sqrt{(K_\mu + m_\mu c^2)^2 - m_\mu^2 c^4}$.

14. Serway and Moses, Questions 12, page 37

What happens to the density of an object as its speed increases, as measured by an Earth observer?

A. Remain the same as it is when at rest **B.** Increase by a factor of γ **C.** Increase by a factor of γ^2 **D.** Increase by a factor of $1/\gamma$ **E.** Non of the above

ANS: C, my own question

15. What is the upper limit of the momentum of an electron?

A. *m_ec* B. *c* Serway, Q12, pg. 1276 Solution: D E. Non of the above

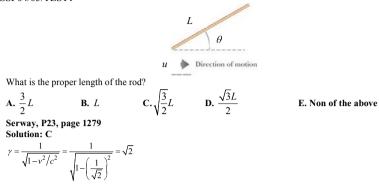
16. Which of the following statement(s) is (are) true?
I Only massless particle can travel at the speed of *c*.
II Not all massless particle can travel at the speed of *c*.
III It is not necessary that a massless particle must travel at the speed of *c*.
IV All particles which are not massless must travel at the speed lower than *c*.

A. II,III B. I, II,III C. I, III, IV D. I, IV E. Non of the above My own question Solution: D

C.0 D. Infinity

17. A moving rod is observed to have a length of L and to be orientated at an angle of $\theta = 45^{\circ}$ with respect to the

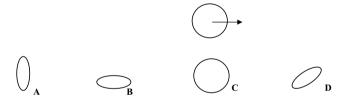
direction of motion, as shown in the figure below. The rod has a speed of $u = \frac{c}{\sqrt{2}}$.



SESSI 04/05/TEST1 Serway, P35, page 1280 Solution: A

We are also given L and θ (both measured in a reference frame moving relative to the rod). Thus, $L_x = L \cos \theta = \frac{L}{\sqrt{2}}$; $L_y = L \sin \theta = \frac{L}{\sqrt{2}}$. L'_x is a proper length, related to L_x by $L_x = \frac{L'_x}{\gamma}$. Therefore, $L'_x = \gamma L_x = \sqrt{2} \frac{L}{\sqrt{2}} = L$, and $L'_y = L_y = \frac{L}{\sqrt{2}}$. (Lengths perpendicular to the motion are unchanged). $\Rightarrow (L')^2 = (L'_y)^2 + (L'_x)^2 = \frac{L^2}{2} + L^2 = \frac{3L^2}{2} \Rightarrow L' = \sqrt{\frac{3}{2}}L$

18. A spaceship in the shape of a sphere moves past and observer on Earth with a speed of v = 0.5c in the direction as indicated by the arrow. What shape will the observer see as the spaceship move past?





19. What is the speed of an object having relativistic momentum of magnitude *p* and rest mass *m*?

A.
$$\frac{p}{m}$$
 B. $\frac{c}{\sqrt{1 + (mc/p)^2}}$ C. $\frac{mc^2}{u}$ D. $\frac{mu^2}{c}$ E. Non of the above

Serway, P32, page 1280 Solution: B

20. An electron with rest mass m_e moves with a speed of $\frac{\sqrt{3}}{2}c$. What is the work required to increase its speed

to
$$\frac{2\sqrt{2}}{3}c$$
?
A. m_ec^2
B. $0.511m_ec^2$
C. $\frac{5}{36}m_ec^2$
D. $\frac{\sqrt{5}}{6}m_ec^2$
E. Non of the above

ZCT 104/3E Modern Physics Semester II, Sessi 2004/05 Test II (18 Feb 200b)

- 1. Which statements is (are) TRUE about photoelectricity according to classical physics? (ANS: D)
- D Light beam of higher intensity is expected to eject electrons with higher kinetic energy from the metal surface (T)
- ID In photoelectric experiment the energy carried by a beam of light is considered to be continuous (T)
- IID Light is wave and not comprised of quantum of energy (T)
- IV) When light is irradiated on the metal surface, some time lag is expected before photoelectrons are ejected from the surface (T)
- A. I.II B. II. III
- С. Ш D. I, II, III, IV
- E. Non of A, B, C, D
- 2. Let a given metal surface is irradiated with monochromatic light of intensity I_1 . Then the same surface is irradiated by monochromatic light with intensity I_2 (where $I_2 > I_1$) but with a longer wavelength. Which of the following statement(s) is (are) true? (ANS: E)
- I) The energy of the photon in the beam with intensity I_2 is larger than that in the beam with intensity I_1 . (F)
- ID The saturated photocurrents will remain unchanged. (F)
- The maximum kinetic energy of the III) photoelectron will increase for the beam with intensity I_2 (F)
- IV) The different intensity of light will alter the work function of the metal surface (F)

A. I, II	B.	П,	Ш
----------	----	----	---

- C. III D. III, IV
- E. Non of A, B, C, D
- 3. Which of the following statements is (are) correct about Bohr's atom and a quantum particle trapped inside a simple infinite quantum well of width d? (ANS: A)
- D The gap separating energy levels of higher quantum number becomes closer

and closer in the Bohr's hydrogen atom, whereas in the case of particle in a box the gap becomes larger and larger at higher quantum levels. (T)

The electron in the Bohr's atom is subjected to a non-zero potential due to Coulomb's attraction, whereas in the box the particle is subjected to zero potential. (T)

ID

D

I)

- IID The energy levels in the Bohr's atom are negative whereas they are positive for the particle in the well. (T)
- IV) In both cases the particles involved form standing waves (T)

A. I, II, III, IV B. II. III C. III D. III. IV E. Non of A. B. C. D

4. Which of the following statements is (are) true? (ANS: C)

- A particle has a de Broglie wavelength that is related to its linear momentum (T)
- A particle's momentum must be ID quantised in all systems, bounded or unbounded (F)
- III) A particle's kinetic energy must be quantised in all systems, bounded or unbounded (F)
- A particle's kinetic energy is only IV) quantised in bounded system (T)

A.	I, II, IV	B. I, II, III
C.	I, IV	D. II, III
E.	Non of A, B, C, D	

- 5. In order to have photoelectrons ejected from a metal surface in a typical photoelectric effect experiment, (ANS: C)
- the frequency of the light used must be larger than a certain cut-off value (T) ID the intensity of the light used must be
- larger than a certain cut-off value (F) the wavelength of the light used must be III)
- larger than a certain cut-off value (F) IVthe saturated photocurrent must be larger than a certain cut-off value (F)

A. I. II. IV B. I. III C. I D. II. III. IV E. Non of A, B, C, D

SESSI 04/05/TEST2

- 6. What of the following statements are TRUE regarding photoelectric effect (PE) and Compton effect (CE)? (ANS: D)
- D In PE light behaves like particle, whereas in CE light behave like wave (F)
- In PE light behaves like wave, whereas ID in CE light behave like particle (F)
- In PE only part of the photon's energy is IID lost to the atom, whereas in CE all of the photon's energy is lost to the free electron (F)
- IV In PE all of the photon's energy is lost to the atom, whereas in CE only part of the photon's energy is lost to the free electron (T)
- A. I.III B. II. III
- C. II. IV D. IV
- E. Non of A. B. C. D
- 7. Which statements is (are) TRUE about photoelectric and Compton effects? (ANS: E)
- Compton effect experiment confirms D that the energy of the quantum of light is proportional to the frequency of the wave model of light (F)
- ID Compton effect experiment confirms that the radiant energy of light is quantized into concentrated bundle (F)
- Photoelectric effect infers that the IID radiant energy of light is quantized into concentrated bundle (T)
- IV Both Compton effect and photoelectric effect confirm that EM radiation has both wave and particle properties (F)

А.	I, III	B.	II, III
С.	II, IV	D.	IV
E.	Non of A, B	, C, D	

- 8. Which of the following is (are) the correct statement(s) about X-ray production in a conventional X-ray tube? (ANS: B)
- I) Part or all of the kinetic energy of the moving electron is converted into X rays photon (T)
- ID X-rays is emitted when the bombarding electrons undergo Compton scattering (F)
- IID The production of x-rays can be considered as a photoelectric process (F) The shortest wavelength in the x-rays IV)
- spectrum is the same for different material (T)

A.	II, III	B. I, IV
C.	II, IV	D. IV
E.	Non of A, B	, C, D

- 9. Which of these statements is (are) true about blackbody radiation? (ANS: B)
- D Rayleigh-Jeans law is behaving in a physically acceptable manner at short wavelengths (F)
- II) Rigel (the blue star) is hotter than Betelguese (red star) because of the position of the peak wavelength in their black body spectrum (T)
- IID According to Rayleigh-Jeans law the average energy of the oscillators is given by the equipartition theorem (T)
- The spectral distribution of radiation IV) from a blackbody can only be explained in terms of quantised energy levels of the oscillators (T)

А.	I, II, III, IV	B. II, III, IV
C.	II, IV	D. III, IV
E.	Non of A, B, C, D	

10. Which of these statements are correct? (ANS: E)

- D We conclude that light behave like wave when we find that the light from the sun arrives to the Earth after 8 minutes it was emitted. (F)
- When we consider light to behave like a II) particle we expect some detectable time lag for the electron to be emitted from the surface of the metal in a PE experiment. (F)
- III) When we consider light to behave like wave we expect some detectable time lag for the electron to be emitted from the surface of the metal in a PE experiment. (T)
- IV) Photoelectric effect occurs at the same energy scale as that of the x-rays production because x-rays production is the inverse of the photoelectric process. (F)

A. I, II, III, IV	B. II, III, IV
C. II, IV	D. III, IV
E. III	

- 11. Which of the following statements is (are) TRUE? (ANS: E)
- The energy levels of the atomic orbit is D quantized (T)
- The energy associated with the orbits of ID the electron in a hydrogen atom is negative because it is not a bounded system (F)
- IID E = 0 means the electron is free from the bondage of the nucleus' potential field. (T)
- IV) Electron at very large quantum number *n* is tightly bounded to the nucleus by the EM force. (F)

A. I, II, III, IV	B. II, III, IV
C. II, IV	D. III, IV
E. I, III	

- 12. Which of the following statements is (are) TRUE about the Bohr's model of hydrogenlike atom? (ANS: C)
- D It applies the Newton's second law for the atom's mechanical stability (T)
- ID The angular momentum is postulated to be quantised via $L = nh/2\pi$ (T)
- IID It assumes the validity of classical electromagnetic theory for the orbiting electron (F)
- The only stable orbits of radius r are IV) those that can fit in a multiple number of standing wave of the electron, i.e $2\pi r =$ $n\lambda(T)$

А.	I, II, III, IV	B. II, III, IV
C.	I, II, IV	D. III,IV
E.	Non of A, B, C, D	

- 13. Which of the following statements is (are) true? (ANS C)
- Thompson suggestion of the Plum D) Pudding Model is falsified by Rutherford's alpha particle experiment (T)
- ID Rutherford suggested the planetary model of atoms. (T)
- de Broglie is the first to experimentally IID confirm that electron manifests wave nature. (F)
- IV) Frank-Hertz experiment confirms the existence of discrete energy levels in mercury atom (T)

A.	I, II, III, IV	B. II, III, IV
C.	I, II, IV	D. III,IV
E.	Non of A, B, C, D	

- 14. Which of the following statement is (are) true about the Plum-pudding model by Thompson and Rutherford's experiment? (ANS A)
- D Plum-pudding model fails to explain the emission & absorption line spectrum from atoms because it predicts only a single unique emission frequency. (T)
- ID Plum-pudding model cannot explain the 180 degree back-scattering of alpha particle seen in Rutherford's scattering experiment. (T)
- IID The planetary model of atoms is plagued by infrared catastrophe (T) IV) In the Rutherford's alpha particle
 - scattering experiment, the large deflection of alpha particle is caused by a close encounter between alpha particle and the diffused distribution of the positive charge of an atom. (F)

B. II. III. IV A. I. II. III C. I. II. IV D. III. IV E. Non of A. B. C. D

- 15. Which of the following statements is (are) true regarding the basic properties of atoms? (ANS: A)
 - Atoms are of microscopic size, $\sim 10^{-10}$ m (T)
- ID Atoms are stable (T)

I)

D)

- III) Atoms contain negatively charges, electrons, but are electrically neutral. (T) IV) Atoms never emit and absorb EM
- radiation. (F)B. II. III. IV

A.	I, II, III	B. II, III, I
C.	I, II, IV	D. III, IV
E.	Non of A, B, C, D	

16. Which of the following statements is (are) true about Bohr's hydrogen-like atom? (ANS C)

The increase in the quantum number nmeans an increase in the energy of the atomic states. (T)

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II)	When <i>n</i> approach infinity, the energy
	states become infinity. (F)
III)	Free electron is the electron which has

the smallest quantum number n (F) IV) The zero point energy is the energy of

	the lowest	possible qu	antum lev	el (T
A.	I. II. III	В		IV

1	1, 11, 111	ь.	,, .
C.	I, IV	D.	III, IV
E.	Non of A, B, C, D		

- 17. Heisenberg's uncertainty principle is a consequence of (ANS: A)
- A. the intrinsic wave nature of particle
- **B.** the intrinsic particle nature of wave
- **C.** the indivisible nature of particle
- **D.** the divisible nature of particle
- E. probabilistic interpretation of the wave function
- 18. Which of the following statements is (are) true about the spectrum from hydrogen atom? (ANS: A)
- Balmer series involve transitions of D electron from higher orbits to the n = 2orbit
- II) Balmer series is the first spectral series of hydrogen atom observed
- When electron in higher orbit is de-III) excited to lower orbit, photons of discrete frequency are emitted from the atom. as seen in the emission spectrum
- When electron in lower orbit is excited IV) to higher orbit, photons of discrete frequency are absorbed by the atom, as seen in the absorption spectrum

A.	I, II, III, IV	B. II, III, IV
C.	I, IV	D. III, IV
E.	Non of A, B, C, D	

- 19. Which of the following statements is (are) true regarding a quantum particle trapped inside an infinite well of width L? (ANS B)
- D It forms stationary (standing) wave inside the well (T)
- ID The linear momentum of the particle becomes quantised (T)
- III) The minimum energy of the particle inside the well is given by $h^2/8mL^2$ (T)
- IV) The energy of the particle inside the well can take on negative value (F)

А.	I, II, III, IV	B. I, II, III
С.	I, IV	D. III, IV
E.	Non of A, B, C, D	

- 20. Which of the following statements is (are) true regarding pair production and pair annihilation of electron-positron pair? (ANS D)
- D Pair annihilation occurs only above the threshold energy of $2m_ec^2$ (F)
- II) Pair production occurs only above the threshold energy of $2m_ec^2$ (T)
- Energy is always conserved in both IID processes of pair production and pair annihilation (T)
- IV Momentum is always conserved in both processes of pair production and pair annihilation (T)

А.	I, II, III, IV	B. I, II, III
C.	I, IV	D. II, III, IV
Е.	Non of A. B. C. D	

UNIVERSITI SAINS MALAYSIA

Final Exam Academic Session 2004/2005 March 2005

ZCT 104E/3 - Physics IV (Modern Physics) *[Fizik IV (Fizik Moden)]*

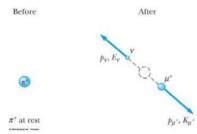
> Duration: 3 hours [Masa: 3 jam]

SESSI 04/05/FINAL

Part A: Objective Instruction: Answer all 40 objective questions in this Part. [Bahagian A: Objektif.] [Arahan: Jawab kesemua 40 soalan objektif dalam Bahagian ini.]

Question 1 - 3 are based on the decay of a π meson into a muon and a massless neutrino shown in the figure below. The mass of the muon is known to be $m_{\mu} = 106 \text{ MeV}/c^2$, and the kinetic energy of the muon is measured to be $K_{\mu} = 4.6 \text{ MeV}$. p_{μ} denotes the momentum of the muon.

[Soalan 1-3 adalah berdasarkan pereputan satu meson π kepada satu muon dan satu neutrino tanpa jisim, sepertimana ditunjukkan dalam gambarajah di bawah. Diketahui jisim muon ialah m_{μ} = 106 MeV/ c^2 , dan tenaga kinetik muon yang terukur ialah K_{μ} = 46 MeV. p_{μ} menandakan momentum muon.]



 How is the momentum of the muon, p_μ related to the kinetic energy of the muon? E_μ denotes the total relativistic energy of muon.

[Bagaimanakah momentum muon p_{μ} dikaitkan dengan tenaga kinetik muon? E_{μ} menandakan tenaga keretatifan muon]

A.
$$p_{\mu}c = \sqrt{\left(K_{\mu} + m_{\mu}c^{2}\right)^{2} - m_{\mu}^{2}c^{4}}$$

B. $p_{\mu} = \sqrt{\left(K_{\mu} + m_{\mu}c^{2}\right)^{2} - m_{\mu}^{2}c^{4}}$
C. $p_{\mu} = \sqrt{2m_{\mu}K_{\mu}}$
D. $p_{\mu}c = \sqrt{\left(E_{\mu}^{2} + m_{\mu}c^{2}\right)^{2}}$

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D] ANS:A. Inspired by Serway and Mosses 2005 edition, pg. 52-53.

2. What is the rest energy of the π meson? [Apakah tenaga rehat meson π ?]

A.
$$K_{\mu} + m_{\mu}c^{2}$$

B. $\left(K_{\mu} + m_{\mu}c^{2}\right) + \sqrt{\left(K_{\mu}^{2} + 2K_{\mu}m_{\mu}c^{2}\right)}$
C. K_{μ}
D. $m_{\nu}c^{2}$

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D] ANS:B, Inspired by Serway and Mosses 2005 edition, pg. 52-53.

3. What is the kinetic energy of the neutrino? [Apakah tenaga kinetik neutrino?]

Α

Please check that the examination paper consists of **XXX** pages of printed material before you begin the examination.

[Sila pastikan bahawa kertas peperiksaan ini mengandungi XXX muka surat yang bercetak sebelum anda memulakan peperiksaan ini.]

Instruction: Answer all questions. Please answer the objective questions from Part A in the objective answer sheet provided. Answer both structured questions from Part B. Please submit the objective answer sheet and the answers to the structured questions separately.

Students are allowed to answer all questions in Bahasa Malaysia or in English.

[<u>Arahan</u>: Jawab **SEMUA** soalan. Sila jawab soalan-soalan objektif daripada bahagian A dalam kertas jawapan objektif yang dibekalkan. Jawab kedua-dua soalan struktur daripada Bahagian B. Hantar kertas jawapan objektif dan jawapan kepada soalan struktur berasingan.]

[Pelajar dibenarkan untuk menjawab samada dalam bahasa Malaysia atau bahasa Inggeris.]

Data

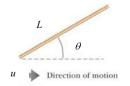
speed of light in free space, $c = 3.00 \times 10^8 \text{ m s}^{-1}$ permeability of free space, $\mu_0 = 4\pi \times 10^{-7} \text{ H m}^{-1}$ permittivity of free space, $\varepsilon_0 = 8.85 \times 10^{-12} \text{ F m}^{-1}$ elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$ Planck constant, $h = 6.63 \times 10^{-34} \text{ J s}$ unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$ rest mass of electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$ rest mass of proton, $m_p = 1.67 \times 10^{-27} \text{ kg}$ molar gas constant, $e = 6.02 \times 10^{-23} \text{ mol}^{-1}$ Avogadro constant, $N_A = 6.02 \times 10^{-31} \text{ N m}^2 \text{ kg}^{-2}$ acceleration of free fall, $g = 9.81 \text{ m s}^{-2}$

C. K_{μ} D. $m_{\mu}c^{2}$ E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D] ANS:A, Inspired by Serway and Mosses 2005 edition, pg. 52-53.

- 4. Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I (T) All inertial frames are equivalent [Semua rangka inersia adalah setara]
 - **II** (T) If light obeys Galilean transformation, light waves would appear stationary in an inertial frame that moves with the same speed with that of the light. [Jika cahaya mematuhi transformasi Galilean, gelombang cahaya akan kelihatan pegun dalam satu rangka inersia yang kelajuannya sama dengan kelajuan cahaya]
 - **III(F)** In an inertial frame moving approximately with the speed of light, light waves would appear stationary according to the postulates of special theory of relativity [Dalam satu rangka inersia yang bergerak dengan kelajuan hampir dengan kelajuan cahaya, gelombang cahaya akan kelihatan pegun mengikut postulat teori kerelatifan khas.]
 - **IV (F)** It is experimentally verified that electromagnetic waves propagate through a medium called Ether [Telah disahkan secara eksperimen bahawa gelombang elektromagnetik merambat melalui satu jenis medium digelar Ether.]

A. II,IIIB. I, II,IIIC. II, III, IVD. I, IIE. Non of A, B, C, D[Jawapan tiada dalam A, B, C, D]ANS:D, my own question

5. A moving rod is observed to have a length of *L* and to be orientated at an angle of $\theta = 45^{\circ}$ with respect to the direction of motion, as shown in the figure below. The rod has a speed of $u = \frac{c}{\sqrt{2}}$. [Suatu rod bergerak diperhatikan mempunyai panjang *L* dan diorientasikan pada suatu sudut $\theta = 45^{\circ}$ merujuk kepada arah gerakannya sepertimana ditunjukkan dalam gambarajah di bawah. Kelajuan rod ialah $u = \frac{c}{\sqrt{2}}$.]



Serway, page 1279, question 23 (modified)

What is the tangent of the angle in the proper frame (in terms of $\tan \theta$)? [Apakah tangen sudutnya (dinyatakan dalam sebutan $\tan \theta$) dalam rangka `proper']

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A. $\tan \theta$ **B.** $\frac{\tan \theta}{\sqrt{2}}$ **C.** $\sqrt{2} \tan \theta$ **D.** $2 \tan \theta$ **E.** Non of A, B, C, D [Jawapan tiada dalam A, B, C, D] **ANS:B**

6. What measurement(s) do two observers in relative motion always agree on? [Apakah ukuran(-ukuran) yang sentiasa disetujui oleh dua orang pemerhati yang berada dalam pergerakan relatif]
I The speed of light c in vacuum [Laju cahaya c dalam vakum]
II The speed v of their relative motion [Laju relatif v di antara mereka]
III The momentum of an object [Momentum suatu objek]

 A. II, III
 B. I, II, IV
 C. II, III, IV
 D. I, II

 E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]
 Serway Q1, pg. 1276
 Solution: B

IV The rest mass of an object [Jisim rehat suatu objek]

7. Given $\{x,t\}$, $\{x',t'\}$ are two sets of coordinates used by two reference frames which are moving with a constant relative velocity, which statement(s) correctly describe(s) the transformation between them?

[Diberi {x,t}, {x',t'} merupakan dua set koordinat yang digunakan oleh dua rangka rujukan yang bergerak dengan halaju relatif mantap, kenyataan yang manakah memerihalkan transformasi di antara dua set koordinat tersebut dengan betul?]

- I {*x*,*t*} is related to {*x*',*t*'} by Galilean transformation at $u \le c$ [{*x*,*t*} dikaitkan dengan {*x*',*t*'} oleh transformasi Galilean pada $u \le c$]
- II {*x*,*t*} is related to {*x*',*t*'} by Galilean transformation at $u \rightarrow c$ [{*x*,*t*} dikaitkan dengan {*x*',*t*'} oleh transformasi Galilean pada $u \rightarrow c$]
- **III** {*x*,*t*} is related to {*x*',*t*'} by Lorentz transformation at $u \le c$ [{*x*,*t*} dikaitkan dengan {*x*',*t*'} oleh transformasi Lorentz pada $u \le c$]
- IV $\{x,t\}$ is related to $\{x',t'\}$ by Lorentz transformation at $u \rightarrow c$ $[\{x,t\}$ dikaitkan dengan $\{x',t'\}$ oleh transformasi Lorentz pada $u \rightarrow c$]

A. I,IIB. I, III,IVC. II, III, IVD. I, IV OnlyE. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]My own questionSolution: B

8. What is the upper limit of the speed of an electron? [Apakah limit atas bagi laju suatu elektron?]
A. m_ec
B. c
C. 0
D. Infinity
E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]
Serway, Q12, pg. 1276
Solution: B

9. The units of the Planck constant *h* are those of: [Unit bagi pemalar Planck *h* adalah sama dengan unit bagi ...]

A. energy B. power C. momentum D. angular momentum E. frequency Solution: D, Chap 38, Q1, RHW 7th ed testbank,

 Rank following electromagnetic radiations according to the energies of their photons, from least to greatest. *Menvusun sinaran elektromagnetik berikut mengikut tenaga foton mereka, daripada yang*

[Menyusun sinarah elekiromagnetik berhali mengikai tenaga joton mereka, daripada ya paling lemah kepada yang paling besar]

1. blue light 2. yellow light 3. x-rays 4. radio waves

A. 1, 2, 3, 4 **B.** 4, 2, 1, 3 **C.** 4, 1, 2, 3 **D.** 3, 2, 1, 4 **E.** 3, 1, 2, 4 **Solution: B, Chap 38, Q9, RHW** 7th ed testbank,

- **11.** In a photoelectric effect experiment the stopping potential is: [Dalam eksperimen kesan fotoelektrik keupayaan penghenti adalah]
 - A. the energy required to remove an electron from the sample [tenaga yang diperlukan untuk menyingkirkan satu elektron daripada sampel]
 - B. the kinetic energy of the most energetic electron ejected [tenaga kenetik bagi elektron terlenting yang paling bertenaga]
 - **C.** the potential energy of the most energetic electron ejected *[tenaga keupayaan bagi elektron terlenting yang paling bertenaga]*
 - D. the photon energy [tenaga foton]

E. the electric potential that causes the electron current to vanish [keupayaan elektrik yang menyebabkan arus elektron hilang]
 Solution: E, Chap 38, Q13, RHW 7th ed testbank,

- 12. In a photoelectric effect experiment no electrons are ejected if the frequency of the incident light is less than A/h, where h is the Planck constant and A is: [Dalam eksperimen kesan fotoelektrik tiada elektron akan terlenting jika frekuensi cahaya tuju adalah kurang daripada A/h, di mana h ialah pamalar Planck dan A ialah:]
 - A. the maximum energy needed to eject the least energetic electron [tenaga maksimum yang diperlukan untuk melentingkan elektron yang paling kurang bertenaga]
 - B. the minimum energy needed to eject the least energetic electron

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[tenaga miminum yang diperlukan untuk melentingkan elektron yang paling kurang bertenaga]

- C. the maximum energy needed to eject the most energetic electron [tenaga maksimum yang diperlukan untuk melentingkan elektron yang paling bertenaga]
- D. the minimum energy needed to eject the most energetic electron [tenaga minimum yang diperlukan untuk melentingkan elektron yang paling bertenaga]

E. the intensity of the incident light [keamatan cahaya tuju]

Solution: D, Chap 38, Q16, RHW 7th ed testbank,

13. Consider the following: [Pertimbangkan yang berikut]

mungkin dalam jarak gelombang adalah]

- I. A photoelectric process in which some emitted electrons have kinetic energy greater than *hf*, where *f* is the frequency of the incident light. [Satu proses fotoelektrik di mana sebahagian elektron terlenting mempunyai tenaga kinetik yang lebih besar daripada hf, di mana f ialah frekuensi cahaya tuju]
- **II.** A photoelectric process in which all emitted electrons have energy less than *hf.* [Satu proses fotoelektrik di mana kesemua elektron terlenting mempunyai tenaga kurang daripada *hf*]
- III. Compton scattering from stationary electrons for which the emitted light has a frequency that is greater than that of the incident light.
 [Penyerakan Compton daripada elektron-elektron rehat yang mana cahaya tertenting mempunyai frekuensi yang lebih besar daripada frekuensi cahaya tuju]
- IV. Compton scattering from stationary electrons for which the emitted light has a frequency that is less than that of the incident light. [Penyerakan Compton daripada elektron-elektron rehat yang mana cahaya tertenting mempunyai frekuensi yang lebih kecil daripada frekuensi cahaya tuju]

The only possible processe(s) is (are) [Proses(-proses) yang mungkin ialah]:

A. I B. III C. I and III D. I and IV E. II and IV Solution: E, Chap 38, Q29, RHW 7th ed testbank (model answer in the testbank is incorrect)

 14. In Compton scattering from stationary electrons the largest change in wavelength that can occur is: [Dalam penyerakan Compton daripada elektron-elektron rehat, perubahan paling besar yang

A. 2.43×10^{-15} m **B.** 2.43×10^{-12} m **C.** 4.9×10^{-12} m **D.** dependent on the frequency of the incident light [bergantung kepada frekuensi cahaya tuju] **E.** dependent on the work function [bergantung kepada fungsi kerja] **Solution: C, Chap 38, Q25, RHW** 7th ed testbank (model answer in the testbank is incorrect)

15. Of the following, Compton scattering from electrons is most easily observed for: [Daripada yang berikut, penyerakan Compton daripada elektron-elektron adalah paling mudah dicerap dalam]

A. microwavesB. infrared lightC. visible lightD. ultraviolet lightE. x raysSolution: E, Chap 38, Q22, RHW 7th ed testbank,

16. In Compton scattering from stationary particles the maximum change in wavelength can be made larger by using: [Dalam penyerkan Compton daripada zarah-zarah rehat, perubahan maksimum dalam jarak gelombang boleh dijadikan lebih besar dengan menggunakan]

A. higher frequency radiation [sinaran yang berfrekuensi lebih tinggi]
B. lower frequency radiation [sinaran yang berfrekuensi lebih rendah]
C. more massive particles [zarah yang berjisim lebih besar]
D. less massive particles [zarah yang berjisim lebih kecil]
E. particles with greater charge [zarah yang casnva lebih besar]

Solution: D, Chap 38, Q21, RHW 7th ed testbank (modified)

17. Evidence for the wave nature of matter is: [Bukti untuk sifat gelombang bagi jasad ialah]

A. Electron diffraction experiments of Davisson and Germer *[eksperimen belauan elektron oleh Davisson dan Germer]*

B. Photoelectric effect [kesan fotoelektrik]

- C. Young's double slit experiment [eksperimen dwi-celah Young]
- D. the Compton effect [kesan Compton]
- E. Frank-Hertz experiment [eksperimen Frank-Hertz]

Solution: A, Chap 38, Q31, RHW 7th ed testbank,

18. Monoenergetic electrons are incident on a single slit barrier. If the energy of each incident electron is increased the central maximum of the diffraction pattern: [Elektron monotenaga ditujukan pada satu sawar celah tunggal. Jika tenaga setiap elektron tuju dinaikkan, maka maksimum pusat corak belauan]

A. widens [dilebarkan] B. narrows [disempitkan]

C. stays the same width [kelebaran tetap tak berubah]

D. widens for slow electrons and narrows for fast electrons [dilebarkan untuk elektron yang lambat dan disempitkan untuk elektron yang pantas]

E. narrows for slow electrons and widens for fast electrons

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[disempitkan untuk elektron yang lambat dan dilebarkan untuk elektron yang pantas]

Solution: B, Chap 38, Q34, RHW 7th ed testbank,

- Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I (T) An ideal blackbody absorbs all of the light that is incident on it. [Jasad hitam yang ideal menyerap kesemua cahaya yang tertuju padanya]
 - II (F) The distribution of energy in the blackbody radiation depends upon the material from which the blackbody is constructed. [Taburan tenaga dalam pancaran jasad hitam bergantung kepada jenis bahan yang membentuk dinding jasad hitam]
 - **III(T)** A blackbody is a perfect emitter of the radiation it generates. [Jasad hitam adalah pemancar pancaran yang sempurna.]
 - **IV (T)** The energy of an ultraviolet photon is more than the energy of an infrared photon. [Tenaga suatu foton ultraungu adalah lebih tinggi daripada tenaga bagi suatu foton inframerah]

 A. III, IV
 B. I, II, III
 C. I, III, IV
 D. I, III

 E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]
 Image: Comparison of the second second

Solution: C I: testgen Physics 2 by Walker, Q1, Walker Chap 30 II: testgen Physics 2 by Walker, Q2, Walker Chap 30 III: testgen Physics 2 by Walker, Q11, Walker Chap 30 IV: testgen Physics 2 by Walker, Q12, Walker Chap 30

20. If the wavelength of a photon is doubled, what happens to its energy? [Jika jarak gelombang digandakan dua kali, apa yang akan berlaku ke atas tenaganya?]

A. It is halved. *[ia diseparuhkan]*B. It stays the same. *[tetap tak berubah]*C. It is doubled. *[ia digandaduakan]*D. It is quadrupled. *[ia digandakan 4 kali]*E. Non of A, B, C, D *[Jawapan tiada dalam A, B, C, D]*

ANS: A, testgen Physics 2 by Walker, Q24, Walker Chap 30

Light of a given wavelength is used to illuminate the surface of a metal, however, no
photoelectrons are emitted. In order to cause electrons to be ejected from the surface of this
metal you should

[Cahaya dengan jarak gelombang tertentu digunakan untuk memancari permukaan satu logam, tapi tiada fotoelektron yang terlentingkan. Unutk menlentingkan elektron daripada permukaan logam tersebut anda kena]

A. use light of a longer wavelength.

[menggunakan cahaya yang berjarak gelombang lebih panjang]

B. use light of a shorter wavelength. [menggunakan cahaya yang berjarak gelombang lebih pendek]
C. use light of the same wavelength but increase its intensity. [menggunakan cahaya yang berjarak gelombang sama tapi menambahkan keamatannya]

D. use light of the same wavelength but decrease its intensity. [menggunakan cahaya yang berjarak gelombang sama tapi mengurangkan keamatannya]

E. Non of A, B, C, D *[Jawapan tiada dalam A, B, C, D]* ANS: B, testgen Physics 2 by Walker, Q35, Walker Chap 30

22. Protons are being accelerated in a particle accelerator at sub-relativistic energies. When the energy of the protons is doubled, their de Broglie wavelength will [Proton dipecutkan dalam satu pemecut zarah pada tenaga sub-kerelatifan. Bila tenaga proton digandaduakan, jarak gelombang de Broglienya akan]

A. increase by a factor of 2. [bertambah dengan satu factor 2] B. decrease by a factor of 2. [berkurang dengan satu factor 2] C. increase by a factor of $\sqrt{2}$. [bertambah dengan satu factor $\sqrt{2}$] D. decrease by a factor of $\sqrt{2}$. [berkurang dengan satu factor $\sqrt{2}$] E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: D, testgen Physics 2 by Walker, Q64, Walker Chap 30

23. A proton and an electron are both accelerated to the same final speed. If λ_p is the de Broglie wavelength of the proton and λ_e is the de Broglie wavelength of the electron, then [Kedua-dua proton dan elektron dipecutkan kepada laju akhir yang sama. Jika λ_p ialah jarak gelombang de Broglie proton dan λ_e ialah jarak gelombang de Broglie elektron maka]

A. $\lambda_p > \lambda_e$. **B.** $\lambda_p = \lambda_e$. **C.** $\lambda_p < \lambda_e$. **D.** Not enough data to answer this question. *[tak cukup data untuk menjawab soalan ini]* **E.** Non of A, B, C, D *[Jawapan tiada dalam A, B, C, D]* **ANS: C, testgen Physics 2 by Walker, Q67, Walker Chap 30**

24. If the position of an electron is measured very precisely there is an uncertainty in measuring its [Jika kedudukan suatu elektron diukur dengan sangat tepat maka akan wujud ketidakpastian dalam pengukuran ...nya]

A. rest mass.	B. momentum.	C. potential energy.
D. charge.	E. Non of A, B, C, D	[Jawapan tiada dalam A, B, C, D]

ANS: B, testgen Physics 2 by Walker, Q71, Walker Chap 30

25. Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]

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- I (T) A zero value for the Planck's constant would mean that the laws of classical physics would apply to quantum physics. [Jika pemalar Planck bernilai sifar ini bermakna hukum-hukum fizik klasik akan teraplikasikan dalam fizik kuantum]
- II (T) In quantum tunneling, electrons and other quantum particles can tunnel through a region of space that would be forbidden to them if they were classical particles. [Dalam penerowongan kuantum, elektron dan zarah-zarah kuantum lain boleh menerowongi satu rantau yang terlarang bagi mereka yang merupakan zarah-zarah klasikal.]
- III(F) A large value for the Planck's constant would mean that the laws of classical physics would apply to quantum physics. [Jika pemalar Planck bernilai besar ini bermakna hukum-hukum fizik klasik akan teraplikasikan dalam fizik kuantum]

A. III B. II, III C. I D. I, II E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D] Solution: D I,II: testgen Physics 2 by Walker, Q72, Walker II: testgen Physics 2 by Walker, Q73, Walker

26. A major advantage of an electron microscope over a visible light microscope is that the electron microscope

[Manfaat yang major bagi satu mikroskop elektron berbanding dengan mikroskop cahaya nampak ialah bahawa mikroskop elektron]

A. has much greater magnification. [memberikan pembesaran yang lebih tinggi]
B. operates with much lower intensity. [beroperasi pada keataman yang lebih rendah]
C. can penetrate opaque samples. [boleh menembusi sampel legap]
D. can have much better resolution. [memberikan leraian yang lebih baik]
E. requires no lenses for its operation. [tidak memerlukan kanta-kanta dalam operasinya]

ANS: D, testgen Physics 2 by Young and Freeman, Q27, Chap 39

27. An important observation that led Bohr to formulate his model of the hydrogen atom was the fact that

[Salah satu pencerapan yang merangsangkan Bohr memformulasikan model atom hidrogennya ialah fakta bahawa]

- A. a low density gas emitted a series of sharp spectral lines. [gas berketumpatan rendah memancarkan pinggir-pinggir spectrum yang tajam]
- **B.** neutrons formed a diffraction pattern when scattered from a nickel crystal. *[neutron membentuk corak belauan bila diserakkan daripada hablur nickel]*
- C. electrons were found to have a wave nature. [elektron didapti mempunyai sifat gelombang]

- **D.** the peak of the blackbody radiation moved to shorter wavelengths as the temperature was increased.
- [puncak jasad hitam bergerak menghampiri jarak gelombang yang lebih pendek bila suhu bertambah]
- E. the emission of light by an atom does not appear to conserve energy. [pancanran cahaya oleh atom tidak mengabadikan tenaga]
 ANS: A, testgen Physics 2 by Young and Freeman, Q40, Chap 39
- 28. The particle nature of light is best illustrated by which of the following? [Sifat zarah cayaha adalah paling baik diilustrasikan oleh yang mana berikut?]
 - A. The scattering of alpha particles from gold foil. [Serakan zarah alfa daripada foil emas]

B. The fact that hot objects emit electromagnetic radiation. [Fakta bahawa objek panas memancarkan pancaran elektromagnetik]

- C. The diffraction pattern observed when a beam of electrons is scattered by a crystal [Corak belauan yang dicerap bila satu bim elektron diserakkan oleh satu hablur]
- **D.** The fact that a rainbow consists of a continuous spectrum of colors *[Fakta bahawa pelangi mengandungi satu spektrum warna yang selanjar]*
- E. The ejection of electrons from a metal surface illuminated by light. [Pelentingan elektron daripada permukaan logam yang disinari cahaya]
 ANS: E, testgen Physics 2 by Young and Freeman, Q18, Chap 38
- 29. A wave function is given by

[Satu fungsi gelombang diberikan oleh] $\Psi(x) = 0$ for x < 0 $\Psi(x) = Ax$ for $0 \le x \le L$ $\Psi(x) = 0$ for x > L

The product of the normalization constant A and the quantity $L^{3/2}$ is equal to: [Hasildarab pemalar normalisasi A dengan kuantiti $L^{3/2}$ bersamaan dengan]

A. $\sqrt{12}$ **B.** $\sqrt{15}$ **C.** $\sqrt{20}$ **D.** $\sqrt{24}$ **E.** $\sqrt{3}$

ANS: E, testgen Physics 2 by Young and Freeman , Q1, Chap 40, modified

30. If a wave function ψ for a particle moving along the x axis is "normalized" then: [Jika satu funsi gelombang ψ untuk satu zarah yang bergerak sepanjang paksi x adalah ternormalisasikan, maka

A. $\int |\psi|^2 dt = 1$ **B.** $\int |\psi|^2 dx = 1$ **C.** $\partial \psi / \partial x = 1$ **D.** $\partial \psi / \partial t = 1$ **E.** $|\psi|^2 = 1$

Solution: B, Chap 39, Q1, RHW 7th ed testbank,

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31. The energy of an electron in a hydrogen atom that is about to get ionised is *[Tenaga elektron dalam atom hidrogen yang hampir-hampir diionkan adalah]*

A. -13.6 eV	B. -3.4 eV	C. -10.2 eV
D. -1.0 eV	E. 0 eV	

Solution: E, Chap 39, Q26, RHW 7th ed testbank, modified.

32. According to the Bohr model of hydrogen atom, the energy E_n of a hydrogen atom of a state with quantum number *n* is proportional to: [Mengikut model hidrogen Bohr tenaga E_n suatu atom hidrogen pada keadaan dengan nombor kuantum n adalah berkadaran dengan]

A. n **B.** n^2 **C.** 1/n **D.** $1/n^2$

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

Solution: D, Chap 39, Q25, RHW 7th ed testbank,

33. The series limit for the Balmer series represents a transition $m \rightarrow n$, where (m, n) is [Limit siri bagi siri Balmer mewakili satu peralihan $m \rightarrow n$, di mana (m, n) ialah]

	A. (2,1)	B. (3,2)	C. (∞,0)	D. (∞,1)	E. (∞,2)
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Solution: E, Chap 39, Q33, RHW 7th ed testbank,

34. The location of a particle is measured and specified as being exactly at x = 0, with *zero* uncertainty in the *x* direction. How does this affect the uncertainty of its velocity component in the *y* direction?

[Lokasi suatu zarah adalah diukur dan dispesifikasikan sebagai tepat-tapat pada x = 0 dengan ketidakpastian sifar dalam arah x. Bagaimanakah keadaan ini mempengaruhi ketidakpastian komponen halajunya dalam arah y?]

A. It does not affect it. [Keadaan ini tidak mempengaruhinya]
B. It makes it infinite. [Keadaan ini menjadikannya infinit]
C. It makes it zero. [Keadaan ini menjadikannya sifar]
D. It makes it negative [Keadaan ini menjadikannya negatif]
E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]
Ans: A, QQ serway 40.10

- **35.** The Balmer series of hydrogen is important because it: *[Siri Balmer bagi hidrogen adalah penting kerana ia]*
 - A. is the only one for which the Bohr theory can be used [merupakan satu-satunya siri yang dapat diaplikasikan oleh teori Bohr]

- B. is the only series which occurs for hydrogen [merupakan satu-satunya siri yang berlaku dalam hidrogen]
- C. is in the visible region [berada dalam rantau nampak]
- **D.** involves the lowest possible quantum number *n* [melibatkan numbor kuantum yang terendah mungkin]
- **E.** involves the highest possible quantum number *n* [melibatkan numbor kuantum yang tertinggi mungkin]

Solution: C, Chap 39, Q34, RHW 7th ed testbank,

- 36. The quantization of energy, E = nhf, is not important for an ordinary pendulum because: [Pengkuantuman tenaga, E = nhf, adalah tidak penting bagi suatu bandul kerana]
 - A. the formula applies only to mass-spring oscillators [formular hanya teraplikasikan ke atas pengayun jisim-spring]
 - **B.** the allowed energy levels are too closely spaced *[selang paras tenaga diizinkan adalah terlalu padat]*
 - C. the allowed energy levels are too widely spaced [selang paras tenaga diizinkan adalah terlalu lebar]
 - **D.** the formula applies only to atoms *[formular hanya teraplikasikan ke atas atom]*
 - E. the value of h for a pendulum is too large [nilai h bagi bandul terlalu besar]
 Solution: B, Chap 38, Q3, RHW 7th ed testbank,
- **37.** A hydrogen atom is in its ground state. Incident on the atom are many photons each having an energy of 5 eV. The result is that *[Suatu atom hidrogen berada dalam keadaan buminya. Foton-foton bertenaga 5 eV setiap satu ditujukan pada atom itu. Hasilnya ialah]*
 - A. the atom is excited to a higher allowed state [atom teruja kepada keadaan dizinkan yang lebih tinggi]
 - **B.** the atom is ionized *[atom diionkan]*
 - **C.** the photons pass by the atom without interaction *[foton merentasi atom tanpa berinteraksi]*

D. the photons are ionised

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[foton diionkan]

E. the atom is de-excited to a lower quantum state [atom ternyah-uja kepada keadaan dizinkan yang lebih rendah]
ANS (C), Serway, qq 42.1, pg. 1360. Because the energy of 5 eV does not correspond to raising the atom from the ground state to an allowed excited state, there is no interaction between the photon and the atom (modified)

38. A hydrogen atom makes a transition from the n = 3 level to the n = 2 level. It then makes a transition from the n = 2 level to the n = 1 level. Which transition results in emission of the longest-wavelength photon?
[Satu atom hidrogen melakukan peralihan dari paras n=3 ke paras n=2. Kemudiannya ia

melakukan satu peralihan dari paras n=2 ke paras n=3 ke paras n=2. Kemudulinya ta melakukan satu peralihan dari paras n=2 ke paras n=1. Peralihan yang manakan menghasilkan pancaran foton berjarak gelombang paling panjang?]

A. the first transition *[peralihan pertama]* B. the second transition *[peralihan kedua]*

C. neither, because the wavelengths are the same for both transitions. *[bukan A ataupun B kerana jarak gelombang kedua-dua kes adalah sama]*

D. one cannot determine the answer because data provided is not sufficient. *[jawapan tidak boleh ditentukan kerana data yang diberikan tak cukup]*

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS (A), Serway, qq 42.3, pg. 1360. The longest-wavelength photon is associated with the lowest energy transition, which is n = 3 to n = 2.

39. An electron and a proton are accelerated to a common relativistic energy (i.e. $E \gg m_e c^2$, $m_p c^2$), where m_e and m_p denote the masses of the electron and proton respectively. Determine the ratio of the de Broglie wavelength of the electron to that of the proton. [Satu elektron dan proton dipecutkan kepada satu tenaga kerelatifan E yang sama, (iaitu $E \gg m_e c^2$, $m_p c^2$), di mana m_e dan m_p menandakan jisim elektron dan proton masing-masing. Tentukan nisbah jarak gelombang de Broglie elektron kepada proton.]

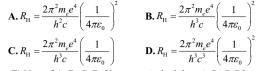
(A)
$$\frac{m_p}{m_e}$$
 (B) $\sqrt{\frac{m_p}{m_e}}$ (C) $\sqrt{\frac{m_e}{m_p}}$ (D) $\frac{m_p}{m_e}$

(E) 1

ANS (E), My own question, pg. 897.

40. How is the empirical Ryberg constant, $R_{\rm H}$, be related to the other constants of nature in the Bohr model of hydrogen atom?

[Bagaimanakah pemalar empirikal Ryberg R_H dikaitkan kepada pemalar-pemalar alam yang lain mengikut model Bohr atom hidrogen?]



(E) Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS (B), Cutnell and Johnson, pg. 910.

Part B: Structured Questions [60 marks] Instruction: Answer both questions 1 and 2 in this Part.

[Bahagian B: Soalan Struktur. 60 markah] [Arahan: Jawab kedua-dua soalan 1 dan 2 dalam Bahagian ini.]

1(a) Consider the Gedanken experiment of a moving train (the O' frame) passing by an observer called Doraemon on the ground (the O frame) with a speed of v, see figure below. The length of the train, as measured by Doraemon, is *L*. Another observer, Doraemiyan is seen by Doraemon to sit at the middle of the train, *L*/2, when Doraemiyan passes by Doraemon at time *t*=0. At that instance, two lightning bolts strike points A and B at the edges of the train such that both events appear to occur simultaneously according to Doraemiyan, *t_A* - *t_B*, as seen by Doraemon, where both *t*'s are measured in Doraemon's frame. Express your answer in terms of v, *L*, and the speed of light *c*. [*Hint: Do you think you should apply time-dilation or length contraction formulae here?*]

[Pertimbangkan eksperimen Gedanken di mana satu tren (rangka O') bergerak melepasi seorang pemerhati Doraemon yang berada di atas bumi (rangka O) dengan laju v, rujuk gambarajah di bawah. Panjang tren sebagaimana yang diukur oleh Doeaemon ialah L. Seorang lagi pemerhati, Doraemiyan diperhatikan oleh Doraemon sebagai duduk di tengahtengah tren, L/2, bila Doraemiyan bergerak melepasi Doraemon pada masa t = 0. Pada ketika itu, dua petir menyambar titik-titik A dan B pada pinggir tren sedemikian rupa supaya keduadua peristiwa itu kelihatan berlaku secara serentak kepada Doraemon. Apakah masa susulan di antara cahaya dari peristiwa A dan peristiwa B yang sampai kepada Doraemiyan, $t_A - t_B$, mengikut Doraemon? Kedua-dua masa t_A , t_B adalah diukur dalam rangka Doraemon. Nyatakan jawapan anda dalam sebutan v, L dan laju cahaya c. [Hint: Adakah anda perlu mengaplikasikan formular-formular pendilatan-masa dan susutan panjang?]

A O frame

[10 marks]

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By the time $t_{\rm B}$, light from event B hits Doramiyan. Since then she has moved for a distance of $vt_{\rm B}$ to the right from Doramon. Hence, light from B fulfils the relation $ct_{\rm B} = L/2 - vt_{\rm B}$.

Likewise, by the time $t_A (> t_B)$ light from A hits Doramiyan. Since then she has moved for a distance of vt_A to the right from Doramon. Hence, light from A fulfils the relation $ct_A = L/2 + vt_A$.

 $t_{\rm B} = L/2(c+v); t_{\rm A} = L/2(c-v)$ $\Rightarrow t_{\rm A} - t_{\rm B} = L/2(c-v) - L/2(c+v) = (uL)/(c^2-v^2)$

[10 marks]

1(b) When a photoelectric surface is illuminated with light of wavelength 437 nm, the stopping potential is 1.67 V.

[Bila satu permukaan fotoelektrik disinari cahaya berjarak gelombang 437 nm, keupayaan penghenti ialah]

[5 + 5 marks]

- (i) What is the work function of the metal in eV? [Apakah fungsi kerja logam tersebut dalam unit eV?]
- (*ii*) What is the maximum speed of the ejected electrons? [Apakah laju maksimum elektron terlenting?]

Solution:

(i) $W_0 = hc/\lambda - K_{\text{max}} = 1240 \text{ nm.eV}/437 \text{ nm} - 1.67 \text{ eV} = 1.17 \text{ eV}$ (ii) $K_{\text{max}} = mv^2/2 \Rightarrow v^2 = (2K_{\text{max}} / m)^{1/2} = (2 \times 1.67 \text{ e J} / 9.11 \times 10^{-31} \text{ kg})^{1/2} = 7.66 \times 10^5 \text{ m/s}$

ANS: testgen Physics 2 by Young and Freeman, Q2.4, Chap 38

1(c) An electron has a speed of 0.95*c*. What is the the magnitude of its momentum? [5 marks] [Suatu elektron berlaju 0.95*c*. Apakah magnitud momentumnya?]

Solution:

 $\gamma = 1/\sqrt{1 - 0.95^2} = 3.20$ $p = m\gamma u = 9.1 \times 10^{-31} \times 3.2 \times (0.95 \times 3 \times 10^8) \text{Ns} = 8.3 \times 10^{-22} \text{Ns}$

Chap 37, Q54, RHW 7th ed testbank,

1(d) A 29.0 pm photon is Compton scattered by a stationary electron. What is the maximum energy loss of the photon? [Satu foton 29.0 pm diserak Compton oleh satu elektron pegun. Apakah kehilangan tenaga foton yang maksimum?]

[5 marks]



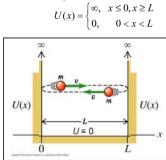
Solution:

Maximal kinetic energy loss of the photon occurs when

$$\Delta \lambda = \Delta \lambda_{\max} = 2\lambda_c = \frac{2hc}{m_c c^2} = \frac{2 \times (1240 \text{keV} \cdot \text{pm})}{522 \text{keV}} = 4.75 \text{pm}$$
$$\Delta E_{\max} = \frac{hc}{\lambda} - \frac{hc}{\lambda_{\max}} = hc \left(\frac{1}{\lambda} - \frac{1}{\lambda + \Delta \lambda_{\max}}\right)$$
$$= (1240 \text{keV} \cdot \text{pm}) \left(\frac{1}{29 \text{pm}} - \frac{1}{29 \text{pm} + 4.75 \text{pm}}\right) = 6.01 \text{ keV}$$

ANS: testgen Physics 2 by Young and Freeman , Q1.12, Chap 38 (Model answer may be incorrect)

2(a) Consider a quantum particle trapped in an infinite quantum well (with width *L*) given by [*Pertimbangkan satu zarah kuantum yang terperangkap dalam satu telaga kuantum infinit (dengan lebar L) yang diberikan oleh*]



The behaviour of a particle inside the infinite well [i.e. the region where U(x) = 0 for 0 < x < L] is governed by the 1-D time-independent Schrodinger equation $\frac{\partial^2 \psi(x)}{\partial x^2} = -B^2 \psi(x)$, where $B^2 = \frac{2mE}{\hbar^2}$. *E* is the energy of the particle. [Kelakuan zarah dalam telaga infinit (iaitu dalam rantau U(x) = 0 for 0 < x < L) diperintah oleh persamaan merdeka-masa Schrodinger 1-D $\frac{\partial^2 \psi(x)}{\partial x^2} = -B^2 \psi(x)$, di mana $B^2 = \frac{2mE}{\hbar^2}$. *E*



(i) Show that ψ(x) = A sin Bx + C cos Bx is a solution to the Schrodinger equation for the particle inside the well, where A, C are some constants.
 [Tunjukkan bahawa ψ(x) = A sin Bx + C cos Bx merupakan penyelesaian kepada persamaan Schrodinger untuk zarah dalam telaga, di mana A dan C adalah pemalar.]

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Solution: Plug
$$\psi(x) = A \sin Bx + C \cos Bx$$
 into the LHS of $\frac{\partial^2 \psi(x)}{\partial x^2} = -B^2 \psi(x)$:
 $\frac{\partial^2 \psi(x)}{\partial x^2} = \frac{\partial^2}{\partial x^2} [A \sin Bx + C \cos Bx] = \frac{\partial}{\partial x} [BA \cos Bx - BC \sin Bx]$
 $= -B^2 A \sin Bx - B^2 C \cos Bx = -B^2 [A \sin Bx + C \cos Bx]$
 $= -B^2 \psi(x) = \text{RHS of the Schroginger equation}$

 (ii) Determine the values of C and B by applying boundary conditions that must be fulfilled by the Schrodinger equation governing the particle.
 [Tentukan nilai-nilai C dan B dengan mengaplikasikan syarat-syarat sempadan yang mesti dipenuhi oleh persamaan Schrodinger yang memerintah zarah itu.]

[4 + 6 marks]

Solution:

Boundary condition (1) Plug $\psi(x = 0) = 0$ into $\psi = AsinBx + CcosBx$, we obtain $\psi(x=0) = 0 = Asin 0 + C cos 0 = C$, i.e. C = 0

[4 marks]

Hence the solution is reduced to $\psi = AsinB$ Next we apply the second boundary condition: $\psi(x = L) = 0 = Asin(BL)$ Only either A or sin(BL) must be zero but not both; A cannot be zero This means it must be sinBL = 0, or in other words $B = n \pi/L \equiv B_n$, $n = 1, 2, 3, \cdots$

[6 marks]

 (iii) Hence show that the energy of the particle in the infinite well is quantized. [Seterusnya tunjukkan bahawa tenaga zarah dalam telaga infinit adalah terkuantumkan]
 [5 marks]

Solution

B

$$\sum_{n=1}^{n} = \frac{2mE_n}{\hbar^2} = \frac{n^2\pi^2}{L^2} \Longrightarrow E_n = \frac{n^2\pi^2\hbar^2}{2mL^2}, n = 1, 2, 3...$$
 [5 marks]

2(b) What is the kinetic energy of an electron at the ground state of the hydrogen atom, given that the ground state energy of the hydrogen atom is -13.6 eV? Give your answer in unit of eV. [Apakah tenaga kinetik elektron pada keadaan bumi atom hidrogen? Diberitahu tenaga bumi atom hidrogen ialah -13.6 eV. Berikan jawapan anda dalam unit eV.]

[10 marks]

Solution: Serway and Moses, Problem 22

From the requirement that the centripetal force comes from the electrostatic force
$$\frac{mv_0^2}{r_0} = \frac{ke^2}{r_0^2}$$
,
[1 marks]

the kinetic energy of the ground state electron can be written as
$$K_0 = \frac{mv_0^2}{2} = \left(\frac{1}{2}\right)\frac{ke^2}{r_0}$$
.

[2 marks]

This gives $K_0 = \frac{ke^2}{2r_0} = 13.6 \text{ eV}$

Potential energy of the electron at ground state is $U_0 = -\frac{ke^2}{r_0}$.

[1 marks]

Hence ground state energy is $E_0 = K_0 + U_0 = \left(\frac{1}{2}\right)\frac{ke^2}{r_0} - \frac{ke^2}{r_0} = -\frac{ke^2}{2r_0} = -13.6 \text{ eV}$.

[3 marks]

[3 marks]

UNIVERSITI SAINS MALAYSIA

KSCP Academic Session 2004/2005

ZCT 104E/3 - Physics IV (Modern Physics) [Fizik IV (Fizik Moden)]

> Duration: 3 hours [Masa: 3 jam]

Please check that the examination paper consists of XXX pages of printed material before you begin the examination.

[Sila pastikan bahawa kertas peperiksaan ini mengandungi XXX muka surat yang bercetak sebelum anda memulakan peperiksaan ini.]

Instruction: Answer all questions. Please answer the objective questions from Part A in the objective answer sheet provided. Answer ALL structured questions from Part B. Please submit the objective answer sheet and the answers to the structured questions separately.

Students are allowed to answer all questions in Bahasa Malaysia or in English.

[Arahan: Jawab SEMUA soalan. Sila jawab soalan-soalan objektif daripada bahagian A dalam kertas jawapan objektif yang dibekalkan. Jawab kesemua soalan struktur daripada Bahagian B. Hantar kertas jawapan objektif dan jawapan kepada soalan struktur berasingan.]

[Pelaiar dibenarkan untuk menjawab samada dalam bahasa Malavsia atau bahasa Inggeris.]

Data

speed of light in free space, $c = 3.00 \text{ x} 10^8 \text{ m s}^{-1}$ permeability of free space, $\mu_0 = 4\pi \times 10^{-7} \text{ H m}^{-1}$ permittivity of free space, $\varepsilon_0 = 8.85 \text{ x } 10^{-12} \text{ F m}^{-1}$ elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$ Planck constant, $h = 6.63 \times 10^{-34} \text{ J s}$ unified atomic mass constant, $u = 1.66 \ge 10^{-27} \text{ kg}$ rest mass of electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$ rest mass of proton, $m_p = 1.67 \text{ x } 10^{-27} \text{ kg}$ molar gas constant, = 8.31 J K⁻¹ mol⁻¹ Avogadro constant, $N_{\rm A} = 6.02 \text{ x } 10^{23} \text{ mol}^{-1}$ gravitational constant, $G = 6.67 \text{ x } 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$ acceleration of free fall, $g = 9.81 \text{ m s}^{-2}$

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Part A: Objective 25 marks

Instruction: Answer all 25 objective questions in this Part. *[Bahagian A: Objektif.]*

[Arahan: Jawab kesemua 25 soalan objektif dalam Bahagian ini.]

ANS: A, Young and Freeman study guide, pg 271

I. A massive particle has a speed of 0.95*c*. Can its energy and speed be increased by more than 500%?

[Laju suatu zarah yang berjisim ialah 0.95c. Bolehkah tenaga dan lajunya bertambah sebanyak 500%?]

A. The energy can but not the speed

- **B.** The speed can but not the energy
- **C.** Both the energy and speed can be increased by this amount
- **D.** Both the energy and speed cannot be increased by this amount
- E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: A, Modified from Young and Freeman study guide, pg 271

2. Consider a photon travelling in vacuum. Can its energy and speed be increased by more than 500%?

[Pertimbangkan suatu foton yang bergerak di dalam vakuum. Bolehkah tenaga dan lajunya bertambah sebanyak 500%?]

- **A.** The energy can but not the speed
- **B.** The speed can but not the energy
- C. Both the energy and speed can be increased by this amount
- **D.** Both the energy and speed cannot be increased by this amount
- E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: B, Modified from Young and Freeman study guide, pg 271, Example 1

3. Constancy of the speed of light in all inertial reference systems implies that *[Kemantapan laju cahaya dalam semua rangka rujukan inersia mengimplikasikan]*

A $x^{2} + y^{2} + z^{2} + c^{2}t^{2} = x'^{2} + y'^{2} + z'^{2} + c^{2}t'^{2}$

B. $x^2 + y^2 + z^2 - c^2 t^2 = x'^2 + y'^2 + z'^2 - c^2 t'^2$

C. x + y + z - ct = x' + y' + z' - ct'

D. x + y + z + ct = x' + y' + z' + ct'

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: C, Modified from Young and Freeman study guide, pg 280, Example 9

4. If a neutron spontaneously decays into a proton, an electron and a neutrino (which is massless), the decay products are observed to have a total kinetic energy of E_k . If the proton mass is M_P and the electron mass is m_e how large is the neutron mass?

[Jika suatu neutron mereput kepada satu proton, satu elektron dan satu neutrino (yang tak berjisim) secara spontan, jumlah tenaga kinetik hasil reputannya dicerap sebagai E_k . Jika jisim proton ialah M_P dan jisim elektron ialah m_e apakah jisim neutron?]

A.
$$(M_P + m_e) - \frac{E_k}{c^2}$$
 B. $\frac{E_k}{c^2} - (M_P + m_e)$ C. $M_P + m_e + \frac{E_k}{c^2}$

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D.
$$\sqrt{\left(M_P + m_e\right)^2 + \left(\frac{E_k}{c^2}\right)^2}$$

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: B, Cutnell, page 1271, QQ 39.10

5. The following pairs of energies represent the rest energy and total energy of three different particles: particle 1: *E*, 2*E*; particle 2: *E*, 3*E*; particle 3: 2*E*, 4*E*. Rank the particles according to their speed.

[Pasangan tenaga berikut mewakili tenaga rehat dan jumlah tenaga bagi tiga zarah yang berbeza: zarah 1: E, 2E; zarah 2: E, 3E; zarah 3: 2E, 4E. Aturkan zarah-zarah tersebut mengikut laju mereka.]

A. $v_3 > v_2 = v_1$ **B.** $v_2 > v_3 = v_1$ **C.** $v_1 > v_2 = v_3$
D. $v_3 > v_2 > v_1$ **E.** Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: A, Modified from Walker Test Item, pg 629, Q28

6. Observer A sees a pendulum oscillating back and forth in a relativistic train and measures its period to be *T_A*. Observer B moves together with the train and measures the period of the pendulum to be *T_B*. These two results will be such that [*Tempoh suatu bandul yang mengayun berulang-alik di dalam suatu keretapi kerelatifan diukur sebagai T_A oleh pemerhati A. Manakala pemerhati B yang gerak bersama dengan keretapi tersebut mengukur tempoh bandul tersebut sebagai <i>T_B*. Keputusan pengukuran tempoh-tempoh

tersebut mengukur tempoh bandul tersebut sebagai T_B . Keputusan pengukuran tempoh-tempoh tersebut adalah]

A. $T_A > T_B$ **B.** $T_A = T_B$ **C.** $T_A < T_B$ **D.** T_A could be greater or smaller than T_B depending on the direction of the motion **E.** Non of A, B, C, D *[Jawapan tiada dalam A, B, C, D]*

ANS: D, Walker Test Item, pg 642, Q1,Q2,Q4, Tutorial 2 Problems 1.

- 7. Which of the following statements are (is) correct? [Pilih kenyataan(-kenyataan) yang benar daripada yang berikut]
 - **I(T)** An ideal blackbody absorbs all of the light that is incident on it. [Jasad hitam yang ideal menyerap kesemua cahaya yang jatuh ke atasnya]
 - **II(T)** The distribution of energy in the blackbody radiation does not depends upon the material from which the blackbody is constructed. *[Taburan tenaga dalam pancaran jasad hitam tidak bergantung kepada jenis bahan yang membentuk jasad hitam itu.]*
 - **III(F)** The correct expression for the energy of a photon is $E = h\lambda$ [*Ekspresi yang betul bagi tenaga suatu foton ialah* $E = h\lambda$]
 - IV(T) For a blackbody, the total intensity of energy radiated over all wavelengths increases as the forth power of the temperature. [Bagi satu jasad hitam, keamatan tenaga yang dipancarkan bila sumbangan kesemua jarak gelombang dijumlahkan bertambah mengikut kuasa empat suhunya.]

A. I,II,III B. I,II C. II, III, IV D. I,II,IV

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

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ANS: E, Young and Freeman study guide, page 286, Question

8. Which of the following statements are (is) correct?

[Pilih kenyataan(-kenyataan) yang benar daripada yang berikut]

- **I(T)** In the Compton Effect, there is a zero wavelength shift for forward scattering $(\theta = 0^{\circ})$ [Dalam kesan Compton, anjakan jarak gelombang sifar berlaku dalam serakan ke depan $(\theta = 0^{\circ})$]
- **II** (**T**) In the Compton Effect, no energy or momentum is transferred to the electron in the forward scattering.

[Dalam kesan Compton, tiada tenaga atau momentum dipindahkan kepada elektron dalam serakan ke depan.]

- III(T) In the Compton Effect, conservation of momentum and energy must be simultaneously satisfied. [Dalam kesan Compton, keabadian tenaga dan momentum mesti dipatuhi secara serentak.]
- IV(T) In the Compton Effect, energy and momentum are transferred to the scattered electron when θ is non zero. [Dalam kesan Compton, tenaga dan momentum dipindahkan kepada elektron terserakkan jika sudut θ bukan sifar.]

A. I,II,III B. I,II C. II, III, IV D. I,II,IV

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: B, Walker Test Item, page 646, Q25, own suggested options

9. Which of the following statements are (is) correct?

[Pilih kenyataan(-kenyataan) yang benar daripada yang berikut]

- I(F) A photon is a particle with positive charge [Foton adalah zarah yang bercas positif]
- **II (F)** A photon's mass is not necessarily zero [Jisim foton tidak semestinya sifar]
- **III(F)** Photon always move with a speed of *c* irrespective of the medium through which it is moving [*Tidak kisah medium apa yang dilaluinya, foton sentiasa bergerak dengan laju c*]
- **IV(T)** The number of photons per unit cross sectional area in a beam of light is proportional to the intensity of the light beam. [Nombor foton per unit keratan rentas dalam satu alur cahaya adalah berkadaran dengan keamatan alur cahaya itu.]

A. I,II,III B. IV C. II, III, IV D. I,II,IV

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: A, Walker Test Item, page 648, Q30

10. In photoelectric effect, which one of the following is the correct expression for the cut-off frequency of the metal in terms of its work function, W_0 ?

[Dalam kesan fotoelektric, kenyataan yang mana satukah adalah ekspresi yang betul yang menyatakan frekuensi penggal sesuatu logam dalam sebutan fungsi kerjanya?]

A. W_0 / h **B.** W_0 / c **C.** h / W_0 **D.** $(h / c) W_0$

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

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ANS: B, Cutnel, page 889, CYU 2

11. In Compton effect, an incident X-ray photon of wavelength λ is scattered by an electron, the scattered photon having a wavelength of λ'. Suppose that the incident photon is scattered by a proton instead of an electron. For a given scattering angle θ, the change λ' - λ in the wavelength of the photon scattered by the proton

[Dalam kesan Compton, suatu foton sinar-X tuju dengan jarak gelombang λ diserakkan oleh suatu elektron manakala jarak gelombang bagi foton terserak ialah λ' . Katakan foton tuju diserakkan oleh suatu proton yang manggantikan elektron. Untuk suatu sudut serakan θ yang diberikan, perubahan $\lambda' - \lambda$ dalam jarak gelombang foton terserak oleh proton adalah]

A. is greater than that scattered by the electron

- **B.** is less than that scattered by the electron
- **C.** is same as that scattered by the electron
- **D.** cannot be determined
- E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: A, Own question

12. In an electron-positron pair production by an energetic photon in the vicinity of a nucleus, the frequency of the photon λ must be

[Dalam penghasilan pasangan elektron-positron oleh suatu foton bertenaga tinggi di persekitaran suatu nucleus, frekuensi foton λ semestinya]

A. $\lambda \le h/2m_e c$ B. $\lambda \ge h/2m_e c$ C. $\lambda \le h/m_e c$ D. $\lambda \ge h/m_e c$ E. $\lambda \le h/2m_e$

13. ANS C: Young and Freeman test bank, pg. 414, Q14

In an important experiment in 1927 a beam of electrons was scattered off a crystal of nickel. The intensity of the scattered beam varied with the angles of scattering, and analysis of these results lead to confirmation of

[Dalam suatu eksperimen yang dilakukan dalam tahun 1927, suatu alur elektron diserakkan oleh suatu hablur nikel. Keamatan alur yang terserak berubah-ubah mengikut sudut ia diserakkan, dan analisis keputusan itu membawa kepada pengesahan]

- **A.** the particle nature of light
- **B.** the Bohr model of atom
- **C.** the wave nature of electrons
- D. the Rutherford model of the nucleus
- **E.** the quantisation of energy levels

ANS A: Young and Freeman test bank, pg. 425, Q2

14. Consider a particle in a box of width *L* and infinite height. Let the particle be in a state n = 11. What is the first value of x ($0 \le x \le L$), where the probability of finding the particle is highest? [Pertimbangkan suatu zarah dalam kotak dengan lebarL dan ketinggian infini. Biar ia berada dalam keadaan n = 11. Apakah nilai x ($0 \le x \le L$) yang pertama di mana keberangkalian menjumpai zarah terserbut adalah paling tinggi?]

A.	L/22	B. <i>L</i> /11	C. <i>L</i>	D. <i>L</i> /10
E.	Non of A, B,	C, D [Jawapan tiada dalam A,	, B, C, D]	

ANS B: Walker test item, pg. 654, Q65

15. Protons are being accelerated in a particle accelerator. When the speed of the proton is doubled, their de Broglie wavelength will

[Proton sedang dipecutkan oleh pemecut zarah. Bila laju proton digandakan dua kali, jarak gelombang de Broglie mereka akan]

A. increase by a factor of 2

- **B.** decrease by a factor of 2
- **C.** increase by a factor of $\sqrt{2}$
- **D.** decrease by a factor of $\sqrt{2}$

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS B: Walker student guide, pg. 506, quiz 9

16. If the minimum uncertainty in an object's position is decreased by half, what can we say about the uncertainty in its momentum?

[Jika ketidakpastian minimum bagi kedudukan suatu objek dikurangkan separuh, apa yang boleh dikatakan ke atas ketidakpastian dalam momentumnya?]

- A. The uncertainty in momentum is at most half of what it was before the change
- B. The uncertainty in momentum is at least twice what it was before the change
- **C.** The uncertainty in momentum does not change

D. The minimum uncertainty in momentum is precisely half of what it was before the change

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS A: Walker student guide, pg. 657, Q6

17. To which of the following values of *n* does the longest wavelength in the Balmer series correspond?

[Nilai n yang manakah bersepadanan dengan jarak gelombang paling panjang dalam siri Balmer?]

A. 3 **B.** 5 **C.** 1 **D.** infiniti **E.** Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS D: Young and Freeman test bank, pg. 418, Q36

18. In order for an atom to emit light, it

[Untuk memancarkan cahaya, sesuatu atom kena]

A. must be in the gaseous state [berada dalam keadaan gas]

B. must be stimulated by external radiation [dirangsang oleh pancaran luar]

C. must be in the ground state [berada dalam keadaan bumi]

D. must be in an excited state [berada dalam keadaan teruja]

E. must be fluorescent [berpendarfluor]

ANS C: Young and Freeman test bank, pg. 660, Q18,19,20

19. Which of the following statements are (is) correct?

[Pilih kenyataan(-kenyataan) yang benar daripada yang berikut]

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- A. Einstein proposed the model of the atomic structure that provides the best explanation of the observation that each atom in the periodic table has a unique sets of spectral lines. [Einstein menyarankan model struktur atom yang membekalkan penjelasan paling baik ke atas pencerapan hahawa setiap atom di dalam jadual berkala mempunyai satu set garisan spektrum yang unik.]
- **B.** According to one of the assumptions of the Bohr model, the electron in a hydrogen atom moves in an elliptical orbit about the nucleus *[Menurut salah satu anggapan model Bohr, elektron di dalam atom hidrogen berkisar di*
- dalam orbit elips yang mengelilingi nucleus.]
- **C.** Bohr's model of an atom includes idea from both classical and quantum physics. [Model atom Bohr mengandungi idea-idea daripada kedua-dua bidang fizik klasik dan fizik kuantum.]
- **D.** The plum-pudding model of atom by Thomson was verified by Rutherford's alpha scattering experiment

[Model atom 'plum-pudding' oleh Thomson telah diverifikasikan oleh eksperimen penyerakan alfa Rutherford.]

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS A: Serway. 1333, Quiz 41.5

20. Consider an electron, a proton and an alpha particle each trapped separately in identical infinite square wells. Which particle corresponds to the highest ground-state energy? [Pertimbangkan suatu elektron, suatu proton dan suatu zarah alfa yang masing-masing diperangkapkan secara berasingan di dalam telaga segiempat infinit yang identikal. Zarah yang manakan bersepadanan dengan paras tenaga bumi yang paling tinggi?]

A. the electron B. the proton C. the alpha particle

D. The ground state energy is the same in all three cases **E.** Non of A, B, C, D *[Jawapan tiada dalam A, B, C, D]*

ANS D: Serway. 1333, Quiz 41.6

21. Consider the three particles in Question 20 again. Which particle has the longest wavelength when the system is in the ground state? [Pertimbangkan semula zarah-zarah dalam Soalan 20. Zarah yang manakan mempunyai jarak gelombang yang paling panjang bila sistem berada dalam keadaan bumi?]
A. the electron B. the proton C. the alpha particle
D. All three particles have the same wavelength
E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS D: Young and Freeman test bank, pg. 663, Q22, 34, 40, 44

22. Which of the following statements are (is) correct?

[Pilih kenyataan(-kenyataan) yang benar daripada yang berikut]

- A. The kinetic energy of the electron in the first Bohr orbit of hydrogen is -13.6 eV. [Tenaga kinetik elektron dalam orbit Bohr pertama ialah -13.6 eV]
- **B.** The electron in a doubly ionised lithium atom experiences a weaker attractive force than the single electron in a hydrogen atom.

[Elektron dalam atom lithium yang dua kali terionkan mengalami daya tarikan yang lebih lemah berbanding dengan elektron tunggal dalam atom hidrogen]

C. In a hydrogen atom, the difference in the energy between adjacent orbit radii increases with the increasing value of n

[Dalam atom hidrogen, perbezaan tenaga di antara dua radius orbit yang berjiranan bertambah bila nilai n bertambah]

- **D.** The Bohr model correctly predicts the energy for the ground state of the hydrogen atom. [Model Bohr meranal dengan tepatnya tenaga keadaan bumi atom hidrogen]
- E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS B: Walker test item, pg. 664, Q36

23. Hydrogen atoms can emit four lines with visible colours from red to violet. These four visible lines emitted by hydrogen atoms are produced by electrons

[Atom hidrogen boleh memancarkan empat garis warna nampak daripada merah ke ungu. Empat garis nampak yang dipancarkan oleh atom hidrogen ini adalah dihasilkan oleh elektron]

A. that starts in the n = 2 level.

- **B.** that end up in the n = 2 level.
- C. that end up in the ground state.
- **D.** that start in the ground state.
- E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS D: Cutnel page 911

24. An electron in the hydrogen atom is in the n = 4 energy level. When this electron makes a transition to a lower level, the wavelength of the photon emitted is in the [Suatu elektron dalam atom hidrogen berada dalam paras n = 4. Bila elektron tersebut melakukan peralihan kepada paras tenaga yang lebih rendah, jarak gelombang foton yang terpancarkan berada dalam]

I. the Lyman series III. the Pashech series		II. the Blamer siries IV. the Pfund series		
A. I	B. II	C. III	D. I,II,III	

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS A: Cutnel page 934, Q 7

25. What is the longest radiation wavelength that can be used to ionized the ground-state hydrogen atom?

[Apakah jarak gelombang pancaran yang paling panjang yang boleh digunakan untuk mengiokan atom hidrogen pada keadaan bumi?]

A. *hc*/(13.6 eV)

- **B.** 2*hc*/(13.6 eV)
- **C.** 13.6 *hc*
- **D.** (13.6 eV)/hc
- E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

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Part B: Structured Questions [75 marks] Instruction: Answer ALL questions in this Part. [Bahagian B: Soalan Struktur. 75 markah] [Arahan: Jawab KESEMUA soalan dalam Bahagian ini.]

1. (a) Based on the physics constants data sheet provided (first page), calculate the ratio of the mass of proton to that of the electron.

[Berdasarkan lampiran data (dalam m/s pertama) pemalar-pemalar fizik yang dibekalkan, hitungkan nisbah antara jisim proton kepada jisim elektron.] [5 marks]

Solution:
$$\frac{M_P}{m_e} = \frac{1.67 \times 10^{-27}}{9.11 \times 10^{-31}} = 1833.2$$

(b) Calculate the kinetic energy of the electrons in a beam, in units of electron rest energy m_ec^2 , such that the relativistic mass of the electrons in the beam is as large is that of the proton. [Hitungkan tenaga kinetik bagi elektron-elektron dalam satu alur elektron, dalam unit tenaga rehat elektron m_ec^2 , sedemikian rupa supaya jisim kerelatifan elektron dalam alur tersebut bersamaan dengan jisim proton.)

Solution: Young and Freeman study guide, pg 281, Quiz 2,3

 $E = m'_{e}c^{2} = m_{e}c^{2} + K$ set $m'_{e}c^{2} = M_{p}c^{2} = (1833.2)m_{e}c^{2}$ $\Rightarrow K = (1833.2 - 1)m_{e}c^{2} = (1832.2)m_{e}c^{2}$

(c) What is the electric potential (in unit of Volt) that is required to accelerate the electron in (b) (from rest) ?

[Apakah beza keupayaan elektrik (dalam unit Volt) yang diperlukan untuk memecutkan elektron dalam (b) di atas (dari keadaan rehat)?]

[5 marks]

[10 marks]

[5 marks]

Solution: Young and Freeman study guide, pg 281, Quiz 2,3 $eV = K = (1832.2)m_ec^2 \Rightarrow V = (1832.2)m_ec^2 / e = 938.9$ MV

(d) If a 'moving clock' runs slower, what will the age difference between two twins if one stays on the Earth while the second makes a round trip to a point in space ten light years from Earth at a speed of 0.95*c*?

[Jika masa bagi 'jam yang bergerak' mengalir lebih perlahan', apakah perbezaaan umur di antara dua orang anak kembar jika salah satu daripada mereka tinggal di Bumi manakala yang seorang lagi menjalani satu penggembaraan dengan laju 0.95c ke satu tempat sejauh 10 tahuncahaya daripada Bumi dan kembali ke Bumi selepas penjelajahan tersebut?]

Solution: Young and Freeman study guide, pg 278, Example 7

$$\gamma = \frac{1}{\sqrt{1 - (0.95)^2}} = 3.2$$

Time taken for the round trip, according to the twin on Earth, is

 $T_E = D/v = 20 c \cdot yr/0.95c = 21.05 yr.$

Time taken for the round trip, according to the twin on ship, is $T_S = D'/\nu = D/(\nu) = 20 \text{ cyr}/(3.2 \text{ 0.95c}) = 6.58 \text{ yr}$, where $D' = 20 \text{ ly}/\gamma$ due to length contraction.

 $\Rightarrow T_E - T_S = (21.05 - 6.58) \text{ yr} = 14.47 \text{ yr}$

2. (a) A 60-W bulb is at an efficiency of 6.20%. What is the number of photons per second given off by the bulb assuming the wavelength of light to be 580 nm?

[6 marks]

Solution: Walker Test Item, page 642, Q5:

energy of 1 photon=
$$\frac{hc}{\lambda} = \frac{1240}{580}$$
 eV=2.13eV

Let number of photon per second =
$$N$$

therefore
$$N \frac{nc}{\lambda} = 2.325 \times 10^{19} \text{ eV/s}$$

 $N = \frac{2.325 \times 10^{19} \text{ eV/s}}{2.13 \text{ eV}} = 1.09 \times 10^{19} \text{ /s}$

(b) The work functions of several metals are listed below.

Metal	ϕ (in eV)
W	4.5
Ag	4.8
Cs	1.8
Cs on W	1.36

- (i) Which metals yield photoelectrons when bombarded with light of wavelength 500 nm?
- (*ii*) For those surfaces where photoemission occurs with the above light source, calculate the stopping potential in volts.
- (*iii*) For the metal tungsten calculate the threshold wavelength which would just start producing photoelectrons.

[3 + (2+2) + 2 = 9 marks]

Solution: Young and Freeman study guide, pg 287, Example 2

- (i) $E = hf = hc/\lambda = 2.48 \text{ eV}$; Cs and Cs on W yields photoelectrons
- (*ii*) For Cs: stopping potential is (2.48 eV 1.8 eV)/e = 0.68 VFor Cs on W: stopping potential is (2.48 eV - 1.36 eV)/e = 1.12 V
- (*iii*) $\lambda_t = hc/\phi = 1240 \text{ eV} \cdot \text{nm} / 4.5 \text{ eV} = 276 \text{ nm}$
- (c) A large number if 30.0 pm photons are scattered twice by stationary electrons. Find the **RANGE** of wavelength of the scattered photon in pm.

[Sejumlah besar foton-foton yang berjarak gelombang 30.0 pm diserakkan dua kali oleh satu elektron rehat. Hitungkan julat bagi jarak gelombang foton yang terserakkan dalam unit pm.] [10 marks]

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Solution: Young and Freeman test bank, pg 409, Q14:

When bombarded once, the maximal increase in the photon wavelength is given by $\Delta \lambda_{\max} = \frac{2h}{m_e c} = 2 \times 2.43 \text{pm} = 4.86 \text{pm}$ when the scattering angle $\theta = 180^\circ$. When the oncescattered photon is scattered again, the maximum shift in wavelength suffered by that photon is also $\Delta \lambda_{\max}$, making the maximal total shift in wavelength = $2 \Delta \lambda_{\max} = 2 \times 4.86 \text{ pm} = 9.72 \text{ pm}$. Hence the range of scattered photon lies between λ_n to $\lambda_n + 2 \Delta \lambda_{\max}$, i.e. 30.0 pm - 39.72 pm.

3. (a) Find the frequency of revolution of electron in n = 1 and n = 2 Bohr orbits. What is the frequency of the photon emitted when an electron in the n = 2 orbit drops to n = 1 orbit? [Hitungkan frekuensi kisaran bagi elektron dalam orbit-orbit Bohr n = 1 dan n = 2. Apakah frekuensi foton yang dipancarkan bila suatu elektron dalam orbit n=2 jatuh ke orbit n = 1?]
 [3 + 2 + 2 + 3 marks]

Solution: Bieser, pg 137/tutorial 5

From Bohr's postulate of quantisation of angular momentum, $L = (mv)r = nh/2\pi$, the velocity is related to the radius as $v = nh/2m\pi$. Furthermore, the quantised radius is given in terms of Bohr's radius as $r_n = n^2 r_0$. Hence, $v = h/2\pi mnr_0$. The frequency of revolution f = 1/T (where T is the period of revolution) can be obtained from $v = 2\pi r/T = 2\pi n^2 r_0 f$. Hence, $f = v/2\pi r = (h/2\pi mnr_0)/2\pi r = h/4\pi^2 mn^3 (r_0)^2$.

For n = 1, $f_1 = h/4\pi^2 m(r_0)^2 = 6.56 \times 10^{15}$ Hz. For n = 2, $f_2 = h/4\pi^2 m(2)^3 (r_0)^2 = 6.56 \times 10^{15}/8$ Hz = 8.2×10^{14} .

Photon's frequency = $\Delta E/h = 13.6 (1/1^2 - 1/2^2) \text{ eV} / h = 2.46 \text{ x } 0^{15} \text{ Hz}$

(b) Consider the case of 'particle in a box' (infinite square well). The lowest energy level of a particle (call it particle A) confined to a 1-D region of space with fixed dimension L is E_0 . If an identical particle (call it particle B) is confined to a similar region with fixed distance L/4, what is the energy of the lowest energy level of the particle B? Express your answer in terms of E_0 . [Pertimbangkan kes 'zarah di dalam kotak' (telaga segiempat infinit). Tenaga paling rendah bagi satu zarah (label ia zarah A) terkongkong di dalam satu ruang 1-D dengan dimensi L yang tetap ialah E_0 . Jika suatu zarah lain (zarah B) yang identical dengan zarah A dikongkongkan di dalam satu ruang yang serupa tapi dengan jarak tetap L/4, apakah tenaga bagi paras tenaga yang terendah bagi zarah B? Nyatakan jawapan anda dalam sebutan E_{-}]

[5 marks]

Solution: Young and Freeman test bank, pg 425, Short Questions 1: $16E_0$

$$E_0 = \frac{h^2}{8mL^2}$$

$$E'_0 = \frac{h^2}{8mL^{*2}} = \frac{h^2}{8m(L/4)^2} = 16\frac{h^2}{8mL^2} = 16E_0$$

(c) Estimate the kinetic energy (in eV) should electrons have if they are to be diffracted from crystal with interatomic distance of the order of a few A.

[Anggarkan tenaga kinetik (dalam unit eV) yang harus diperolehi oleh elektron-elektron jika mereka hendak dibelaukan oleh hablur yang berjarak antara-atom dalam tertib beberapa Å] [5 marks]

Solution

Serway, Mosses and Mayer, page 150, Example 4.3

For diffraction to happen, we require λ ~ interactomic distance ~ a few Å

$$p = \frac{hc}{\lambda c} \sim \frac{1240 \text{eV} \cdot \text{nm}}{\text{few} (0.1 \text{nm}) \times c} = \frac{0.01124 \text{MeV}}{\text{few} \times c}$$
$$\Rightarrow K = \frac{p^2}{2m_e} \sim \left(\frac{0.0124 \text{MeV}/c}{\text{few}}\right)^2 \frac{1}{2 \times 0.5 \text{MeV}/c^2} = \frac{1.5 \times 10^{-4}}{\text{few}^2} \text{MeV}$$

(d) What is the frequency of the de Broglie waves associated with a body of rest mass m_0 moving with velocity v?

[Apakah frekuensi bagi gelombang de Broglie yang dikaitkan dengan jasad yang jisim rehatnya m_0 dan bergerak dengan laju v?]

[5 marks]

Solution: Arthur Beiser 5th edition, page 99

$$E = hf = mc^{2} = \gamma m_{0}c^{2} = \frac{m_{0}c^{2}}{\sqrt{1 - \frac{v^{2}}{c^{2}}}} \Rightarrow f = \frac{m_{0}c^{2}}{h\sqrt{1 - \frac{v^{2}}{c^{2}}}}$$

PAST YEAR TESTS AND EXAM QUESTIONS (2003/04 – 2005/06)

SESSI 03/04/TEST1

ZCT 104/3E Modern Physics Semester Test I, Sessi 2003/04 Duration: 1 hour

Answer all questions

1. A radar antenna is rotating at an angular speed of 0.25 rad/s, as measured on Earth. To an observer moving past the antenna at a speed of 0.8*c*, what is its angular speed in rad/s?

A. 0.42 B. 0.09 C.1.92 D. 0.15 E. Non of the above ANS: D, Cutnell, Q1, pg. 877

Suppose that you are travelling on board a spacecraft that is moving with respect to the Earth at a speed of 0.975*c*. You are breathing at a rate of 8.0 breaths per minute. As monitored on Earth, what is your breathing rate?
 A. 13.3 B. 2.88 C.22.2 D. 1.77

E. Non of the above ANS: D, Cutnell, Q4, pg. 877

- 3. At what speed is the magnitude of the relativistic momentum of a particle three times the magnitude of the non-relativistic momentum?
 A. 0.999c B. 0.900c C.0.911c D. 0.94 3c
 E. Non of the above ANS: D, Cutnell, Q17, pg. 878
- 4. An electron and a positron collide and undergo pair-annihilation. If each particle is moving at a speed of 0.8*c* relative to the laboratory before the collision, determine the energy of each of the resultant photon.

A. 0.85MeV B. 1.67 MeV C. 0.51 MeV D. 0.72MeV E. Non of the above ANS: A, Cutnell, Q17, pg. 878, modified

5. Ultraviolet light with a frequency of 3.0×10^{15} Hz strikes a metal surface and ejects electrons that have a maximum kinetic energy of 6.1 eV. What is the work function of the metal?

A. 13.6 eV B. 1.67 eV C. 0.51 eV D. 6.3 eV E. Non of the above ANS: D, Cutnell, Q5, pg. 900, modified

6. X-ray of wavelength 1.2 Å strikes a crystal of d-spacing 4.4 Å. Where does the diffraction angle of the second order occur?

A.16° **B.** 33° **C.** 55° **D.** 90° **E.** Non of the above ANS: B, Schaum's 3000 solved problems, Q38.46, pg. 715

- 7. A honeybee (mass 1.3×10^{-4} kg) is crawling at a speed of 0.020 m/s. What is the de Broglie wavelength of the bee?
 - **A.** 1.6×10^{-28} m **B.** 4.6×10^{-28} m **C.** 2.6×10^{-28} m **D.** 3.06×10^{-28} m **E.** Non of the above ANS: C, Cutnell, Q21, pg. 901, modified

SESSI 03/04/TEST1

8. An electron is trapped within a sphere whose diameter is 6×10^{-15} m. Estimate the minimum uncertainty in the electron's momentum in MeV/*c*.

A. 16 **B.** 1 **C.** 50 **D.** 2 **E.** 10 ANS:A, Cutnell, Q32, pg. 901, modified

9. Incident x-rays have a wavelength of 0.3120 nm and are scattered by the "free electron" in a graphite target. The angle of the scattered x-ray photon is 135 degree. What is the magnitude of the momentum of the incident photon?

 A. 0.01300 MeV/c
 B. 0.00391 MeV/c
 C. 0.03450 MeV/c

 D. 0.01315 MeV/c
 E. 0.00397 MeV/c
 ANS:E, Cutnell, Q15, pg. 900

 I0. What is the magnitude of the momentum of the scattered photon in Question 9?

 A. 0.01300 MeV/c
 B. 0.00391 MeV/c
 C. 0.03450 MeV/c

 D. 0.01315 MeV/c
 E. 0.00397 MeV/c
 ANS:B , Cutnell, Q15, pg. 900

11. Which of the following statement(s) is (are) true?

- I(T) When two observer who are moving relative to each other measure the same physical quantity, they may obtain different values
- II(T) The laws of physics are the same for observers in all inertial frames
- III (T) The speed of light in free space has the same value in all direction and in all inertial frames
- IV(F) Maxwell theory of electromagnetic radiation is inconsistent with special theory of relativity

A. II,III B. I, II,III C. II, III, IV D. I only E. I,II,III,IV

ANS:B, Christman's pocket companion, pg. 291.292

- 12. Which of the following statement(s) is (are) true?
 - I(T) Relativity theory requires a revision of the definition of momentum if it were to be consistent with conservation of momentum
 - **II(F)** The kinetic energy of a relativistic particle with rest mass m_0 moving with speed v is given by $m_0 c^2 (1 \gamma)$, where γ is the Lorentz factor
 - **III (F)** The total energy of a relativistic particle is given by $m_0 c^2 (m_0 \text{ is the rest mass})$
 - **IV(F)** The classical expression of kinetic energy $K = \frac{p^2}{2m_0^2}$, where p is the linear momentum of the

particle, is a special case of the relativistic energy $E = \sqrt{(pc)^2 + (m_0 c^2)^2}$

A. II,III	B. I, II,III	C. II, III, IV
D. I, IV	E. I,II, III,IV	

ANS: **I only** (free mark will be given for this question since the correct answer is not in the option) Christman's pocket companion, pg. 299.300

13. Which of the following statement(s) is (are) true?

SESSI 03/04/TEST1

- **I(T)** Photon carries momentum
- **II(F)** The Compton shift $\Delta \lambda$ is greater for higher-energy photons
- **III(F)** The Compton shift $\Delta \lambda$ is smaller for lower-energy photons

A. I only	B. I, II	C. II, III
D. I,III	E. I,II, III	

ANS:A, Machlup, pg. 497

14. Which of the following statements correctly describe the following experiments? I(T) Photoelectricity exhibits particle nature of light

II(F) Electron diffraction exhibits wave nature of light

III (T) Compton effect exhibits particle nature of electron

W(T) Compton affact avhibits partials nature of light

IV(I) Comptone	filect exhibits particle i	lature of light
A. II.III	B. I, II,III	C. II, III, IV

A. II.III B. I, II,III E. I,II, III,IV D. I,III, IV

ANS:D, My own questions

- 15. Which of the following statements correctly describe light?
 - I(T) According to Einstein, the energy in an electromagnetic beam is concentrated in discrete bundles called photon
 - II(T) According to the classical Maxwell theory of radiation, light is described as electromagnetic wave
 - **III** (F) The energy of the photon is proportional to the root-mean-square of the amplitude of the electromagnetic fields
 - IV (*) The intensity of a beam of light is proportional to the root-mean-square of the amplitude of the electromagnetic fields

A. II,III	B. I, II,IV	C. II, III, IV
D. I,III, IV	E. I,II, III,IV	

ANS:C (Free mark will be given for this question because statement IV may appear confusing and illstated).

(*) Rigorously speaking, statement IV is correct because the "root-mean-square of the amplitude" is equal to the square of the amplitude. The amplitude is a constant independent of time and space, hence whether you average its square over a complete period or simply squaring it without taking its

"average" the answer is still the same. Mathematically this is stated as $\langle E_0^2 \rangle = \frac{1}{T} \int_{0}^{T} E_0^2 dt = E_0^2$.

My own questions

16. Which of the following statements correctly describe photoelectricity?

- I(T) If the frequency is unchanged the number of electrons ejected depends on the incident intensity II(F) If the frequency is unchanged the kinetic energies of electrons ejected depends on the incident
- intensity **III** (**T**) In photoeletricity the fundamental event is the interaction of a single quantum of light with a
- single particle of matter

IV(T)	Electrons are	ejected imm	ediately wh	hen photoel	ectricity	occurs
A. II,II	I	B. I, II,I	I	C. II, I	II, IV	

D. I.III. IV E. I.II. III.IV

ANS:D, Christman's pocket companion, pg. 302-303

SESSI 03/04/TEST1

17.	Which I(T) II(T)	f the following statements correctly describe Compton scattering? The Compton effect has to be treated relativistically The Compton effect is significant only when the incident wavelength of the light used is comparable to the Compton wavelength of the electron	
	III(T)	The maximum change in wavelength is given by $\Delta \lambda_{max} = 2\lambda_C$, where λ_C is the Compton	n
	IV (F)	wavelength of electron The Compton effect is much larger for electrons bounded to atoms than for free electrons	
	A. 11,11 D. 1,111		
	ANS:B	partly Christman's pocket companion, pg. 305, partly own question	
18.	I(F) II(T) III(T)	f the following statement(s) is (are) true? The Davisson-Gremer experiment verifies the particle nature of electromagnetic wave in the Davisson-Gremer experiment the wavelength of the electron is comparable to the nteratomic spacing in the crystal At the quantum scale particles behave like waves At the quantum scale waves behave like particles	

A. II,III	B. I, II,III	C. II, III, IV
D. I,III, IV	E. I,II, III,IV	

ANS:C, My own question

19. An increase in the voltage applied to an x-ray tube causes an increase in the x-rays'

- I(F) wavelength II(F) speed

III(T) energy IV (T) frequency

A. III,IV B. I, II,III C. II, III, IV D. I.III, IV E. I,II, III,IV

ANS:A, Arthur Beiser, Modern technical physics, Q 7, pg. 801

20. The description of a particle in terms of matter waves is legitimate because

I(F) It is based on common sense

II(F) The analogy with electromagnetic waves is plausible

III(T) theory and experiment agree

C. II, III A. III only B. I. II D. I.III E. I.II, III

ANS:A, Arthur Beiser, Modern technical physics, Q 9, pg. 801

Data

speed of light in free space, $c = 3.00 \times 10^8 \text{ m s}^{-1}$

elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$

the Planck constant, $h = 6.63 \times 10^{-34} \text{ J s}$

unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$

rest mass of electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$

SESSI 03/04/TEST1 rest mass of proton, $m_p = 1.67 \ge 10^{-27} \text{ kg}$

SESSI 03/04/TEST2

ZCT 104/3E Modern Physics Semester Test II, Sessi 2003/04 Duration: 1 hour

Data

speed of light in free space, $c = 3.00 \times 10^8 \text{ m s}^{-1}$ elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$ the Planck constant, $h = 6.63 \times 10^{-37} \text{ Js}$ unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$ rest mass of electron, $m_c = 9.11 \times 10^{-31} \text{ kg}$ rest mass of proton, $m_m = 1.67 \times 10^{-27} \text{ kg}$

Answer all questions

1. A particle of mass m is confined to a one-dimensional box of length L. The particle's momentum is given by

D. $n\hbar/2L$

 A. h/2L
 B. nh/2L
 C. ħ/2L

 E. Non of the above
 ANS: B. Ronald and William, O10.20, pg. 92

2. The energy of the particle in Q1 is given by

A.
$$n^2 \frac{\hbar^2}{8m\pi t^2}$$
 B. $n^2 \frac{\hbar^2}{8mL^2}$ **C.** $n^2 \frac{\pi^2 h^2}{2mL^2}$ **D.** $n^2 \frac{\hbar^2}{2mL^2}$

E. Non of the above ANS: B, Ronald and William, Q10.20, pg. 92

3. What is the ionisation energy of the hydrogen atom?

A. infinity	B. 0	C13.6 eV	D. 13.6 eV
E. Non of the abov	e		
ANS: D, Modern	Technical Phys	ics, Beiser, pg. 786	

4. What is the ground state energy of the hydrogen atom?

A. infinity	B. 0	C. -13.6 eV	D. 13.6 eV
E. Non of the above	/e		
ANS: C, Modern	Technical Phys	ics, Beiser, pg. 786	

5. An electron collides with a hydrogen atom in its ground state and excites it to a state of n = 3. How much energy was given to the hydrogen atom in this collision?

 A. -12.1 eV
 B. 12.1 eV
 C. -13.6 eV
 D. 13.6 eV

 E. Non of the above
 ANS: B, Modern Technical Physics, Beiser, Example 25.6, pg. 786

6. Which of the following transitions in a hydrogen atom emits the photon of lowest frequency?

A. n = 3 to n = 4**B.** n = 2 to n = 1**C.** n = 8 to n = 2**D.** n = 6 to n = 2**E.** Non of the above **ANS: D, Modern Technical Physics, Beiser, Q40, pg. 802, modified**

SESSI 03/04/TEST2

7. In Bohr's model for hydrogen-like atoms, an electron (mass *m*) revolves in a circle around a nucleus with positive charges *Ze*. How is the electron's velocity related to the radius *r* of its orbit?

A.
$$v = \frac{1}{4\pi\varepsilon_0} \frac{Ze^2}{mr}$$
 B. $v = \frac{1}{4\pi\varepsilon_0} \frac{Ze^2}{mr^2}$ **C.** $v = \frac{1}{4\pi\varepsilon_0} \frac{Ze}{mr^2}$ **D.** $v^2 = \frac{1}{4\pi\varepsilon_0} \frac{Ze^2}{mr}$

ANS: D, Schaum's series 3000 solved problems, Q39.13, pg 722 modified

8. How is the total energy of the electron in Question 7 related the radius of its orbit?

A.
$$E = \frac{1}{4\pi\varepsilon_0} \frac{Ze^2}{2r}$$
B.
$$E = \frac{1}{4\pi\varepsilon_0} \frac{Ze}{2r}$$
C.
$$E = -\frac{1}{4\pi\varepsilon_0} \frac{Ze}{2r}$$
D.
$$E = -\frac{1}{4\pi\varepsilon_0} \frac{Ze^2}{2r}$$

E. Non of the above ANS: D, Schaum's 3000 solved problems, Q39.14, pg. 722

9. The quantum number n of the lowest energy state of a hydrogen atom

A. is 0B. is 1C. depends on the orbit sizeD. depends on the electron speedE. Non of the aboveANS: B, Modern Technical Physics, Beiser, Q23, pg. 802

10. The electron of a ground state hydrogen atom

A. has left the atom
highest energyB. is at rest
E. Non of the aboveC. is in its orbit of lowest energy
E. Non of the aboveD. is in its orbit of
t of highest energyANS: C, Modern Technical Physics, Beiser, Q16, pg. 801

11. A proton and an electron, far apart and at rest initially, combine to form a hydrogen atom in the ground state, A single photon is emitted in this process. What is its wavelength?

A. 13.6 nm B. 20 nm C. 91 nm D. infinity E. Non of the above ANS: C, Modern Technical Physics, Beiser, Q30, pg. 804

12. The wave function of a particle trapped in an infinite quantum well of width L is given by

$$\psi_n = A_n \sin \frac{n\pi x}{L}$$
. Determine the normalisation constant A_n .
A. $\sqrt{\frac{L}{2}}$ **B.** $\frac{2}{L}$ **C.** $\sqrt{\frac{2n}{L}}$ **D.** $\sqrt{\frac{2}{L}}$ **E.** Non of the above
ANS: D, my own question

13. Where does the particle in Question 12 spend most of its time while in the ground state? **A.** around x = 0 **B.** around x = L **C.** around x = L/2 **D.** around x = L/4 **E.** Non of the above **ANS:C. My own question**

SESSI 03/04/TEST2

14. How many different photons can be emitted by hydrogen atoms that undergoes transitions to the ground states from the n = 5 states?

A. 3 B. 6 C. 10 D. 15 E. Non of the above ANS: C, Ronald and William, Q11.8, pg. 109

- 15. Which of the following statements are true about an electron trapped on the *x*-axis by infinite potential energy barriers at x = 0 and x = L?
 - I(T) Inside the trap the coordinate-dependent part of the wave function ψ satisfy the Schrödinger equation
 - **II(T)** ψ obeys the boundary conditions $\psi(0) = 0$ and $\psi(L) = 0$
 - III (F) The probability to locate the electron is everywhere the same inside the well

IV(T) Outside the trap, $\psi = 0$

A. II,III B. I, II,III C. II, III, IV D. I, II, IV only E. Non of the above

ANS:D. Christman's pocket companion. Item 40.3. pg. 312

16. Which of the following statements are true?

I(T)	The energy of a particle trapped inside	e an finite quantum well is quantised	
II(T)	The energy of a particle trapped inside an infinite quantum well is quantised		
III (F)	III (F) The lowest energy of a particle trapped in an infinite quantum well is zero		
A. II,I	II B. I, II,III	C. II, III	
D. I, II	E. Non of the above		
ANS:D my own question			

17. Which of the following statement(s) is (are) true?

- I(T) The plum pudding model cannot explains the backscattering of alpha particles from thin gold foils
- **II(T)** Rutherford model assumes that an atom consists of a tiny but positively charged nucleus surrounded by electrons at a relatively large distance
- **III(T)** In the Bohr model, an electron in a stationary state emits no radiation
- IV(T) In the Bohr model, electrons bound in an atom can only occupy orbits for which the angular momentum is quantised

A. III,IV	B. I, II.III	C. I, II, III.IV	D. I,II
E. Non of the above			
ANS:C,Giancoli, Summery on pg 972			

18. Which of the following statement(s) is (are) true?

- I(F) Bohr's theory worked well for one electron ions as well as for multi-electron atoms
- **II(F)** Bohr's model is plagued by the infrared catastrophe
- **III(F)** In the Bohr model, n = 1 corresponds to the first excited state
 - IV(T) Rutherford model cannot explain the stability of atomic orbit

A. III,IV	B. I, II.III	C. I, II, III.IV	D. I,II
E. Non of the ab	ove		
ANS:E, My own	question		

19. Which of the following statements are correct?

I(F) Balmer series corresponds to the spectral lines emitted when the electron in a hydrogen atom makes transitions from higher states to the n = 1 state

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- **II(F)** Lyman series corresponds to the spectral lines emitted when the electron in a hydrogen atom makes transitions from higher states to the n = 2 state
- **II(T)** Paschen series corresponds to the spectral lines emitted when the electron in a hydrogen atom makes transitions from higher states to the n = 3 state

A. II,III B. I, II,III C. II, III D. III only E. Non of the above ANS:D, My own questions

20. Which of the following statements are correct?

- I(T) Frank-Hertz experiment shows that atoms are excited to discrete energy levels
- II(T) Frank-Hertz experimental result is consistent with the results suggested by the line spectra
- III (T) The predictions of the quantum theory for the behaviour of any physical system must correspond to the prediction of classical physics in the limit in which the quantum number specifying the state of the system becomes very large
- IV(T) The structure of atoms can be probed by using electromagnetic radiation

A. II,III B. I, II,IV C. II, III, IV

D. I,II, III, IV E. Non of the above

ANS:D, My own questions

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UNIVERSITI SAINS MALAYSIA

Second Semester Examination Academic Session 2003/2004

February/March 2004

ZCT 104E/3 - Physics IV (Modern Physics) [Fizik IV (Fizik Moden)]

Duration: 3 hours [Masa: 3 jam]

Please check that the examination paper consists of **SIXTEEN** pages of printed material before you begin the examination.

[Sila pastikan bahawa kertas peperiksaan ini mengandungi ENAM BELAS muka surat yang bercetak sebelum anda memulakan peperiksaan ini.]

<u>Instruction</u>: Answer any **FOUR (4)** questions. Students are allowed to answer all questions in Bahasa Malaysia or in English.

[<u>Arahan</u>: Jawab mana-mana **EMPAT** soalan. Pelajar dibenarkan menjawab semua soalan sama ada dalam Bahasa Malaysia atau Bahasa Inggeris.]

- 2 -

Data

speed of light in free space, $c = 3.00 \text{ x} 10^8 \text{ m s}^{-1}$

permeability of free space, $\mu_0 = 4\pi \text{ x } 10^{-7} \text{ H m}^{-1}$

permittivity of free space, $\varepsilon_0 = 8.85 \text{ x } 10^{-12} \text{ F m}^{-1}$

elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$

the Planck constant, $h = 6.63 \times 10^{-34} \text{ J s}$

unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$

rest mass of electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$

rest mass of proton, $m_{\rm p} = 1.67 \text{ x } 10^{-27} \text{ kg}$

molar gas constant, = 8.31 J K⁻¹ mol⁻¹

the Avogadro constant, $N_{\rm A} = 6.02 \text{ x } 10^{23} \text{ mol}^{-1}$

gravitational constant, $G = 6.67 \times 10-11 \text{ N m}^2 \text{ kg}^{-2}$

acceleration of free fall, $g = 9.81 \text{ m s}^{-2}$

- 3 -

[ZCT 104E]

Question 1. (25 marks)

1.1 A spaceship of proper length L_p takes t seconds to pass an Earth observer. What is its speed as measured by the Earth observer according to classical physics? [Sebuah kapal angkasa yang panjang proper-nya L_p mengambil masa t untuk bergerak melalui seorang pemerhati di Bumi. Mengikut fizik klasik, apakah kelajuannya yang terukur oleh pemerhati di Bumi itu?]

A.
$$L_p/t$$
 B. $\frac{cL_p/t}{\sqrt{c^2 + (L_p/t)^2}}$ **C.** c **D.** L_p

E. Non of the above [Tiada dalam pilihan di atas]

ANS: A, Serway solution manual 2, Q9A, pg. 336

1.2 In Question 1, what is its speed as measured by the Earth observer according to special relativity? [Dalam soalan 1, apakah kelajuan yang terukur oleh pemerhati di Bumi mengikut teori kerelatifan khas?]

A.
$$L_p/t$$
 B. $\frac{cL_p/t}{\sqrt{c^2 + (L_p/t)^2}}$ **C.** c **D.** L_p

E. Non of the above [*Tiada dalam pilihan di atas*]

ANS: B, Serway solution manual 2, Q9A, pg. 336

1.3 What is the momentum of a proton if its total energy is twice its rest energy? [Apakah momentum bagi suatu proton jika jumlah tenaganya adalah dua kali tenaga rehatnya?]

A. 1620 Ns **B.** 1 MeV/*c* **C.** 938 MeV/*c* **D.** 2 MeV/*c*

E. 1620 MeV/c

ANS: E, Serway solution manual 2, Q21, pg. 339

1.4 The power output of the Sun is 3.8×10²⁶ W. How much rest mass is converted to kinetic energy in the Sun each second?
 [Output kuasa Matahari ialah 3.8×10²⁶ W. Berapakah jisim rehat yang ditukarkan kepada tenaga kinetik setiap saat di dalam Matahari?]

A. 4.2×10^9 kg **B.** 1.3×10^{17} kg **C.** 3.6×10^8 kg

....3/-

[ZCT 104E]

D. 6.6×10^{10} kg **E.** 4.2×10^{8} kg

ANS: A, Serway solution manual 2, Q37, pg. 340

1.5 What is the value of *hc/e* in unit of nm · eV [*Apakah nilai hc/e dalam unit* nm · eV ?]

A. 1.240 **B.** 1240×10^{-6} **C.** 1240 **D.** 1240×10^{-9}

E. 1240×10^{-3}

ANS: C, my own question [note: typo: the quantity should read hc instead of hc/e]

1.6 By what factor is the mass of an electron accelerated to the speed of 0.999c larger than its rest mass? [Berapa besarnya factor jisim satu elektron yang dipecutkan kepada kelajuan 0.999c berbanding dengan jisim rehatnya?]

A. 31.6 B. 0.03 C. 0.04 D. 22.3 E. 1.0

ANS: D, my own question

- 1.7 The rest mass of a photon [Jisim rehat foton]
 - A. is zero
 - [ialah sifar] **B**. is the same as that of an electron [sama dengan jisim elektron] **C**. depends on its frequency [bergantung kepada frekuensinya] **D**. depends on its energy [bergantung kepada tenaganya] **E**. Non of the above [Tiada dalam pilihan di atas]

ANS: A, Modern physical technique, Beiser, MCP 6, pg. 801

- 1.8 Determine the vacuum wavelength corresponding to a γ -ray energy of 10^{19} eV [*Tentukan jarak gelombang vakum bagi sinar* γ yang bersepadanan dengan tenaga 10^{19} eV]
 - **A.** 1.24×10^{-9} pm
 - **B.** $1.24 \times 10^{-16} \text{ pm}$

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- **C.** 1.24×10^{-25} nm **D.** 1.24×10^{-16} nm
- **D.** 1.24×10^{-1} m
- **E.** 1.24×10^{-25} nm

ANS: D, Schaum's 3000 solved problems, Q38.3, pg. 708

- 1.9 To produce an x-ray quantum energy of 10⁻¹⁵ J electrons must be accelerated through a potential difference of about [Untuk menghasilkan sinar-x dengan tenaga kuantum 10⁻¹⁵ J suatu elektron mesti dipecutkan melalui satu beza keupayaan yang nilainya lebih kurang]
 - **A.** 4 kV
 - **B.** 6 kV
 - **C.** 8 kV
 - **D.** 9 kV **E.** 10 kV

ANS: B, OCR ADVANCED SUBSIDIARY GCE PHYSICS B (PDF), Q10, pg. 36

Question 1.10– 1.12 [Soalan 1.10-1.12]

- **A.** 10^{-4} m **B.** 10^{-7} m **C.** 10^{-10} m **D.** 10^{-12} m **E.** 10^{-15} m
- 1.10 Which of the values in the list above is the best estimate of the radius of an atom? [Nilai yang manakah dalam senarai di atas memberikan anggaran yang paling baik untuk radius satu atom?]

ANS: C, OCR ADVANCED PHYSICS B (PDF), Q1, pg. 74

1.11 Which of the values in the list above is the best estimate of the wavelength of visible light? [Nilai yang manakan dalam senarai di atas memberikan anggaran yang paling baik untuk jarak gelombang cahaya ternampak?]

ANS: B, OCR ADVANCED PHYSICS B (PDF), Q1, pg. 74

1.12 Which of the values in the list above is the best estimate of the wavelength of a 1.5 MeV electron?

[Nilai yang manakan dalam senarai di atas memberikan anggaran yang paling baik untuk jarak gelombang bagi elektron 1.5 MeV?]

ANS: D, OCR ADVANCED PHYSICS B (PDF), Q1, pg. 74

1.13 What is the momentum of a single photon of red light ($\nu = 400 \times 10^{12}$ Hz) moving through free space?

[Apakah momentum foton cahaya merah ($v = 400 \times 10^{12}$ Hz) yang bergerak melalui ruang bebas?]

A. 8.8×10⁻²⁷ kg m/s **B**. 6 keV **C**. 1240 eV/c **D**. 1.65 eV/c **E**. 2.4 eV/c

ANS: D, Schaum's 3000 solved problems, Q8.12, pg. 709

1.14 What potential difference must be applied to stop the fastest photoelectrons emitted by a nickel surface under the action of ultraviolet light of wavelength 2000 Å? The work function of nickel is 5.00 eV.

[Apakah beza keupayaan yang mesti dikenakan untuk menghentikan fotoelektron paling pantas yang dipancarkan dari permukaan nikel di bawah tindakan cahaya ultraungu yang jarak gelombangnya 2000 Å? Fungsi kerja nikel ialah 5.00 eV.]

A. 1.0 kV **B**. 1.2 kV **C**. 2.0 V **D**. 1.0 V **E**. 1.2 V

ANS: E, Schaum's 3000 solved problems, Q38.18, pg. 710

- 1.15 Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I. The assumption of the Ether frame is inconsistent with the experimental observation

[Tanggapan rangka Ether adalah tidak konsisten dengan pemerhatian eksperimen]

- II. The speed of light is constant [Kelajuan cahaya adalah malar]
- III. Maxwell theory of electromagnetic radiation is inconsistent with the notion of the Ether frame [Teori sinaran keelektromagnetan Maxwell adalah tidak konsisten dengan tanggapan rangka Ether]

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IV Special relativity is inconsistent with the notion of the Ether frame *[Kerelatifan Khas adalah tidak konsistent dengan tanggapan rangka Ether]*

A. III,IV **B.** I, II, III **C.** I, II, III,IV

D. I, II **E.** I, II,IV

ANS: E, my own question

- 1.16 Which of the following statements are true about light? [Yang manakah kenyataan berikut adalah benar berkenaan dengan cahaya?]
 - I. It propagates at the speed of $c = 3 \times 10^8$ m/s in all medium [Cahaya tersebar pada kelajuan $c = 3 \times 10^8$ m/s dalam semua jenis medium]
 - II. It's an electromagnetic wave according to the Maxwell theory [Cahaya ialah gelombang elektromagnetik mengikut teori Maxwell]
 - **III.** It's a photon according to Einstein [Cahaya ialah foton menurut Einstein]
 - **IV.** It always manifests both characteristics of wave and particle simultaneously in a given experiment [Cahaya sentiasa memperlihatkan kedua-dua ciri gelombang dan kezarahan secara serentak dalam sesuatu eksperimen]
 - **A.** I,IV **B.** II, III,IV **C.** I, II, III,IV
 - **D.** I, II **E.** II,III

ANS: E, my own question

- 1.17 Which of the following statements are true about Lorentz transformation? [Yang manakah kenyataan berikut adalah benar berkenaan dengan transformasi Lorentz?]
 - I. It relates the space-time coordinates of one inertial frame to the other [*Ia menghubung-kaitkan koordinat-koordinat ruang-masa suatu rangka inersia dengan koordinat-koordinat ruang-masa rangka inersia lain*]
 - **II.** It is the generalisation of Galilean transformation [*Ia merupakan generalisasi transformasi Galilean*]
 - III. It constitutes one of the Einstein's special relativity postulates

[Ia merupakan salah satu postulat teori kerelatifan khas Einstein]

- **IV.** Its derivation is based on the constancy of the speed of light postulate [*Ia diterbitkan berdasarkan postulat kemalaran kelajuan cahaya*]
- **A.** I,IV **B.** I,II, IV **C.** I, II, III,IV
- D. I, II E. II,III
- ANS: B, my own question
- 1.18 The expression of linear momentum has to be modified in the relativistic limit in order to

[Ekspresi momentum linear kena dimodifikasikan pada limit relativistik supaya]

- I. preserve the consistency between the Lorentz transformation and conservation of linear momentum *[konsistensi antara transformasi Lorentz dengan keabadian momentum linear terpelihara]*
- **II.** preserve the consistency between the Galilean transformation and conservation of linear momentum *[konsistensi antara transformasi Galilean dengan keabadian momentum linear terpelihara]*
- III. preserve the consistency between special relativity with Newtonian mechanics [konsistensi antara kerelatifan khas dengan mekanik Newton terpelihara]
- IV. preserve the consistency between the Lorentz transformation and Galilean transformation [konsistensi antara transformasi Lorentz dengan transformasi Galilean terpelihara]
- A. I only B. I,II, IV C. I, III,IV D. III,IV E. IV only

ANS: A, my own question

Question 2. (25 marks) [Soalan 2 (25 markah)]

2.1 What is the kinetic energy of the fastest photoelectrons emitted by a copper surface, of work function 4.4 eV when illuminated by visible light 0f 700 nm? [Apakah tenaga kinetik fotoelektron paling pantas yang dipancarkan oleh permukaan kuprum, yang fungsi kerjanya 4.4 eV, semasa disinari cahaya

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ternampak 700 nm?]

A. 1.17 eV
B. 6.17 eV
C. 1.17 eV
D. 1.0 eV
E. non of the above [*Tiada dalam pilihan di atas*]

ANS: E, Schaum's 3000 solved problems, Q38.21, pg. 710

2.2 Suppose that a beam of 0.2-MeV photon is scattered by the electrons in a carbon target. What is the wavelength of those photon scattered through an angle of 90°? [Katakan satu bim foton 0.2 MeV diserakkan oleh elektron di dalam sasaran karbon. Apakah jarak gelombang bagi foton yang diserakkan melalui satu sudut 90°?]

A. 0.00620 nm B. 0.00863 nm C. 0.01106 nm D. 0.00243 nm E. non of the above *[Tiada dalam pilihan di atas]* ANS: B, Schaum's 3000 solved problems, Q38.31, pg. 712

2.3 Determine the cut-off wavelength of x-rays produced by 50-keV electrons in a x-ray vacuum tube? [Tentukan jarak gelombang penggal bagi sinar-x yang dihasilkan oleh elektron 50 keV dalam satu tiub sinar-x vakum.]

A. 0.000248 Å
B. 2.48 Å
C. 248 Å
D. 0.248 Å
E. non of the above [*Tiada dalam pilihan di atas]*

ANS: D, Schaum's 3000 solved problems, Q38.39, pg. 714

A lamp emits light of frequency 5.0×10¹⁵ Hz at a power of 25 W. The number of photons given off per seconds is [Suatu lampu memancarkan cahaya berfrekuensi 5.0×10¹⁵ Hz pada kuasa 25 W. Bilangan foton yang dihasilkan per saat ialah]

A. 1.3×10^{-19} **B.** 8.3×10^{-17} **C.** 7.5×10^{18} **D.** 1.9×10^{50}

E. 2.9×10^{13} ANS:C , Modern physical technique, Beiser, MCP 34, pg. 802, modified

- 2.5 Which of the following transitions in a hydrogen atom emits the photon of lowest frequency? [Dalam senarai di bawah, peralihan yang manakah memancarkan foton frekuensi terendah di dalam atom hidrogen?]
 - A. n = 1 to n = 2 B. n = 2 to n = 1 C. n = 2 to n = 6

 D. n = 6 to n = 2 E. n = infinitely large to n = 1 [n = sebesar tak terhingga ke n = 1]

ANS:D, Modern physical technique, Beiser, MCP 40, pg. 802

- 2.6 The speed of an electron whose de Broglie wavelength is 1.0×10^{-10} m is [Kelajuan satu elektron yang jarak gelombang de Broglie-nya 1.0×10^{-10} m ialah
-]

A. 6.6×10^{-24} m/s **B.** 3.8×10^3 m/s **C.** 7.3×10^6 m/s

D. 1.0×10^{10} m/s **E.** 6.6×10^2 m/s ANS:C, Modern physical technique, Beiser, MCP 36, pg. 802

2.7 A large value of the probability density of an atomic electron at a certain place and time signifies that the electron

[Nilai yang besar bagi ketumpatan kebarangkalian suatu elektron atom pada sesuatu tempat dan masa menunjukkan elektron itu]

- A. is likely to be found there [agak mungkin dijumpai di sana]
- **B.** is certain to be found there *[pasti dijumpai di sana]*
- C. has a great deal of energy there [mempunyai banyak tenaga di sana]
- **D.** has a great deal of charge *[mempunyai banyak cas]*
- **E.** is unlikely to be found there

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[tidak berapa mungkin dijumpai di sana]

ANS:A, Modern physical technique, Beiser, MCP 25, pg. 802

- 2.8 Ionisation energy of hydrogen is 13.5 eV. What is the shortest wavelength in the Lyman series of hydrogen atom? [Tenaga pengionan hidrogen ialah 13.5 eV. Apakah jarak gelombang terpendek dalam siri Lyman hidrogen?]
 - **A.** 364 nm **B.** 121 nm **C.** 91 nm **D.** 819 nm

E. 103 nm ANS:C, my own question

2.9 If the momentum of a particle is doubled, its wavelength is multiplied ______ times [Jika momentum suatu zarah digandakan dua, jarak gelombangnya digandakan ______kali]

A. 1 B. 2 C. 1/2 D. 8 E. 0

ANS: C, Machlup, Review question 7, pg. 522, modified

- 2.10 A standing wave cannot have less than _____ antinode. In quantum mechanics, that fundamental mode would be called the ______. [Suatu gelombang pegun tidak boleh mempuyai kurang daripada _____antinod. Dalam mekanik kuantum, mod asas ini dinamakan _____.]
 - A. 1, first excited state [keadaan teruja pertama] [keadaan dasar]
 - C. 2, first excited state [keadaan teruja pertama] [keadaan dasar]
 - E. 0, ground state [keadaan dasar]
 ANS: B, Machlup, Review question 9, pg. 522, modified
- 2.11 Assume that the uncertainty in the position of a particle is equal to its de Broglie wavelength. What is the minimal uncertainty in its velocity, v_x ? [Anggapkan bahawa ketidakpastian dalam kedudukan suatu zarah adalah sama dengan jarak gelombang de Broglie-nya. Apakah ketidakpastian minimum dalam halajunya v_x ?]

A. $v_x/4\pi$ **B.** $v_x/2\pi$ **C.** $v_x/8\pi$ **D.** v_x

E. v_x/π

ANS: A, Schaum's 3000 solved problems, Q38.66, pg. 718

2.12 If the ionisation energy for a hydrogen atom is 13.6 eV, what is the energy of the level with quantum number n = 3?[Jika tenaga pengionan satu atom hidrogen ialah 13.6 eV, apakah tenaga untuk paras yang bernombor kuantum n = 3?]

A. 1.51 eV	B. 3.4 eV	C. 12.1 eV
D. -1.51 eV	E. -3.4 eV	

ANS: D, Schaum's 3000 solved problems, Q39.6, pg. 720

2.13 What is the zero-point energy of an electron trapped in an infinite potential well

of size L = 0.5 A

[Apakah tenaga titik-sifar bagi elektron yang terperangkap di dalam suatu telaga

keupayaan infinit yang saiznya L = 0.5 A]

A. 7.5×10^{-9} eV **B.** 11.7×10^{-6} eV **C.** 0.30×10^{-6} eV

D. 13.6 eV **E.** 65×10^{-6} eV

ANS: 150 eV. Free marks will be given for this question since there is no correct answer in the options.

- 2.14 A moving body is described by the wave function ψ at a certain time and place; ψ^2 is proportional to the body's [Suatu jasad bergerak diperihalkan oleh fungsi gelombang ψ pada suatu masa dan tempat tertentu; ψ^2 adalah berkadar dengan]
 - A. electric field [medan elektrik]
 B. speed [kelajuan]
 C. energy [tenaga]
 D. probability of being found [kebarangkalian untuk dijumpai]
 E. mass [jisim]

ANS:D, Modern physical technique, Beiser, MCP 11, pg. 801

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2.16

2.15 The continuous x-ray spectrum produced in an x-ray tube can be explained by [Keselanjaran spektrum sinar-x yang dihasilkan dalam suatu tiub sinar-x dapat diterangkan oleh]

0	-		
І. П. Ш. IV.	[Teori klasik gelombang keelektromagnetan] II. Pair production [Penghalisan pasangan] III. Bremsstrahlung [Bremsstrahlung]		
A. I,IV	B. I,II, IV	C. I, III,IV	D. I, III
Planck consta [Pemalar Pla			
I.	is a universal constant [ialah satu pemalar universal]		
II.	is the same for all r	netals	7
III.	is different for diffe	erent metals	
IV.	characterises the qu [mencirikan skala k	antum scale	enamanj
A. I,IV	B. I,II, IV	C. I, III,IV	D. I, III
E. II,III			

ANS: B, Machlup, Review question 8, pg. 496, modified

- 2.17 A neon sign produces [Suatu lampu neon menghasilkan]
 - I. a line spectrum [suatu spektrum garis] II. an emission spectrum [suatu spektrum pancaran] III. an absorption spectrum [suatu spektrum penyerapan] IV. photons [foton]

A. I,IV **B.** I,II, IV **C.** I, III,IV **D.** I, III

E. II,III

ANS:B, Modern physical technique, Beiser, MCP 20, pg. 801, modified

- 2.18 Which of the following statements are true? [Kenyataan berikut yang manakah benar?]
 - I.. the ground states are states with lowest energy [keadaan asas adalah keadaan dengan tenaga yang paling rendah]
 - II. ionisation energy is the energy required to raise an electron from ground state to free state [tenaga pengionan adalah tenaga yang diperlukan untuk menaikan suatu elektron dari keadaan asas ke keadaan bebas]
 - **III**. Balmer series is the lines in the spectrum of atomic hydrogen that corresponds to the transitions to the n = 1 state from higher energy states [Balmer siri adalah garis-garis spectrum atom hidrogen yang bersepadanan dengan peralihan dari paras-paras tenaga yang lebih tinggi ke paras n = 1]

A. I,IV **B.** I,II, IV **C.** I, III,IV **D.** I, II

E. II,III

ANS: D, My own question (note: this is an obvious typo error with the statement IV missing. In any case, only statement I, II are true.)

Question 3. (25 marks)

[Soalan 3. (25 markah)]

(a) Lithium, beryllium and mercury have work functions of 2.3 eV, 3.9 eV and 4.5 eV, respectively. If a 400-nm light is incident on each of these metals, determine

[Fungsi kerja Lithium, beryllium dan raksa adalah 2.3 eV, 3.9 eV dan 4.5 eV masing-masing. Jika cahaya 400 nm ditujukan ke atas setiap satu logam itu, tentukan]

- (i) which metals exhibit the photoelectric effect, and [logam yang manakah memperlihatkan kesan fotoelectrik, dan]
- (ii) the maximum kinetic energy for the photoelectron in each case (in eV)

[tenaga kinetik maksimum untuk fotoelektron dalam setiap kes itu (dalam unit eV)]

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	Serway solution manual 2, Q21, pg. 357
(b)	Molybdenum has a work function of 4.2 eV.

- [Fungsi kerja Molybdenum ialah 4.2 eV.]
 - (i) Find the cut-off wavelength (in nm) and threshold frequency for the photoelectric effect. [Carikan jarak gelombang penggal (dalam unit nm) dan frekuensi ambang untuk kesan fotoelektrik]
 - (ii) Calculate the stopping potential if the incident radiation has a wavelength of 180 nm.
 [Hitungkan keupayaan penghenti jika sinaran tuju mempunyai jarak gelombang 180 nm.]

Serway solution manual 2, Q16, pg. 356

(c) A 0.0016-nm photon scatters from a free electron. For what scattering angle of the photon do the recoiling electron and the scattered photon have the same kinetic energy? [Suatu foton 0.0016 nm diserakkan oleh elektron bebas. Apakah sudut serakan foton supaya elektron yang tersentak dan foton yand terserak itu mempunyai tenaga kinetik yang sama?]

Serway solution manual 2, Q35, pg. 358

Solution:

Q3a(i) The energy of a 400 nm photon is $E = hc/\lambda = 3.11 \text{ eV}$ [2 mark]

The effect will occur only in lithium* [2 marks, with or without explanation]

Q3a(ii)

For lithium, $K_{max} = h_V - W_0 = 3.11 \text{ eV} - 2.30 \text{ eV} = 0.81 \text{ eV}^*$ [3 marks]

[Note*: for Q3a(i,ii), the full 2+2+3 marks only for the unique answer set {lithium, $K_{max} = 0.81$ eV}. Minus 2 marks for any extra answer set involving other metals]

Q3b(i)

Cut-off frequency = $\lambda_{cutoff} = hc/W_0$ = 1240 nm eV / 4.2 eV = **295 nm** Cut-off frequency (or threshold frequency)= $v_{cutoff} = c/\lambda = 1.01 \times 10^{15}$ Hz [3 + 3 marks]

Q3b(ii)

Stopping potential $V_{stop} = (hc/\lambda - W_0) / e = (1240 \text{ nm.eV}/180 \text{ nm} - 4.2 \text{ eV})/e = 2.7 \text{ V}$

[3 marks]

Q3c

The energy of the incoming photon is $E_i = hc/\lambda = 0.775 \text{ MeV}$ [3 mark]

Since the outgoing photon and the electron each have half of this energy in kinetic form, $E_o = hc/\lambda' = 0.775 \text{ MeV} / 2 = 0.388 \text{ MeV} and$ $\lambda' = hc/E_o = 1240 \text{ eV}. \text{ nm} / 0.388 \text{ MeV} = 0.0032 \text{ nm}$ The Compton shift is $\Delta \lambda = \lambda' - \lambda = (0.0032 - 0.0016) \text{ nm} = 0.0016 \text{ nm}$

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[3 marks]
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By \Delta \lambda = \lambda_c (1 - \cos \theta) = h/m_e c (1 - \cos \theta)

0.0016 \text{ nm} = 0.00243 \text{ nm} (1 - \cos \theta)

\Rightarrow \theta = 70^\circ

[3 marks]
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Question 4. (25 marks) [Soalan 4. (25 markah]

- (a) An electron is contained in a one-dimensional box of width 0.100 nm. Using the particle-in-a-box model, [Suatu elektron terkandung di dalam satu kotak satu dimensi yang lebarnya 0.100 nm. Dengan menggunakan model zarah-dalam-satu-kotak]
 - (i) Calculate the n = 1 energy level and n = 4 energy level for the electron in eV.
 [Hitungkan paras tenaga n = 1 dan n = 4 untuk elektron itu dalam unit eV.]
 - (ii) Find the wavelength of the photon (in nm) in making transitions that will eventually get it from the the n = 4 to n = 1 state [*Hitungkan jarak gelombang foton (dalam unit nm) semasa ia membuat peralihan yang membawanya dari keadaan* n = 4 *ke keadaan* n = 1]

Serway solution manual 2, Q33, pg. 380, modified

- (b) Consider a 20-GeV electron. [Pertimbangkan suatu elektron 20 GeV.]
 - (i) What is its Lorentz factor γ ? [Apakah faktor Lorentznya?]
 - (ii) What is its de Broglie wavelength? [Apakah jarak gelombang de Broglie-nya?]
 Serway solution manual 2, Q12, pg. 376, modified

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- (c) A photon is emitted as a hydrogen atom undergoes a transition from the n = 6 state to the n = 2 state. Calculate [Suatu foton dipancarkan ketika suatu atom hidrogen melakukan satu peralihan dari keadaan n = 6 ke n = 2. Hitungkan]
 - (i) the energy [tenaga]
 (ii) the wavelength [jarak gelombang]
 (iii) the frequency [frekuensi]
 of the emitted photon
 - [foton yang dipancarkan]

Serway solution manual 2, Q47, pg. 360, modified

Solution:

Q4a(i) In the particle-in-a-box model, standing wave is formed in the box of dimension *L*: $\lambda_n = \frac{2L}{n}$ [1 marks]

The energy of the particle in the box is given by

$$K_n = E_n = \frac{p_n^2}{2m_e} = \frac{(h/\lambda_n)^2}{2m_e} = \frac{n^2 h^2}{8m_e L^2} = \frac{n^2 \pi^2 \hbar^2}{2m_e L^2}$$

[2 marks]

$$E_1 = \frac{\pi^2 \hbar^2}{2m_e L^2} = 37.7 \text{ eV}$$
[2 mark]

 $E_4 = 4^2 E_1 = 603 \text{ eV}$ [2 mark]

Q4a(ii)

The wavelength of the photon going from n = 4 to n = 1 is $\lambda = hc/(E_6 - E_1)$ = 1240 eV nm/ (603 – 37.7) eV = **2.2 nm** [2 marks]

Q4b(i)

From $E = \gamma m_e c^2$, $\gamma = E/m_e c^2 = 20 \text{ GeV}/0.51 \text{ MeV} = 39216$ [4 marks]

Q4b(ii)

Momentum p = E/c = 20 GeV/c (rest mass of electron ignored, $m_e c^2 \ll E$) $\lambda = hc/E = hc/pc = 1240 \text{ eV nm} / 20 \text{ GeV} = 6.2 \times 10^{-17} \text{ m}$ [3 marks]

O4c

For hydrogen,
$$E_n = -\frac{13.6}{n^2} eV$$

Q4c(i)
 $\Delta E_{6\to 2} = E_6 - E_2 = -13.6 \left(\frac{1}{6^2} - \frac{1}{2^2}\right) eV = 3.02 eV$

[3 marks]

O4c(ii)

 $\lambda_{6\to 2} = hc / \Delta E_{6\to 2} = 1240$ nm · eV / 3.02eV = 410 nm [3 marks]

O4c(iii)

 $v = c/\lambda = 7.32 \text{ x } 10^{14} \text{ Hz}$ [3 marks]

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UNIVERSITI SAINS MALAYSIA

KSCP Academic Session 2003/2004

April 2004

ZCT 104E/3 - Physics IV (Modern Physics) [Fizik IV (Fizik Moden)]

Duration: 3 hours [Masa: 3 jam]

Please check that the examination paper consists of ELEVEN pages of printed material before you begin the examination.

[Sila pastikan bahawa kertas peperiksaan ini mengandungi SEBLELAS muka surat vang bercetak sebelum anda memulakan peperiksaan ini.]

Instruction: Answer all FOUR (4) questions.

Students are allowed to answer all questions in Bahasa Malaysia or in English.

Please answer Question 1 in the objective answer form provided. Submit the objective answer form and the answers to the structured questions (i.e. O2 - O4) separately.

[Arahan: Jawab kesemua EMPAT soalan. Pelajar dibenarkan menjawab semua soalan sama ada dalam Bahasa Malaysia atau Bahasa Inggeris. Sila jawab Soalan 1 dalam kertas jawapan objecktif yang dibekalkan. Hantar kertas jawapan objecktif dan jawapan kepada soalan struktur (iaitu Soalan 2 – Soalan 4) berasingan.]

Data

speed of light in free space, $c = 3.00 \text{ x} 10^8 \text{ m s}^{-1}$ permeability of free space, $\mu_0 = 4\pi \times 10^{-7} \text{ H m}^{-1}$ permittivity of free space. $\varepsilon_0 = 8.85 \text{ x } 10^{-12} \text{ F m}^{-1}$ elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$ the Planck constant, $h = 6.63 \times 10^{-34} \text{ J s}$ unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$ rest mass of electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$ rest mass of proton, $m_p = 1.67 \times 10^{-27} \text{ kg}$ molar gas constant, = 8.31 J K⁻¹ mol⁻¹ the Avogadro constant, $N_{\rm A} = 6.02 \text{ x } 10^{23} \text{ mol}^{-1}$ gravitational constant, $G = 6.67 \text{ x } 10\text{-}11 \text{ N m}^2 \text{ kg}^{-2}$ acceleration of free fall, $g = 9.81 \text{ m s}^{-2}$

Q1. [25 marks]

- 1.1 What were the consequences of the negative result of the Michelson-Morley experiment? [Antara berikut yang manakah akibat keputusan negatif eksperimen Michelson-Morley?]
 - I. It render untenable the hypothesis of the ether [*Ia menjadikan hipotesis ether tidak dapat dipertahankan*]
 - II. It suggests the speed of light in the free space is the same everywhere, regardless of any motion of source or observer [Ia mencadangkan bahawa laju cahaya dalam ruang bebas adalah sama di mana-mana sahaja, tidak kira sama ada punca cahaya atau pemerhati mempunyai sebarang pergerkan]
 - **III.** It implies the existence of a unique frame of reference in which the speed of light in this frame is equal to *c* [*Ia mengimplikasikan kewujudan suatu rangka rujukan yang laju cahaya dalam rangka tersebut adalah bersamaan dengan c*]

A. III only B. I,II C. I, III D. I, II, III E. Non of the above [*Tiada dalam pilihan di atas*]

Ans: B

Murugeshan, S. Chand & Company, New Delhi, pg. 25, Q1.

- **1.2** Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I. The expression for kinetic energy of a relativistic particle is given by $\frac{1}{2}mv^2$

[Ekspresi tenaga kinetic suata zarah kerelatifan ialah $\frac{1}{2}mv^2$]

- **II.** Special theory of relativity is applicable to accelerating system [Teori kerelatifan khas boleh dipergunakan ke atas sistem yang mengalami pecutan]
- **III.** The maximal velocity ever attainable is that of light in free space [Laju maksimum yang mungkin tercapai ialah laju cahaya dalam ruang bebas]
- IV. The mass of a particle becomes infinite at the speed equal to *c* [Jisim suatu zarah menjadi infinit pada kelajuan bersamaan dengan c]

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A. II.III	B. I.II.III.IV	C. I. II. III	D. III. IV

E. Non of the above [Tiada dalam pilihan di atas]

Ans: D

Murugeshan, S. Chand & Company, New Delhi, pg. 18, Q23.(for I), pg. 26, Q5.(for II), pg. 27, Q12.(for III), pg. 27, Q14.(for IV),

- **1.3** Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I The concept of Bohr orbit violates the uncertainty principle [Konsep orbit Bohr melanggar prinsip ketidakpastian]
 - II A hydrogen atom has only a single electron [Atom hidrogen mempunyai satu elektron tunggal sahaja]
 - III The spectrum of hydrogen consists of many lines even though a hydrogen atom has only a single electron [Spektrum hidrogen terdiri daripada banyak pinggir (garisan) walaupun atom hidrogen hanya mempunyai satu elektron sahaja]
 - IV Most of an atom consists of empty space [Kebanyakan daripada isipadu suatu atom terdiri daripada ruang kosong]
 - A. I,II B. I,II,III,IV C. I, II, III D. III, IV E. Non of the above *[Tiada dalam pilihan di atas]*

Ans: D

Murugeshan, S. Chand & Company, New Delhi, pg. 86, Q13.(for I), pg. 88, Q19.(for II,III), pg. 87, Q11.(for IV)

- 1.4 Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I In the Bohr theory of the hydrogen atom, the potential energy of the orbiting electron is positive [Dalam teori atom hidrogen Bohr, tenaga keupayaan elektron yang mengorbit ialah positif]
 - II In the Bohr theory of the hydrogen atom, the kinetic energy of the orbiting electron is positive [Dalam teori atom hidrogen Bohr, tenaga kinetik elektron yang mengorbit ialah positif]
 - **III** In the Bohr theory of the hydrogen atom, the potential energy of the orbiting electron is negative

[Dalam teori atom hidrogen Bohr, tenaga keupayaan elektron yang mengorbit ialah negatif]

IV. In the Bohr theory of the hydrogen atom, the kinetic energy of the orbiting electron is negative [Dalam teori atom hidrogen Bohr, tenaga kinetik elektron yang mengorbit ialah negatif]

A. I,II	B. III,IV	C. I, IV	D. II, III
E. Non of t	he above [Tiada da	lam pilihan di atas]	

Ans: D

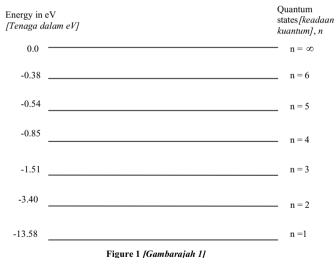
Murugeshan, S. Chand & Company, New Delhi, pg. 91, Q36

Q1.5 – Q1.7 refers to the energy diagrams shown in Figure 1.

[Soalan 1.5 - Soalan 1.7 merujuk kepada gambarajah yang terpapar di Gambarajah 1.]

Some of the energy levels of the hydrogen atom are shown (not to proportion)

[Beberapa paras tenaga atom hidrogen dipaparkan seperti berikut (tidak mematuhi nisbah)]



1.5 How much energy in eV is required to raise an electron from the ground state to the n = 5 state? (ignore selection rules) [Apakah tenaga (dalam unit eV) yang diperlukan untuk menaikkan suatu elektron dari keadaan bumi ke keadaan n = 5? (abaikan petua pilihan)]

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1.6

1.7

1.8

A. 13.58 E. Non of the al	B. 10.18 bove [Tiada dalam]	C. 12.73 pilihan di atas]	D. 13.04	
	Ans: D Murugeshan, S. Chand & Company, New Delhi, pg. 92, Q44, modified; Diagram adopted from Gautreau and Savin, Schaum's series, pg. 105.			
electron makes [Apakah angga	What is the approximate wavelength of photon (in nm) emitted when the electron makes a transition from state $n = 6$ to $n = 2$? (ignore selection rules) [Apakah anggaran jarak gelombang (dalam unit nm) untuk foton yang terpancar semasa elektron beralih dari keadaan $n = 6$ ke $n = 2$? (abaikan petua pilihan)]			
A. 91 E. Non of the al	B. 122 bove [Tiada dalam]	C. 94 pilihan di atas]	D. 410	
Ans: D My own questic	on			
undergoes trans rules) [Terdapat berap mengalami perc	How many different photons can be emitted by the hydrogen atom that undergoes transitions to the $n = 4$ state from the $n = 6$ state? (ignore selection rules) [Terdapat berapa foton berbeza yang terpancar oleh atom hidrogen yang mengalami peralihan ke keadaan $n = 6$ dari keadaan $n = 4$? (abaikan petua			
	B. 4 C. 1 bove [Tiada dalam]	D. 6 pilihan di atas]		
Ans: A Murugeshan, S. Chand & Company, New Delhi, pg. 90, Q30, modified				
In relativity, which of the following observable(s) is (are) not absolute but depend on the reference frame of observer? [Dalam teori kerelatifan, pembolehcerap yang mana adalah tidak mutlak tetapi bersandar kepada rangka rujukan pemerhati?]				
I. Space II. Time III. Mass				

IV. Energy

A. I,II B. I,II,III,IV C. I, II, III D. III,IV E. Non of the above /Tiada dalam pilihan di atas]

Ans: B

Murugeshan, S. Chand & Company, New Delhi, pg. 28, Q23.

- **1.9** Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - γ-rays have much shorter wavelength than x-rays [Jarak gelombang sinar γ adalah jauh lebih pendek daripada jarak gelombang sinar x]
 - II. The wavelength of *x*-rays in a *x*-ray tube can be controlled by varying the accelerating potential *[Jarak gelombang sinar x dalam suatu tiub sinar x dapat dikawal dengan menyelaraskan beza upaya pecutan]*
 - III. *x*-rays are electromagnetic waves [Sinar x ialah gelombang elektromagnetik]
 - IV. x-rays show diffraction pattern when passing through crystals [Sinar x memperlihatkan corak belauan semasa ia melalui hablur]

 A. I,II
 B. I,II,III,IV
 C. I, II, III
 D. III.IV

 E. Non of the above [Tiada dalam pilihan di atas]

Ans: B

Murugeshan, S. Chand & Company, New Delhi, pg. 132, Q1.(for I), pg. 132, Q3 (for II), pg. 132, Q4 (for III,IV)

- **1.10** Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I. Photoelectric effect arises due to the absorption of electrons by photons [Kesan fotoelektrik muncul kerana penyerapan elektron oleh foton]
 - **II.** Compton effect arises due to the scattering of photons by free electrons [Kesan Compton muncul kerana penyerakan foton oleh elektron bebas]
 - **III.** In the photoelectric effect, only part of the energy of the incident photon is lost in the process [Dalam kesan fotoelektrik, hanya sebahagian daripada tenaga foton tuju terlesap dalam proses tersebut]
 - IV. In the Compton effect, the photon completely disappears and all of its energy is given to the Compton electron [Dalam kesan Compton, foton hilang langsung dan kesemua tenaganya diberikan kepada elektron Compton]

A. I,II B. II,III,IV C. I, II, III D. III,IV

Ans: E [I = false; II = true; III = false; IV = false] Murugeshan, S. Chand & Company, New Delhi, pg. 134, Q13,

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- **1.11** Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I. Compton effect is experimentally observed for visible light rays [Kesan Compton boleh dicerap secara eksperimen bagi cahaya ternampak]
 - II. The presence of the unmodified line in Compton scattering can be explained in terms of Rayleigh scatterings [Kehadiran pinggir (garisan) yang tidak terubah dalam penyerakan Compton dapat diterangkan dengan penyerakan Rayleigh]
 - III. In Compton scattering, one neglects the effect of the nucleus on the x-rays [Dalam penyerakan Compton, kita mengabaikan kesan ke atas sinar x oleh nucleus]
 - A. II, III B. I, III C. I, II, III D. II only E. Non of the above *[Tiada dalam pilihan di atas]*

Ans: A

Murugeshan, S. Chand & Company, New Delhi, pg. 134, Q14 (for I), Q15 (for II), Q16 (for III),

- **1.12** Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I The energy of the quantum of light is proportional to the frequency of the wave model of light [Tenaga kuantum cahaya adalah berkadar dengan frekuensi model gelombang cahaya]
 - II In photoelectricity, the photoelectrons has as much energy as the quantum of light which causes it to be ejected [Dalam kesan fotoelektrik, fotoelektron mempunyai tenaga sebanyak tenaga kuantum cahaya yang menyebabkan fotoelektron terlenting]
 - III In photoelectricity, no time delay in the emission of photoelectrons would be expected in the quantum theory [Dalam teori kuantum, tiada tunda masa dalam pemancaran fotoelektron dijangkakan untuk kesan fotoelektrik]

A. II, IIIB. I, IIIC. I, II, IIID. I ONLYE. Non of the above [Tiada dalam pilihan di atas]

Ans: B

Murugeshan, S. Chand & Company, New Delhi, pg. 136, Q28 (for I), Q29, Q30 (for II,III)

1.13 An electron, proton and an alpha-particle have the same de Broglie wavelength. Which one moves faster? *[Elektron, proton dan zarah alpha ketiga-tiganya mempunyai jarak gelombang de Broglie yang sama. Yang manakah bergerak dengan lebih pantas?]*

A. Electron B. Proton C. Alpha-particle
D. All particles move at the same speed [kesemua zarah bergerak dengan kelajuan yang sama]
E. Non of the above [Tiada dalam pilihan di atas]

Ans: A

Murugeshan, S. Chand & Company, New Delhi, pg. 163, Q3

- **1.14** Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I. The de Broglie wavelengths of macroscopic bodies are generally too tiny to be experimentally detected [Jarak gelombang de Broglie jasad makroskopik secara amnya adalah terlalu kecil untuk dikesan secara eksperimen]
 - **II.** If Planck's constant were smaller than it is, quantum phenomena would be more conspicuous than they are now [Jika nilai pemalar Planck adalah lebih kecil daripada nilainya yang sedia ada, fenomena kuantum akan menjadi lebih sedia tercerap berbanding dengan ketercerapannya yang sedia ada]
 - III In quantum theory, the physical variables (e.g. energy, momentum) used to describe a confined electron are discrete [Dalam teori kuantum, pembolehubah fizikal (misalnya tenaga dan momentum) yang memerihalkan sesuatu elektron yang terkurung adalah diskrit

 A. II, III
 B. I ONLY
 C. I, II, III
 D. I, III

 E. Non of the above [Tiada dalam pilihan di atas]
 D. I, III

Ans: D

Murugeshan, S. Chand & Company, New Delhi, pg. 163, Q1 (for I), Q12 (for II), Q21 (for III)

1.15 Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]

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I. The experimental proof for which electron posses a wavelength $\lambda = \frac{h}{n}$

was first verified by Davisson and Germer [Pembuktian scara eksperimen bahawa elektron mempunyai jarak gelombang $\lambda = \frac{h}{p}$ pada mula-mulanya ditentukan oleh Davisson and Germer]

- II. The experimental proof of the existence of discrete energy levels in atoms involving their excitation by collision with low-energy electron was confirmed in the Frank-Hertz experiment [Pembuktian secara eksperimen kewujudan paras tenaga diskrit dalam atom yang melibatkan pengujaan mereka oleh perlanggaran dengan elektron bertenaga rendah telah dipastikan dalam eksperimen Frank-Hertz]
- III. Compton scattering experiment establishes that light behave like particles [Penyerakan Compton menetapkan bahawa cahaya berlagak seperti zarah]
- IV. Photoelectric experiment establishes that electrons behave like wave [Kesan fotoelektrik menetapkan bahawa elektron berlagak seperti gelombang]
- A. I,IIB. I,II,III,IVC. I, II, IIID. III,IVE. Non of the above [Tiada dalam pilihan di atas]

Ans: C

Serway and Moses, pg. 127 (for I), pg. 133 (for II), own options (for III,IV)

Q2. [25 marks]

(a) A man in a spaceship moving at a velocity of 0.9*c* with respect to the Earth shines a light beam in the same direction in which the spaceship is travelling.

[Seorang yang berada di dalam satu kapal angkasa yang bergerak pada halaju 0.9c relatif kepada Bumi menyinarkan satu bim cahaya ke arah yang mana kapal angkasa itu sedang bergerak.]

Compute the velocity of the light beam relative to Earth using [Hitungkan halaju bim cahaya itu relatif kepada Bumi dengan menggunakan]

(i) Galilean approach [pendekatan Galileo]

[3 marks]

(ii) Special relativity approach [pendekatan teori kerelatifan khas]

[6 marks]

Please define clearly all the symbols used in your working. [Sila nyatakan dengan jelas definasi simbol-simbol yang digunakan dalam kerja anda.] Ans

(a) O' is the moving frame travelling at v = 0.9c with respect to the Earth. Speed of the light beam as seen in the frame O' is u' = c. O is the Earth frame. We wish to find the speed of the light beam as seen from frame O, u.

(i) According to Galilean transformation, u = u' + v = c + 0.9c = 1.9c.

(ii) Use $u = \frac{u' + v}{c + 0.9c}$

$$u = \frac{u}{1 + \left(\frac{v}{c^2}\right)u'} = \frac{c}{1 + \left(\frac{0.9c}{c^2}\right)c} = c \implies v = c$$

Acosta, Q4-7, pg. 53, modified

(b) How fast does a rocket have to go for its length to be contracted to 99% of its rest length? [Berapa cepatkah suatu roket harus bergerak supaya panjangnya menyusut kepada 99% daripada panjang rehatnya?]

[5 marks]

Ans:

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$$\frac{L}{L_0} = 0.99 = \sqrt{1 - \left(\frac{v}{c}\right)^2}$$

 $\Rightarrow v = 0.141c$

Gautreau and Savin, Schaum's series modern physics, pg.21, Q. 4.1

(c) The average lifetime of μ-meson with a speed of 0.95c is measured to be 6×10⁻⁶ s. Compute the average lifetime of μ-meson in a frame in which they are at rest.
 [Hayat purata meson-μ yang bergerak dengan kelajuan 0.95c adalah

diukur sebagai 6×10⁻⁶ s. Hitungkan hayat purata meson-µ dalam rangka di mana mereka adalah rehat] [5 marks]

Ans:

Lorentz factor is
$$\gamma = \frac{1}{\sqrt{1 - \left(\frac{v}{c}\right)}} = \frac{1}{\sqrt{1 - (0.95)}} = 3.20$$

The time measured in a frame in which the μ -mesons are at rest is the proper time, Δt_0 :

 $\Delta t_0 = \Delta t / \gamma = = 6 \times 10^{-6} \text{ s}/3.2 = 1.87 \times 10^{-6} \text{ s}$

Gautreau and Savin, Schaum's series modern physics, pg.24, Q 5.1

- (d) (i) What is the rest mass of a proton in terms of MeV? [Apakah jisim rehat satu proton dalam unit MeV?] [2 marks]
 - (ii) What is the relativistic mass of a proton (in terms of MeV) whose kinetic energy is 1 GeV? [Apakah jisim kerelatifan satu proton (dalam unit MeV) yang bertenaga kerelatifan 1 GeV?]

[4 marks]

Ans:

- (i) $m_p c^2 = 1.67 \times 10^{-27} \text{kg x} (3 \times 10^8 \text{ m/s})^2 = 1.503 \times 10^{-10} \text{ J} = 1.503 \times 10^{-10} / (1.6 \times 10^{-19}) \text{ eV} = 939.4 \text{ MeV}$
- (ii) $K = (\gamma 1)m_pc^2 = 1 \text{ GeV}$ $(\gamma - 1) = 1 \text{ GeV}/m_pc^2 = 1 \text{ GeV}/939.4 \text{ MeV} = 1.06$ $\gamma = 1.06 + 1 = 2.06$ $mc^2 = \gamma m_pc^2 = 2.06 \times 939.4 \text{ MeV} = 1939.4 \text{ MeV}$

Note: Due to the inconsistency between the English and Malay version of question I would also give full mark to those who used total relativisic energy $E = \gamma m_{p}c^{2} = 1$ GeV in the calculation (instead of using $K = (\gamma - 1)m_{p}c^{2} = 1$ GeV).

Gautreau and Savin, Schaum's series modern physics, pg.55, Q 8.34, slightly modified.

Q3. [25 marks]

(a) A proton is accelerated from rest through a potential of 1 kV. Find its de Broglie wavelength.
 [Suatu proton dipecutkan dari keadaan rehat melalui satu beza keupayaan 1 keV. Hitungkan jarak gelombang de Broglienya.]

[6 marks]

Ans.

$$K = \frac{p^2}{2m_p} = \text{kinetic energy of the proton} = 1 \text{ keV.}$$
$$\lambda = \frac{h}{p} = \frac{h}{\sqrt{2m_p K}} = \frac{h}{\sqrt{2m_p K}} = \frac{6.63 \times 10^{-34} \text{ J} \cdot \text{s}}{\sqrt{2 \times 1.67 \times 10^{-27} \text{ kg} \cdot 1000 \times 1.6 \times 10^{-19} \text{ J}}} = 9.1 \times 10^{-3} \text{ Å}$$

Gautreau and Savin, Schaum's series modern physics, pg.97, Q. 10.38

(b) Determine the cutoff wavelength in Å of x-rays produced by a 50-keV electrons in a x-ray tube.

[Tentukan jarak gelombang penggal (dalam unit $\overset{\circ}{A}$) sinar x yang dihasilkan oleh elektron 50 keV dalam suatu tiub sinar x.] [5 marks]

Ans.

$$\lambda_{cutoff} = \frac{hc}{eV} = \frac{1240 \text{eV} \cdot \text{nm}}{50 \text{keV}} = 0.0248 \text{nm} = 0.24 \text{ Å}$$

Schaum's series 3000 solved problem, pg.714, Q. 38.39

(c) Determine the photon flux (in unit of number of photons per unit time per unit area) associated with a beam of monochromatic light of

wavelength 3000 Å and intensity 3×10^{-14} W/m².

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[Tentukan fluks foton (dalam unit bilangan foton per unit masa per unit luas) yang bersepadanan dengan suatu bim cahaya monokromatik

berjarak gelombang 3000 $\stackrel{o}{A}$ dan berkeamatan $3 \times 10^{-14} \text{ W/m}^2$.]

[8 marks]

Ans:

N

$$= I/\varepsilon = I \cdot \left(\frac{\lambda}{hc}\right)$$

= 3×10⁻¹⁴ W/m² × $\frac{300 \text{ nm}}{1240 \text{ eV} \cdot \text{ nm}}$
= 7.26×10⁻¹⁵ $\left(\frac{W}{\text{ eV}}\right)$ /m² = 7.26×10⁻¹⁵ (6.25×10¹⁸ / s)/m² = 45375 photon / m² · s

Gautreau and Savin, Schaum's series modern physics, pg.98, Q. 10.53

(d) Suppose that the x-component of the velocity of a 2×10⁻⁴ kg mass is measured to an accuracy of ±10⁻⁶ m/s. What is the limit of the accuracy with which we can locate the particle along the x-axis? [Andaikan bahawa komponen x halaju suatu jasad berjisim 2×10⁻⁴ kg diukur tepat kepada kejituan ±10⁻⁶ m/s. Apakah limit kejituan kedudukannya yang boleh kita pastikan sepanjang paksi-x?] [6 marks]

Ans.

$$\Delta p \Delta x \ge \frac{\hbar}{2}; \ p = mv;$$

$$\Delta (mv) \Delta x = m \Delta v \Delta x \ge \frac{\hbar}{2}$$

$$\Delta x \ge \frac{\hbar}{2m\Delta y} = \frac{h}{4\pi m\Delta y} = 2.63 \times 10^{-25} \,\mathrm{m}$$

Gautreau and Savin, Schaum's series modern physics, pg.98, Q. 10.53

Q4. [25 makrs]

(a) Given the ground state energy of hydrogen atom -13.6 eV, estimate the ionisation energy for He⁺.
 [Diberi bahawa tenaga keadaan bumi atom hidrogen ialah -13.6 eV, anggarkan tenaga pengionan untuk He⁺.]
 [5 marks]

Ans: Generally, the energy state of an hydrogen-like atom with Z charge in its nucleus is given by $E_n = \frac{Z^2}{n^2} E_0$, $E_0 =$ ground state energy of hydrogen atom.

Hence ionisation energy of He⁺ (with Z = 2) = E_{∞} (He⁺) - E_0 (He⁺) = 0 - $\frac{2^2}{1^2}E_0$ = -4(-13.6) eV = 54.4 eV

(b) What are the n values in the transition that produces the third longest wavelength in the Balmer series in the hydrogen atom? (ignore selection rules) [Apakah nilai-nilai n yang peralihannya menghasilkan jarak gelombang yang ketiga paling panjang dalam siri Balmer atom hidrogen? (abaikan petua pilihan)]

[4 marks]

Ans: $n = 5 \rightarrow n = 2$ Giancoli, pg. 856, Q. 50, modified.

(c) Given the Bohr radius of the hydrogen atom $r_0 = 0.5 \stackrel{o}{A}$, estimate the speed (in m/s) of the electron in the ground state orbit of the hydrogen atom.

[Diberi bahawa radius Bohr atom hidrogen ialah $r_0 = 0.5$ Å, anggarkan laju (dalam m/s) elektron dalam orbit keadaan bumi atom hidrogen.]

[8 marks]

Ans: Equating the centrepetal force required by the electron to the electrostatic force,

$$\frac{mv^2}{r} = \frac{e^2}{4\pi\varepsilon_0 r^2} \Rightarrow v_0^2 = \frac{e^2}{4\pi\varepsilon_0 mr_0} \Rightarrow v_0 = \sqrt{\frac{e^2}{4\pi\varepsilon_0 mr_0}} = 2.25 \times 10^6 \,\mathrm{m/s}$$

My own question

(d) Given the Rydberg constant
$$R = 1.0967758 \ge 10^{-3} \text{ A}^{\circ^{-1}}$$
, determine, in

Α,

- (i) the shortest, and
- (ii) the longest

wavelengths of the Lyman series of hydrogen.

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[Diberi bahawa pemalar Rydberg ialah R =
$$1.0967758 \times 10^{-3} \text{ \AA}^{\circ^{-1}}$$

Tentukan, dalam unit $\overset{\circ}{A}$, jarak gelombang yang

(i) paling pendek, dan(ii) paling panjang

dalam siri Lyman hidrogen]

[4 + 4 marks]

Ans:

(i) Wavelengths in the Lyman series are given by $n_l = 1$ $\frac{1}{\lambda} = R\left(\frac{1}{1^2} - \frac{1}{n^2}\right), n = 2,3,4...$

(ii) The longest wavelength corresponds to
$$n = 2$$
:

$$\frac{1}{\lambda_{\text{max}}} = \left(1.097 \times 10^{-3} \text{ \AA}^{-1}\right) \left(\frac{1}{1^2} - \frac{1}{2^2}\right), \text{ or } \lambda_{\text{max}} = 1215 \text{ \AA}^{-1}$$

The longest wavelength corresponds to $n \to \infty$

$$\frac{1}{\lambda_{\min}} = \left(1.097 \times 10^{-3} \text{ Å}^{-1}\right) \left(\frac{1}{1^2} - \frac{1}{\infty^2}\right), \text{ or } \lambda_{\max} = 912 \text{ Å}$$

Gautreau and Savin, Schaum's series modern physics, pg.107, Q. 11.1

ZCT 104/3E Modern Physics Semester II, Sessi 2004/05 Test I (17 Dec 2004)

Data

Speed of light in free space, $c = 3.00 \times 10^8 \text{ ms}^{-1}$ Elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$ The Planck constant, $h = 6.63 \times 10^{-34} \text{ J} \text{ s}$ Unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$ Rest mass of electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$ Rest mass of proton, $m_p = 1.67 \times 10^{-27} \text{ kg}$

- What are the major flaws in the classical model of blackbody radiation given by Rayleigh-Jeans laws? I (F) Molecular energy is quantized
 - **II (F)** Molecules emit or absorb energy in discrete irreducible packets
 - III(T) The intensity of short wavelength radiation emitted by a blackbody approaches infinity as the wavelength decreases.
 IV (T) Energy is continuously divisible
 - iv (i) Energy is continuously divisible

A. III, IV B. I, II,III C. II, III, IV D. I, II E. Non of the above

ANS:A, Serway, questions 1, 2, page 1313

- 2. What are the assumptions did Planck make in dealing with the problem of radiation?
 - I (T) Molecular energy is quantized
 - II (T) Molecules emit or absorb energy in discrete irreducible packets
 - **III(F)** The intensity of short wavelength radiation emitted by a blackbody approaches infinity as the wavelength decreases.
 - IV (F) Energy is continuously divisible

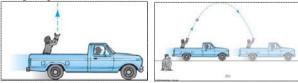
A. III, IV B. I, II,III C. II, III, IV D. I, II E. Non of the above

ANS:D, Serway, questions 1, 2, page 1313

3. An unstable high-energy particle enters a detector and leaves a track of length d before it decays. Its speed relative to the detector was v = c/2. What is its proper lifetime? That is how long would the particle have lasted before decay had it been at rest with respect to the detector?

A.
$$\frac{d}{c}$$
 B. $\frac{4d}{\sqrt{3c}}$ C. $\frac{2d}{\sqrt{3c}}$ D. $\frac{\sqrt{3d}}{c}$ E. Non of the above
RHW 7th ed. P5, pg. 1050
Solution: D

4. A ball was thrown upward by an observer in a van moving with constant speed *u* << *c*. He is observed by an observer in a rest frame attached to the ground, see figure below. Which of the following statement(s) is (are) true regarding the two inertial frames of reference?



I The ball thrown follows different path

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- II The kinematical laws of classical mechanics are valid only the moving frame (the van) but not to the rest frame attached to ground.
- III Classically Galilean transformation relates the trajectory of the ball in the rest frame with that in the moving frame.
- IV Since $u \ll c$, Lorentz transformation will fail to relate the trajectory of the ball in the rest frame with that in the moving frame.

A. II,III B. I, II,III C. II, III, IV D. I Only E. Non of the above My own question Solution: E (I, III are true)

5. What measurement(s) do two observers in relative motion always agree on? I The relativistic mass of an object II The relativistic momentum of an object III The relativistic energy of an object IV $E^2 - p^2$, where p is the magnitude of relativistic momentum and E the relativistic energy the object

A. II,III B. I, II,III C. II, III, IV D. IV Only E. Non of the above

My own question Solution: D

Free marks will be given for this question due to the typo in IV. It should actually reads: " $E^2 - c^2 p^2$, where p is the ".

Actually, the original statement is dimensionally correct in the natural unit system in which the c is taken to have a value of 1. However since we are adopting S.I. unit throughout the course we will take the original statement to be 'dimensionally wrong' as far as the ZCT 104 courses is concerned.

6. Which of the following statement(s) is (are) true?

I The upper limit of the speed of an electron is the speed of light *c*.

II As more energy E is fed into an object its momentum approaches $\frac{E}{2}$.

III There is no upper limit to the relativistic momentum of an electron. **IV** There is an upper limit to the relativistic momentum of an electron.

A. III B. I, II,III C II, IV D. IV Only E. Non of the above Serway Q12, pg. 1276 Solution: B

 The rest energy and total energy respectively, of three particles, expressed in terms of a basic amount *A* are (1) *A*, 2*A*; (2) *A*, 3*A*; (3) 3*A*, 4*A*. Without written calculation, rank the particles according to their kinetic energy, greatest first.

A. 2 > 1 = 3 E. 3 > 1 = 2 B. 1 > 2 = 3 C. 2 > 1 > 3 D. 2 = 1 = 3

RHW 7th ed. Q1, pg. 1050 Solution: A

8. The length of a spaceship is measured to be exactly half its rest length. By what factor do the spaceship's clocks run slow relative to clocks in the observer's frame?

A. 0.866 B. 0.745 C. 2.000 D. 0.366 E. 0.134

SESSI 04/05/TEST1 Solution: C

9. The length of a spaceship is measured to be exactly half its rest length. What is the speed parameter $\beta = v/c$ of the spaceship relative to the observer's frame?

A. 0.87 B. 2.00 C. 0.75 D. 2.73 E. 4.00 ANS: A We solve $L = L_0 \sqrt{1 - \left(\frac{\nu}{c}\right)^2} = L_0 \sqrt{1 - \beta} = \frac{L_0}{\gamma}$ for ν and then plug in: $\beta = \sqrt{1 - \left(\frac{L}{L_0}\right)^2} = \sqrt{1 - \left(\frac{1}{2}\right)^2} = 0.866.$ Resnick and Halliday, 7th edition, Problem 12, Pg. 1051

10. Consider a light pulse emitted from the origin, O, of a stationary frame S. The origin of a moving frame S', O', which overlaps with O at t = t' = 0 is moving with a constant speed *u* with respect to O. Which statement(s) correctly describe(s) the position of the wavefront of the light sphere as measured from the origins? r(r') is the distance of the wavefront from the origin O (O') at time t(t').

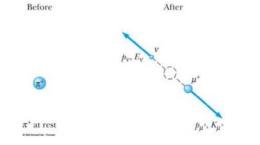
$$\mathbf{I} \quad r = ct \qquad \qquad \mathbf{II} \quad r' = ct' \qquad \qquad \mathbf{III} \quad r' = r \qquad \qquad \mathbf{IV} \quad r' = ut$$

A. I,II B. I, II,III C. II, III, IV D. IV Only E. Non of the above My own question Solution: A

11. Which of the following statement(s) is (are) true regarding Lorentz transformation (LT)?
I Time dilation can be recovered from LT
II Length contraction can be recovered from LT
III Absolute simultaneity is not guaranteed by LT
IV Galilean transformation is a generalisation of LT

A. II,III B. I, II,III C. II, III, IV D. I, II E. Non of the above My own question Solution: B

Question 12-13 are based on the decay of a π meson into a muon and a massless neutrino shown in figure below. The mass of the muon is known to be $m_{\mu} = 106 \text{ MeV}/c^2$, and the kinetic energy of the muon is measured to be $K_{\mu} = 4.6 \text{ MeV}$. p_{μ} denotes the momentum of the muon.



SESSI 04/05/TEST1

12. What is the momentum of the neutrino?

A.
$$\sqrt{\left(K_{\mu}+m_{\mu}c^{2}\right)^{2}-m_{\mu}^{2}c^{4}}$$

B. $\left(K_{\mu}+m_{\mu}c^{2}\right)$
C. $\sqrt{2m_{\mu}K_{\mu}}$
D. p_{μ}
E. Non of the above
Serway and Mosses. pg. 53
Solution: D

13. What is the total relativistic energy of the neutrino?

A.
$$\sqrt{(K_{\mu} + m_{\mu}c^2)^2 - m_{\mu}^2c^4}$$

B. $(K_{\mu} + m_{\mu}c^2) + \sqrt{(K_{\mu}^2 + 2K_{\mu}m_{\mu}c^2)^2}$
C. K_{μ}
D. $m_{\mu}c^2$
E. Non of the above
Serway and Mosses. pg. 52
Ans: A

Solution: $E_v = \sqrt{(p_v^2 c^2 + m_v^2 c^4)} = p_v c \ (m_v c^2 = 0)$. The momentum of neutrino, $p_v^2 = p_\mu^2$ (from Question 12 above) is related to the kinetic energy of the muon via $E_\mu = \sqrt{(p_\mu^2 c^2 + m_\mu^2 c^4)} = m_\mu c^2 + K_\mu$. Therefore the momentum of the neutrino is related to the kinetic energy of the muon via $p_v^2 c^2 = (m_\mu c^2 + K_\mu)^2 - m_\mu^2 c^4$. Taking the square root, we then have $E_v = p_v c = \sqrt{(K_\mu + m_\mu c^2)^2 - m_\mu^2 c^4}$.

14. Serway and Moses, Questions 12, page 37

What happens to the density of an object as its speed increases, as measured by an Earth observer?

A. Remain the same as it is when at rest **B.** Increase by a factor of γ **C.** Increase by a factor of γ^2 **D.** Increase by a factor of $1/\gamma$ **E.** Non of the above

ANS: C, my own question

15. What is the upper limit of the momentum of an electron?

A. *m_ec* B. *c* Serway, Q12, pg. 1276 Solution: D E. Non of the above

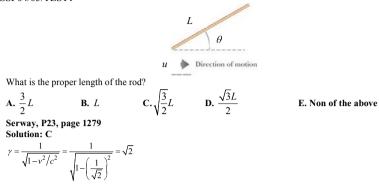
16. Which of the following statement(s) is (are) true?
I Only massless particle can travel at the speed of *c*.
II Not all massless particle can travel at the speed of *c*.
III It is not necessary that a massless particle must travel at the speed of *c*.
IV All particles which are not massless must travel at the speed lower than *c*.

A. II,III B. I, II,III C. I, III, IV D. I, IV E. Non of the above My own question Solution: D

C.0 D. Infinity

17. A moving rod is observed to have a length of L and to be orientated at an angle of $\theta = 45^{\circ}$ with respect to the

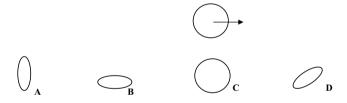
direction of motion, as shown in the figure below. The rod has a speed of $u = \frac{c}{\sqrt{2}}$.



SESSI 04/05/TEST1 Serway, P35, page 1280 Solution: A

We are also given L and θ (both measured in a reference frame moving relative to the rod). Thus, $L_x = L\cos\theta = \frac{L}{\sqrt{2}}$; $L_y = L\sin\theta = \frac{L}{\sqrt{2}}$. L'_x is a proper length, related to L_x by $L_x = \frac{L'_x}{\gamma}$. Therefore, $L'_x = \gamma L_x = \sqrt{2} \frac{L}{\sqrt{2}} = L$, and $L'_y = L_y = \frac{L}{\sqrt{2}}$. (Lengths perpendicular to the motion are unchanged). $\Rightarrow (L')^2 = (L'_y)^2 + (L'_x)^2 = \frac{L^2}{2} + L^2 = \frac{3L^2}{2} \Rightarrow L' = \sqrt{\frac{3}{2}}L$

18. A spaceship in the shape of a sphere moves past and observer on Earth with a speed of v = 0.5c in the direction as indicated by the arrow. What shape will the observer see as the spaceship move past?





19. What is the speed of an object having relativistic momentum of magnitude *p* and rest mass *m*?

A.
$$\frac{p}{m}$$
 B. $\frac{c}{\sqrt{1 + (mc/p)^2}}$ C. $\frac{mc^2}{u}$ D. $\frac{mu^2}{c}$ E. Non of the above

Serway, P32, page 1280 Solution: B

20. An electron with rest mass m_e moves with a speed of $\frac{\sqrt{3}}{2}c$. What is the work required to increase its speed

to
$$\frac{2\sqrt{2}}{3}c$$
?
A. m_ec^2
B. $0.511m_ec^2$
C. $\frac{5}{36}m_ec^2$
D. $\frac{\sqrt{5}}{6}m_ec^2$
E. Non of the above

ZCT 104/3E Modern Physics Semester II, Sessi 2004/05 Test II (18 Feb 200b)

- 1. Which statements is (are) TRUE about photoelectricity according to classical physics? (ANS: D)
- D Light beam of higher intensity is expected to eject electrons with higher kinetic energy from the metal surface (T)
- ID In photoelectric experiment the energy carried by a beam of light is considered to be continuous (T)
- IID Light is wave and not comprised of quantum of energy (T)
- IV) When light is irradiated on the metal surface, some time lag is expected before photoelectrons are ejected from the surface (T)
- A. I.II B. II. III
- С. Ш D. I, II, III, IV
- E. Non of A, B, C, D
- 2. Let a given metal surface is irradiated with monochromatic light of intensity I_1 . Then the same surface is irradiated by monochromatic light with intensity I_2 (where $I_2 > I_1$) but with a longer wavelength. Which of the following statement(s) is (are) true? (ANS: E)
- I) The energy of the photon in the beam with intensity I_2 is larger than that in the beam with intensity I_1 . (F)
- ID The saturated photocurrents will remain unchanged. (F)
- The maximum kinetic energy of the III) photoelectron will increase for the beam with intensity I_2 (F)
- IV) The different intensity of light will alter the work function of the metal surface (F)

A. I, II	B.	П,	Ш
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- C. III D. III, IV
- E. Non of A, B, C, D
- 3. Which of the following statements is (are) correct about Bohr's atom and a quantum particle trapped inside a simple infinite quantum well of width d? (ANS: A)
- D The gap separating energy levels of higher quantum number becomes closer

and closer in the Bohr's hydrogen atom, whereas in the case of particle in a box the gap becomes larger and larger at higher quantum levels. (T)

The electron in the Bohr's atom is subjected to a non-zero potential due to Coulomb's attraction, whereas in the box the particle is subjected to zero potential. (T)

ID

D

I)

- IID The energy levels in the Bohr's atom are negative whereas they are positive for the particle in the well. (T)
- IV) In both cases the particles involved form standing waves (T)

А.	I, II, III, IV	B. II, III
C.	III	D. III, IV
E.	Non of A, B, C, D	

- 4. Which of the following statements is (are) true? (ANS: C)
 - A particle has a de Broglie wavelength that is related to its linear momentum (T)
- A particle's momentum must be ID quantised in all systems, bounded or unbounded (F)
- III) A particle's kinetic energy must be quantised in all systems, bounded or unbounded (F)
- A particle's kinetic energy is only IV) quantised in bounded system (T)

A.	I, II, IV	B. I, II, III
C.	I, IV	D. II, III
E.	Non of A, B, C, D	

- 5. In order to have photoelectrons ejected from a metal surface in a typical photoelectric effect experiment, (ANS: C)
- the frequency of the light used must be larger than a certain cut-off value (T) ID the intensity of the light used must be
- larger than a certain cut-off value (F) the wavelength of the light used must be III)
- larger than a certain cut-off value (F) IVthe saturated photocurrent must be larger than a certain cut-off value (F)

A. I. II. IV B. I. III C. I D. II. III. IV E. Non of A, B, C, D

SESSI 04/05/TEST2

- 6. What of the following statements are TRUE regarding photoelectric effect (PE) and Compton effect (CE)? (ANS: D)
- D In PE light behaves like particle, whereas in CE light behave like wave (F)
- In PE light behaves like wave, whereas ID in CE light behave like particle (F)
- In PE only part of the photon's energy is IID lost to the atom, whereas in CE all of the photon's energy is lost to the free electron (F)
- IV In PE all of the photon's energy is lost to the atom, whereas in CE only part of the photon's energy is lost to the free electron (T)
- A. I.III B. II. III
- C. II. IV D. IV
- E. Non of A. B. C. D
- 7. Which statements is (are) TRUE about photoelectric and Compton effects? (ANS: E)
- Compton effect experiment confirms D that the energy of the quantum of light is proportional to the frequency of the wave model of light (F)
- ID Compton effect experiment confirms that the radiant energy of light is quantized into concentrated bundle (F)
- Photoelectric effect infers that the IID radiant energy of light is quantized into concentrated bundle (T)
- IV Both Compton effect and photoelectric effect confirm that EM radiation has both wave and particle properties (F)

А.	I, III	B.	II, III
С.	II, IV	D.	IV
E.	Non of A, B	, C, D	

- 8. Which of the following is (are) the correct statement(s) about X-ray production in a conventional X-ray tube? (ANS: B)
- I) Part or all of the kinetic energy of the moving electron is converted into X rays photon (T)
- ID X-rays is emitted when the bombarding electrons undergo Compton scattering (F)
- IID The production of x-rays can be considered as a photoelectric process (F) The shortest wavelength in the x-rays IV)
- spectrum is the same for different material (T)

А.	II, III	B. I, IV
C.	II, IV	D. IV
E.	Non of A, B	, C, D

- 9. Which of these statements is (are) true about blackbody radiation? (ANS: B)
- D Rayleigh-Jeans law is behaving in a physically acceptable manner at short wavelengths (F)
- II) Rigel (the blue star) is hotter than Betelguese (red star) because of the position of the peak wavelength in their black body spectrum (T)
- IID According to Rayleigh-Jeans law the average energy of the oscillators is given by the equipartition theorem (T)
- The spectral distribution of radiation IV) from a blackbody can only be explained in terms of quantised energy levels of the oscillators (T)

А.	I, II, III, IV	B. II, III, IV
C.	II, IV	D. III, IV
E.	Non of A, B, C, D	

10. Which of these statements are correct? (ANS: E)

- D We conclude that light behave like wave when we find that the light from the sun arrives to the Earth after 8 minutes it was emitted. (F)
- When we consider light to behave like a II) particle we expect some detectable time lag for the electron to be emitted from the surface of the metal in a PE experiment. (F)
- III) When we consider light to behave like wave we expect some detectable time lag for the electron to be emitted from the surface of the metal in a PE experiment. (T)
- Photoelectric effect occurs at the same IV) energy scale as that of the x-rays production because x-rays production is the inverse of the photoelectric process. (F)

A. I, II, III, IV	B. II, III, IV
C. II, IV	D. III, IV
E. III	

- 11. Which of the following statements is (are) TRUE? (ANS: E)
- The energy levels of the atomic orbit is D quantized (T)
- The energy associated with the orbits of ID the electron in a hydrogen atom is negative because it is not a bounded system (F)
- IID E = 0 means the electron is free from the bondage of the nucleus' potential field. (T)
- IV) Electron at very large quantum number *n* is tightly bounded to the nucleus by the EM force. (F)

A. I, II, III, IV	B. II, III, IV
C. II, IV	D. III, IV
E. I, III	

- 12. Which of the following statements is (are) TRUE about the Bohr's model of hydrogenlike atom? (ANS: C)
- It applies the Newton's second law for D the atom's mechanical stability (T)
- ID The angular momentum is postulated to be quantised via $L = nh/2\pi$ (T)
- IID It assumes the validity of classical electromagnetic theory for the orbiting electron (F)
- The only stable orbits of radius r are IV) those that can fit in a multiple number of standing wave of the electron, i.e $2\pi r =$ $n\lambda(T)$

А.	I, II, III, IV	B. II, III, IV
C.	I, II, IV	D. III,IV
E.	Non of A, B, C, D	

- 13. Which of the following statements is (are) true? (ANS C)
- D) Thompson suggestion of the Plum Pudding Model is falsified by Rutherford's alpha particle experiment (T)
- ID Rutherford suggested the planetary model of atoms. (T)
- de Broglie is the first to experimentally IID confirm that electron manifests wave nature. (F)
- IV) Frank-Hertz experiment confirms the existence of discrete energy levels in mercury atom (T)

A.	I, II, III, IV	B. II, III, IV
C.	I, II, IV	D. III,IV
E.	Non of A, B, C, D	

- 14. Which of the following statement is (are) true about the Plum-pudding model by Thompson and Rutherford's experiment? (ANS A)
- I) Plum-pudding model fails to explain the emission & absorption line spectrum from atoms because it predicts only a single unique emission frequency. (T)
- ID Plum-pudding model cannot explain the 180 degree back-scattering of alpha particle seen in Rutherford's scattering experiment. (T)
- IID The planetary model of atoms is plagued by infrared catastrophe (T) IV) In the Rutherford's alpha particle
 - scattering experiment, the large deflection of alpha particle is caused by a close encounter between alpha particle and the diffused distribution of the positive charge of an atom. (F)

A. I. II. III B. II. III. IV C. I. II. IV D. III. IV E. Non of A. B. C. D

- 15. Which of the following statements is (are) true regarding the basic properties of atoms? (ANS: A)
 - Atoms are of microscopic size, $\sim 10^{-10}$ m (T)
- ID Atoms are stable (T)

I)

D)

- III) Atoms contain negatively charges, electrons, but are electrically neutral. (T) IV) Atoms never emit and absorb EM
- radiation. (F)B. II. III. IV

A.	I, II, III	B. II, III, I
C.	I, II, IV	D. III, IV
E.	Non of A, B, C, D	

16. Which of the following statements is (are) true about Bohr's hydrogen-like atom? (ANS C)

The increase in the quantum number nmeans an increase in the energy of the atomic states. (T)

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II)	When <i>n</i> approach infinity, the energy
	states become infinity. (F)
III)	Free electron is the electron which has

the smallest quantum number n (F) IV) The zero point energy is the energy of

,	the lowest p	ossible quantum	level (T
	тиш	впп	пw

А.	I, II, III	B. II, III, IV
С.	I, IV	D. III, IV
E.	Non of A, B, C, D	

- 17. Heisenberg's uncertainty principle is a consequence of (ANS: A)
- A. the intrinsic wave nature of particle
- **B.** the intrinsic particle nature of wave
- **C.** the indivisible nature of particle
- **D.** the divisible nature of particle
- E. probabilistic interpretation of the wave function
- 18. Which of the following statements is (are) true about the spectrum from hydrogen atom? (ANS: A)
- Balmer series involve transitions of D electron from higher orbits to the n = 2orbit
- II) Balmer series is the first spectral series of hydrogen atom observed
- When electron in higher orbit is de-III) excited to lower orbit, photons of discrete frequency are emitted from the atom. as seen in the emission spectrum
- When electron in lower orbit is excited IV) to higher orbit, photons of discrete frequency are absorbed by the atom, as seen in the absorption spectrum

A.	I, II, III, IV	B. II, III, IV
C.	I, IV	D. III, IV
E.	Non of A, B, C, D	

- 19. Which of the following statements is (are) true regarding a quantum particle trapped inside an infinite well of width L? (ANS B)
- D It forms stationary (standing) wave inside the well (T)
- ID The linear momentum of the particle becomes quantised (T)
- III) The minimum energy of the particle inside the well is given by $h^2/8mL^2$ (T)
- IV) The energy of the particle inside the well can take on negative value (F)

А.	I, II, III, IV	B. I, II, III
C.	I, IV	D. III, IV
E.	Non of A, B, C, D	

- 20. Which of the following statements is (are) true regarding pair production and pair annihilation of electron-positron pair? (ANS D)
- D Pair annihilation occurs only above the threshold energy of $2m_ec^2$ (F)
- II) Pair production occurs only above the threshold energy of $2m_ec^2$ (T)
- Energy is always conserved in both IID processes of pair production and pair annihilation (T)
- IV Momentum is always conserved in both processes of pair production and pair annihilation (T)

А.	I, II, III, IV	B. I, II, III
C.	I, IV	D. II, III, IV
E.	Non of A. B. C. D	

UNIVERSITI SAINS MALAYSIA

Final Exam Academic Session 2004/2005 March 2005

ZCT 104E/3 - Physics IV (Modern Physics) *[Fizik IV (Fizik Moden)]*

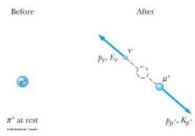
> Duration: 3 hours [Masa: 3 jam]

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Part A: Objective Instruction: Answer all 40 objective questions in this Part. [Bahagian A: Objektif.] [Arahan: Jawab kesemua 40 soalan objektif dalam Bahagian ini.]

Question 1 - 3 are based on the decay of a π meson into a muon and a massless neutrino shown in the figure below. The mass of the muon is known to be $m_{\mu} = 106 \text{ MeV}/c^2$, and the kinetic energy of the muon is measured to be $K_{\mu} = 4.6 \text{ MeV}$. p_{μ} denotes the momentum of the muon.

[Soalan 1-3 adalah berdasarkan pereputan satu meson π kepada satu muon dan satu neutrino tanpa jisim, sepertimana ditunjukkan dalam gambarajah di bawah. Diketahui jisim muon ialah m_{μ} = 106 MeV/ c^2 , dan tenaga kinetik muon yang terukur ialah K_{μ} = 46 MeV. p_{μ} menandakan momentum muon.]



1. How is the momentum of the muon, p_{μ} related to the kinetic energy of the muon? E_{μ} denotes the total relativistic energy of muon.

[Bagaimanakah momentum muon p_{μ} dikaitkan dengan tenaga kinetik muon? E_{μ} menandakan tenaga keretatifan muon]

A.
$$p_{\mu}c = \sqrt{\left(K_{\mu} + m_{\mu}c^{2}\right)^{2} - m_{\mu}^{2}c^{4}}$$

B. $p_{\mu} = \sqrt{\left(K_{\mu} + m_{\mu}c^{2}\right)^{2} - m_{\mu}^{2}c^{4}}$
C. $p_{\mu} = \sqrt{2m_{\mu}K_{\mu}}$
D. $p_{\mu}c = \sqrt{\left(E_{\mu}^{2} + m_{\mu}c^{2}\right)^{2}}$

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D] ANS:A, Inspired by Serway and Mosses 2005 edition, pg. 52-53.

 What is the rest energy of the π meson? [Apakah tenaga rehat meson π ?]

A.
$$K_{\mu} + m_{\mu}c^{2}$$

B. $\left(K_{\mu} + m_{\mu}c^{2}\right) + \sqrt{\left(K_{\mu}^{2} + 2K_{\mu}m_{\mu}c^{2}\right)}$
C. K_{μ}
D. $m_{\nu}c^{2}$

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D] ANS:B, Inspired by Serway and Mosses 2005 edition, pg. 52-53.

3. What is the kinetic energy of the neutrino? [Apakah tenaga kinetik neutrino?]

A.
$$\sqrt{\left(K_{\mu}+m_{\mu}c^{2}\right)^{2}-m_{\mu}^{2}c^{4}}$$
 B. $\left(K_{\mu}+m_{\mu}c^{2}\right)+\sqrt{\left(K_{\mu}^{2}+2K_{\mu}m_{\mu}c^{2}\right)}$

Please check that the examination paper consists of **XXX** pages of printed material before you begin the examination.

[Sila pastikan bahawa kertas peperiksaan ini mengandungi XXX muka surat yang bercetak sebelum anda memulakan peperiksaan ini.]

Instruction: Answer all questions. Please answer the objective questions from Part A in the objective answer sheet provided. Answer both structured questions from Part B. Please submit the objective answer sheet and the answers to the structured questions separately.

Students are allowed to answer all questions in Bahasa Malaysia or in English.

[<u>Arahan</u>: Jawab **SEMUA** soalan. Sila jawab soalan-soalan objektif daripada bahagian A dalam kertas jawapan objektif yang dibekalkan. Jawab kedua-dua soalan struktur daripada Bahagian B. Hantar kertas jawapan objektif dan jawapan kepada soalan struktur berasingan.]

[Pelajar dibenarkan untuk menjawab samada dalam bahasa Malaysia atau bahasa Inggeris.]

Data

speed of light in free space, $c = 3.00 \times 10^8 \text{ m s}^{-1}$ permeability of free space, $\mu_0 = 4\pi \times 10^{-7} \text{ H m}^{-1}$ permittivity of free space, $\varepsilon_0 = 8.85 \times 10^{-12} \text{ F m}^{-1}$ elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$ Planck constant, $h = 6.63 \times 10^{-34} \text{ J s}$ unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$ rest mass of electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$ rest mass of proton, $m_p = 1.67 \times 10^{-27} \text{ kg}$ molar gas constant, $e = 6.02 \times 10^{-23} \text{ mol}^{-1}$ Avogadro constant, $N_A = 6.02 \times 10^{-31} \text{ N m}^2 \text{ kg}^{-2}$ acceleration of free fall, $g = 9.81 \text{ m s}^{-2}$

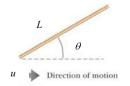
C. K_{μ} D. $m_{\mu}c^{2}$ E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D] ANS:A, Inspired by Serway and Mosses 2005 edition, pg. 52-53.

- 4. Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I (T) All inertial frames are equivalent [Semua rangka inersia adalah setara]
 - **II** (T) If light obeys Galilean transformation, light waves would appear stationary in an inertial frame that moves with the same speed with that of the light. [Jika cahaya mematuhi transformasi Galilean, gelombang cahaya akan kelihatan pegun dalam satu rangka inersia yang kelajuannya sama dengan kelajuan cahaya]
 - **III(F)** In an inertial frame moving approximately with the speed of light, light waves would appear stationary according to the postulates of special theory of relativity [Dalam satu rangka inersia yang bergerak dengan kelajuan hampir dengan kelajuan cahaya, gelombang cahaya akan kelihatan pegun mengikut postulat teori kerelatifan khas.]
 - **IV (F)** It is experimentally verified that electromagnetic waves propagate through a medium called Ether [Telah disahkan secara eksperimen bahawa gelombang elektromagnetik merambat melalui satu jenis medium digelar Ether.]

 A. II,III
 B. I, II,III
 C. II, III, IV
 D. I, II

 E. Non of A, B, C, D
 [Jawapan tiada dalam A, B, C, D]
 ANS:D, my own question

5. A moving rod is observed to have a length of *L* and to be orientated at an angle of $\theta = 45^{\circ}$ with respect to the direction of motion, as shown in the figure below. The rod has a speed of $u = \frac{c}{\sqrt{2}}$. [Suatu rod bergerak diperhatikan mempunyai panjang *L* dan diorientasikan pada suatu sudut $\theta = 45^{\circ}$ merujuk kepada arah gerakannya sepertimana ditunjukkan dalam gambarajah di bawah. Kelajuan rod ialah $u = \frac{c}{\sqrt{2}}$.]



Serway, page 1279, question 23 (modified)

What is the tangent of the angle in the proper frame (in terms of $\tan \theta$)? [Apakah tangen sudutnya (dinyatakan dalam sebutan $\tan \theta$) dalam rangka `proper']

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A. $\tan \theta$ **B.** $\frac{\tan \theta}{\sqrt{2}}$ **C.** $\sqrt{2} \tan \theta$ **D.** $2 \tan \theta$ **E.** Non of A, B, C, D [Jawapan tiada dalam A, B, C, D] **ANS:B**

6. What measurement(s) do two observers in relative motion always agree on? [Apakah ukuran(-ukuran) yang sentiasa disetujui oleh dua orang pemerhati yang berada dalam pergerakan relatif]
I The speed of light c in vacuum [Laju cahaya c dalam vakum]
II The speed v of their relative motion [Laju relatif v di antara mereka]
III The momentum of an object [Momentum suatu objek]

 A. II, III
 B. I, II, IV
 C. II, III, IV
 D. I, II

 E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]
 Serway Q1, pg. 1276
 Solution: B

IV The rest mass of an object [Jisim rehat suatu objek]

7. Given $\{x,t\}$, $\{x',t'\}$ are two sets of coordinates used by two reference frames which are moving with a constant relative velocity, which statement(s) correctly describe(s) the transformation between them?

[Diberi {x,t}, {x',t'} merupakan dua set koordinat yang digunakan oleh dua rangka rujukan yang bergerak dengan halaju relatif mantap, kenyataan yang manakah memerihalkan transformasi di antara dua set koordinat tersebut dengan betul?]

- I {*x*,*t*} is related to {*x*',*t*'} by Galilean transformation at $u \le c$ [{*x*,*t*} dikaitkan dengan {*x*',*t*'} oleh transformasi Galilean pada $u \le c$]
- II {*x*,*t*} is related to {*x*',*t*'} by Galilean transformation at $u \rightarrow c$ [{*x*,*t*} dikaitkan dengan {*x*',*t*'} oleh transformasi Galilean pada $u \rightarrow c$]
- III {*x*,*t*} is related to {*x'*,*t'*} by Lorentz transformation at $u \le c$ [{*x*,*t*} dikaitkan dengan {*x'*,*t'*} oleh transformasi Lorentz pada $u \le c$]
- IV {*x*,*t*} is related to {*x'*,*t'*} by Lorentz transformation at $u \rightarrow c$ [{*x*,*t*} dikaitkan dengan {*x'*,*t'*} oleh transformasi Lorentz pada $u \rightarrow c$]

A. I,IIB. I, III,IVC. II, III, IVD. I, IV OnlyE. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]My own questionSolution: B

8. What is the upper limit of the speed of an electron? [Apakah limit atas bagi laju suatu elektron?]
A. m_ec
B. c
C. 0
D. Infinity
E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]
Serway, Q12, pg. 1276
Solution: B

9. The units of the Planck constant *h* are those of: [Unit bagi pemalar Planck *h* adalah sama dengan unit bagi ...]

A. energy B. power C. momentum D. angular momentum E. frequency Solution: D, Chap 38, Q1, RHW 7th ed testbank,

 Rank following electromagnetic radiations according to the energies of their photons, from least to greatest. *Menvusun sinaran elektromagnetik berikut mengikut tenaga foton mereka, daripada yang*

[Menyusun sinarah elekiromagnetik berhali mengikai tenaga joton mereka, daripada ya paling lemah kepada yang paling besar]

1. blue light 2. yellow light 3. x-rays 4. radio waves

A. 1, 2, 3, 4 **B.** 4, 2, 1, 3 **C.** 4, 1, 2, 3 **D.** 3, 2, 1, 4 **E.** 3, 1, 2, 4 **Solution: B, Chap 38, Q9, RHW** 7th ed testbank,

- **11.** In a photoelectric effect experiment the stopping potential is: [Dalam eksperimen kesan fotoelektrik keupayaan penghenti adalah]
 - A. the energy required to remove an electron from the sample [tenaga yang diperlukan untuk menyingkirkan satu elektron daripada sampel]
 - **B.** the kinetic energy of the most energetic electron ejected *[tenaga kenetik bagi elektron terlenting yang paling bertenaga]*
 - **C.** the potential energy of the most energetic electron ejected *[tenaga keupayaan bagi elektron terlenting yang paling bertenaga]*
 - D. the photon energy [tenaga foton]

E. the electric potential that causes the electron current to vanish [keupayaan elektrik yang menyebabkan arus elektron hilang]
 Solution: E, Chap 38, Q13, RHW 7th ed testbank,

- 12. In a photoelectric effect experiment no electrons are ejected if the frequency of the incident light is less than A/h, where h is the Planck constant and A is: [Dalam eksperimen kesan fotoelektrik tiada elektron akan terlenting jika frekuensi cahaya tuju adalah kurang daripada A/h, di mana h ialah pamalar Planck dan A ialah:]
 - A. the maximum energy needed to eject the least energetic electron [tenaga maksimum yang diperlukan untuk melentingkan elektron yang paling kurang bertenaga]
 - B. the minimum energy needed to eject the least energetic electron

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[tenaga miminum yang diperlukan untuk melentingkan elektron yang paling kurang bertenaga]

- C. the maximum energy needed to eject the most energetic electron [tenaga maksimum yang diperlukan untuk melentingkan elektron yang paling bertenaga]
- **D.** the minimum energy needed to eject the most energetic electron [tenaga minimum yang diperlukan untuk melentingkan elektron yang paling bertenaga]

E. the intensity of the incident light [keamatan cahaya tuju]

Solution: D, Chap 38, Q16, RHW 7th ed testbank,

13. Consider the following: [Pertimbangkan yang berikut]

mungkin dalam jarak gelombang adalah]

- I. A photoelectric process in which some emitted electrons have kinetic energy greater than *hf*, where *f* is the frequency of the incident light. [Satu proses fotoelektrik di mana sebahagian elektron terlenting mempunyai tenaga kinetik yang lebih besar daripada hf, di mana f ialah frekuensi cahaya tuju]
- **II.** A photoelectric process in which all emitted electrons have energy less than *hf.* [Satu proses fotoelektrik di mana kesemua elektron terlenting mempunyai tenaga kurang daripada *hf*]
- III. Compton scattering from stationary electrons for which the emitted light has a frequency that is greater than that of the incident light.
 [Penyerakan Compton daripada elektron-elektron rehat yang mana cahaya tertenting mempunyai frekuensi yang lebih besar daripada frekuensi cahaya tuju]
- IV. Compton scattering from stationary electrons for which the emitted light has a frequency that is less than that of the incident light. [Penyerakan Compton daripada elektron-elektron rehat yang mana cahaya tertenting mempunyai frekuensi yang lebih kecil daripada frekuensi cahaya tuju]

The only possible processe(s) is (are) [Proses(-proses) yang mungkin ialah]:

A. I B. III C. I and III D. I and IV E. II and IV Solution: E, Chap 38, Q29, RHW 7th ed testbank (model answer in the testbank is incorrect)

 14. In Compton scattering from stationary electrons the largest change in wavelength that can occur is: [Dalam penyerakan Compton daripada elektron-elektron rehat, perubahan paling besar yang

A. 2.43×10^{-15} m **B.** 2.43×10^{-12} m **C.** 4.9×10^{-12} m **D.** dependent on the frequency of the incident light [bergantung kepada frekuensi cahaya tuju] **E.** dependent on the work function [bergantung kepada fungsi kerja] **Solution: C, Chap 38, Q25, RHW** 7th ed testbank (model answer in the testbank is incorrect)

15. Of the following, Compton scattering from electrons is most easily observed for: [Daripada yang berikut, penyerakan Compton daripada elektron-elektron adalah paling mudah dicerap dalam]

A. microwavesB. infrared lightC. visible lightD. ultraviolet lightE. x raysSolution: E, Chap 38, Q22, RHW 7th ed testbank,

16. In Compton scattering from stationary particles the maximum change in wavelength can be made larger by using: [Dalam penyerkan Compton daripada zarah-zarah rehat, perubahan maksimum dalam jarak gelombang boleh dijadikan lebih besar dengan menggunakan]

A. higher frequency radiation [sinaran yang berfrekuensi lebih tinggi]
B. lower frequency radiation [sinaran yang berfrekuensi lebih rendah]
C. more massive particles [zarah yang berjisim lebih besar]
D. less massive particles [zarah yang berjisim lebih kecil]
E. particles with greater charge [zarah yang casnva lebih besar]

Solution: D, Chap 38, Q21, RHW 7th ed testbank (modified)

17. Evidence for the wave nature of matter is: [Bukti untuk sifat gelombang bagi jasad ialah]

A. Electron diffraction experiments of Davisson and Germer *[eksperimen belauan elektron oleh Davisson dan Germer]*

B. Photoelectric effect [kesan fotoelektrik]

- C. Young's double slit experiment [eksperimen dwi-celah Young]
- D. the Compton effect [kesan Compton]
- **E.** Frank-Hertz experiment *[eksperimen Frank-Hertz]*

Solution: A, Chap 38, Q31, RHW 7th ed testbank,

18. Monoenergetic electrons are incident on a single slit barrier. If the energy of each incident electron is increased the central maximum of the diffraction pattern: [Elektron monotenaga ditujukan pada satu sawar celah tunggal. Jika tenaga setiap elektron tuju dinaikkan, maka maksimum pusat corak belauan]

A. widens [dilebarkan] B. narrows [disempitkan]

C. stays the same width [kelebaran tetap tak berubah]

D. widens for slow electrons and narrows for fast electrons [dilebarkan untuk elektron yang lambat dan disempitkan untuk elektron yang pantas]

E. narrows for slow electrons and widens for fast electrons

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[disempitkan untuk elektron yang lambat dan dilebarkan untuk elektron yang pantas]

Solution: B, Chap 38, Q34, RHW 7th ed testbank,

- Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]
 - I (T) An ideal blackbody absorbs all of the light that is incident on it. [Jasad hitam yang ideal menyerap kesemua cahaya yang tertuju padanya]
 - II (F) The distribution of energy in the blackbody radiation depends upon the material from which the blackbody is constructed. [Taburan tenaga dalam pancaran jasad hitam bergantung kepada jenis bahan yang membentuk dinding jasad hitam]
 - **III(T)** A blackbody is a perfect emitter of the radiation it generates. [Jasad hitam adalah pemancar pancaran yang sempurna.]
 - **IV (T)** The energy of an ultraviolet photon is more than the energy of an infrared photon. [Tenaga suatu foton ultraungu adalah lebih tinggi daripada tenaga bagi suatu foton inframerah]

 A. III, IV
 B. I, II, III
 C. I, III, IV
 D. I, III

 E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]
 Image: Comparison of the second second

Solution: C I: testgen Physics 2 by Walker, Q1, Walker Chap 30 II: testgen Physics 2 by Walker, Q2, Walker Chap 30 III: testgen Physics 2 by Walker, Q11, Walker Chap 30 IV: testgen Physics 2 by Walker, Q12, Walker Chap 30

20. If the wavelength of a photon is doubled, what happens to its energy? [Jika jarak gelombang digandakan dua kali, apa yang akan berlaku ke atas tenaganya?]

A. It is halved. *[ia diseparuhkan]*B. It stays the same. *[tetap tak berubah]*C. It is doubled. *[ia digandaduakan]*D. It is quadrupled. *[ia digandakan 4 kali]*E. Non of A, B, C, D *[Jawapan tiada dalam A, B, C, D]*

ANS: A, testgen Physics 2 by Walker, Q24, Walker Chap 30

21. Light of a given wavelength is used to illuminate the surface of a metal, however, no photoelectrons are emitted. In order to cause electrons to be ejected from the surface of this metal you should

[Cahaya dengan jarak gelombang tertentu digunakan untuk memancari permukaan satu logam, tapi tiada fotoelektron yang terlentingkan. Unutk menlentingkan elektron daripada permukaan logam tersebut anda kena]

A. use light of a longer wavelength.

[menggunakan cahaya yang berjarak gelombang lebih panjang]

B. use light of a shorter wavelength. [menggunakan cahaya yang berjarak gelombang lebih pendek]
C. use light of the same wavelength but increase its intensity. [menggunakan cahaya yang berjarak gelombang sama tapi menambahkan keamatannya]

D. use light of the same wavelength but decrease its intensity. [menggunakan cahaya yang berjarak gelombang sama tapi mengurangkan keamatannya]

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D] ANS: B, testgen Physics 2 by Walker, Q35, Walker Chap 30

22. Protons are being accelerated in a particle accelerator at sub-relativistic energies. When the energy of the protons is doubled, their de Broglie wavelength will [Proton dipecutkan dalam satu pemecut zarah pada tenaga sub-kerelatifan. Bila tenaga proton digandaduakan, jarak gelombang de Broglienya akan]

A. increase by a factor of 2. [bertambah dengan satu factor 2] B. decrease by a factor of 2. [berkurang dengan satu factor 2] C. increase by a factor of $\sqrt{2}$. [bertambah dengan satu factor $\sqrt{2}$] D. decrease by a factor of $\sqrt{2}$. [berkurang dengan satu factor $\sqrt{2}$] E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: D, testgen Physics 2 by Walker, Q64, Walker Chap 30

23. A proton and an electron are both accelerated to the same final speed. If λ_p is the de Broglie wavelength of the proton and λ_e is the de Broglie wavelength of the electron, then [Kedua-dua proton dan elektron dipecutkan kepada laju akhir yang sama. Jika λ_p ialah jarak gelombang de Broglie proton dan λ_e ialah jarak gelombang de Broglie elektron maka]

A. $\lambda_p > \lambda_e$. **B.** $\lambda_p = \lambda_e$. **C.** $\lambda_p < \lambda_e$. **D.** Not enough data to answer this question. *[tak cukup data untuk menjawab soalan ini]* **E.** Non of A, B, C, D *[Jawapan tiada dalam A, B, C, D]* **ANS: C, testgen Physics 2 by Walker, Q67, Walker Chap 30**

24. If the position of an electron is measured very precisely there is an uncertainty in measuring its [Jika kedudukan suatu elektron diukur dengan sangat tepat maka akan wujud ketidakpastian dalam pengukuran ...nya]

A. rest mass.	B. momentum.	C. potential energy.
D. charge.	E. Non of A, B, C, D	[Jawapan tiada dalam A, B, C, D]

ANS: B, testgen Physics 2 by Walker, Q71, Walker Chap 30

25. Which of the following statement(s) is (are) true? [Manakah kenyataan yang berikut adalah benar?]

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- I (T) A zero value for the Planck's constant would mean that the laws of classical physics would apply to quantum physics. [Jika pemalar Planck bernilai sifar ini bermakna hukum-hukum fizik klasik akan teraplikasikan dalam fizik kuantum]
- II (T) In quantum tunneling, electrons and other quantum particles can tunnel through a region of space that would be forbidden to them if they were classical particles. [Dalam penerowongan kuantum, elektron dan zarah-zarah kuantum lain boleh menerowongi satu rantau yang terlarang bagi mereka yang merupakan zarah-zarah klasikal.]
- III(F) A large value for the Planck's constant would mean that the laws of classical physics would apply to quantum physics. [Jika pemalar Planck bernilai besar ini bermakna hukum-hukum fizik klasik akan teraplikasikan dalam fizik kuantum]

A. III B. II, III C. I D. I, II E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D] Solution: D I,II: testgen Physics 2 by Walker, Q72, Walker II: testgen Physics 2 by Walker, Q73, Walker

26. A major advantage of an electron microscope over a visible light microscope is that the electron microscope

[Manfaat yang major bagi satu mikroskop elektron berbanding dengan mikroskop cahaya nampak ialah bahawa mikroskop elektron]

A. has much greater magnification. [memberikan pembesaran yang lebih tinggi]
B. operates with much lower intensity. [beroperasi pada keataman yang lebih rendah]
C. can penetrate opaque samples. [boleh menembusi sampel legap]
D. can have much better resolution. [memberikan leraian yang lebih baik]
E. requires no lenses for its operation. [tidak memerlukan kanta-kanta dalam operasinya]

ANS: D, testgen Physics 2 by Young and Freeman, Q27, Chap 39

27. An important observation that led Bohr to formulate his model of the hydrogen atom was the fact that

[Salah satu pencerapan yang merangsangkan Bohr memformulasikan model atom hidrogennya ialah fakta bahawa]

- A. a low density gas emitted a series of sharp spectral lines. [gas berketumpatan rendah memancarkan pinggir-pinggir spectrum yang tajam]
- **B.** neutrons formed a diffraction pattern when scattered from a nickel crystal. [neutron membentuk corak belauan bila diserakkan daripada hablur nickel]
- C. electrons were found to have a wave nature. [elektron didapti mempunyai sifat gelombang]

- **D.** the peak of the blackbody radiation moved to shorter wavelengths as the temperature was increased.
- [puncak jasad hitam bergerak menghampiri jarak gelombang yang lebih pendek bila suhu bertambah]
- E. the emission of light by an atom does not appear to conserve energy. [pancanran cahaya oleh atom tidak mengabadikan tenaga]
 ANS: A, testgen Physics 2 by Young and Freeman, Q40, Chap 39
- 28. The particle nature of light is best illustrated by which of the following? [Sifat zarah cayaha adalah paling baik diilustrasikan oleh yang mana berikut?]
 - A. The scattering of alpha particles from gold foil. [Serakan zarah alfa daripada foil emas]

B. The fact that hot objects emit electromagnetic radiation. [Fakta bahawa objek panas memancarkan pancaran elektromagnetik]

- C. The diffraction pattern observed when a beam of electrons is scattered by a crystal [Corak belauan yang dicerap bila satu bim elektron diserakkan oleh satu hablur]
- **D.** The fact that a rainbow consists of a continuous spectrum of colors *[Fakta bahawa pelangi mengandungi satu spektrum warna yang selanjar]*
- E. The ejection of electrons from a metal surface illuminated by light. [Pelentingan elektron daripada permukaan logam yang disinari cahaya]
 ANS: E, testgen Physics 2 by Young and Freeman, Q18, Chap 38
- 29. A wave function is given by

[Satu fungsi gelombang diberikan oleh] $\Psi(x) = 0$ for x < 0 $\Psi(x) = Ax$ for $0 \le x \le L$ $\Psi(x) = 0$ for x > L

The product of the normalization constant A and the quantity $L^{3/2}$ is equal to: [Hasildarab pemalar normalisasi A dengan kuantiti $L^{3/2}$ bersamaan dengan]

A. $\sqrt{12}$ **B.** $\sqrt{15}$ **C.** $\sqrt{20}$ **D.** $\sqrt{24}$ **E.** $\sqrt{3}$

ANS: E, testgen Physics 2 by Young and Freeman, Q1, Chap 40, modified

30. If a wave function ψ for a particle moving along the x axis is "normalized" then: [Jika satu funsi gelombang ψ untuk satu zarah yang bergerak sepanjang paksi x adalah ternormalisasikan, maka

A. $\int |\psi|^2 dt = 1$ **B.** $\int |\psi|^2 dx = 1$ **C.** $\partial \psi / \partial x = 1$ **D.** $\partial \psi / \partial t = 1$ **E.** $|\psi|^2 = 1$

Solution: B, Chap 39, Q1, RHW 7th ed testbank,

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31. The energy of an electron in a hydrogen atom that is about to get ionised is *[Tenaga elektron dalam atom hidrogen yang hampir-hampir diionkan adalah]*

A. -13.6 eV	B. -3.4 eV	C. -10.2 eV
D. -1.0 eV	E. 0 eV	

Solution: E, Chap 39, Q26, RHW 7th ed testbank, modified.

32. According to the Bohr model of hydrogen atom, the energy E_n of a hydrogen atom of a state with quantum number *n* is proportional to: [Mengikut model hidrogen Bohr tenaga E_n suatu atom hidrogen pada keadaan dengan nombor kuantum n adalah berkadaran dengan]

A. n **B.** n^2 **C.** 1/n **D.** $1/n^2$

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

Solution: D, Chap 39, Q25, RHW 7th ed testbank,

33. The series limit for the Balmer series represents a transition $m \rightarrow n$, where (m, n) is [Limit siri bagi siri Balmer mewakili satu peralihan $m \rightarrow n$, di mana (m, n) ialah]

	A. (2,1)	B. (3,2)	C. (∞,0)	D. (∞,1)	E. (∞,2)
--	-----------------	-----------------	-----------------	-----------------	-----------------

Solution: E, Chap 39, Q33, RHW 7th ed testbank,

34. The location of a particle is measured and specified as being exactly at x = 0, with *zero* uncertainty in the *x* direction. How does this affect the uncertainty of its velocity component in the *y* direction?

[Lokasi suatu zarah adalah diukur dan dispesifikasikan sebagai tepat-tapat pada x = 0 dengan ketidakpastian sifar dalam arah x. Bagaimanakah keadaan ini mempengaruhi ketidakpastian komponen halajunya dalam arah y?]

A. It does not affect it. [Keadaan ini tidak mempengaruhinya]
B. It makes it infinite. [Keadaan ini menjadikannya infinit]
C. It makes it zero. [Keadaan ini menjadikannya sifar]
D. It makes it negative [Keadaan ini menjadikannya negatif]
E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]
Ans: A, QQ serway 40.10

- **35.** The Balmer series of hydrogen is important because it: *[Siri Balmer bagi hidrogen adalah penting kerana ia]*
 - A. is the only one for which the Bohr theory can be used [merupakan satu-satunya siri yang dapat diaplikasikan oleh teori Bohr]

- B. is the only series which occurs for hydrogen [merupakan satu-satunya siri yang berlaku dalam hidrogen]
- C. is in the visible region [berada dalam rantau nampak]
- **D.** involves the lowest possible quantum number *n* [melibatkan numbor kuantum yang terendah mungkin]
- **E.** involves the highest possible quantum number *n* [melibatkan numbor kuantum yang tertinggi mungkin]

Solution: C, Chap 39, Q34, RHW 7th ed testbank,

- 36. The quantization of energy, E = nhf, is not important for an ordinary pendulum because: [Pengkuantuman tenaga, E = nhf, adalah tidak penting bagi suatu bandul kerana]
 - A. the formula applies only to mass-spring oscillators [formular hanya teraplikasikan ke atas pengayun jisim-spring]
 - **B.** the allowed energy levels are too closely spaced *[selang paras tenaga diizinkan adalah terlalu padat]*
 - C. the allowed energy levels are too widely spaced [selang paras tenaga diizinkan adalah terlalu lebar]
 - **D.** the formula applies only to atoms *[formular hanya teraplikasikan ke atas atom]*
 - E. the value of h for a pendulum is too large [nilai h bagi bandul terlalu besar]
 Solution: B, Chap 38, Q3, RHW 7th ed testbank,
- **37.** A hydrogen atom is in its ground state. Incident on the atom are many photons each having an energy of 5 eV. The result is that *[Suatu atom hidrogen berada dalam keadaan buminya. Foton-foton bertenaga 5 eV setiap satu ditujukan pada atom itu. Hasilnya ialah]*
 - A. the atom is excited to a higher allowed state [atom teruja kepada keadaan dizinkan yang lebih tinggi]
 - **B.** the atom is ionized *[atom diionkan]*
 - **C.** the photons pass by the atom without interaction *[foton merentasi atom tanpa berinteraksi]*

D. the photons are ionised

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[foton diionkan]

E. the atom is de-excited to a lower quantum state [atom ternyah-uja kepada keadaan dizinkan yang lebih rendah]
ANS (C), Serway, qq 42.1, pg. 1360. Because the energy of 5 eV does not correspond to raising the atom from the ground state to an allowed excited state, there is no interaction between the photon and the atom (modified)

38. A hydrogen atom makes a transition from the n = 3 level to the n = 2 level. It then makes a transition from the n = 2 level to the n = 1 level. Which transition results in emission of the longest-wavelength photon?
[Satu atom hidrogen melakukan peralihan dari paras n=3 ke paras n=2. Kemudiannya ia

melakukan satu peralihan dari paras n=2 ke paras n=3 ke paras n=2. Kemudulinya ta melakukan satu peralihan dari paras n=2 ke paras n=1. Peralihan yang manakan menghasilkan pancaran foton berjarak gelombang paling panjang?]

A. the first transition *[peralihan pertama]* B. the second transition *[peralihan kedua]*

C. neither, because the wavelengths are the same for both transitions. *[bukan A ataupun B kerana jarak gelombang kedua-dua kes adalah sama]*

D. one cannot determine the answer because data provided is not sufficient. *[jawapan tidak boleh ditentukan kerana data yang diberikan tak cukup]*

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS (A), Serway, qq 42.3, pg. 1360. The longest-wavelength photon is associated with the lowest energy transition, which is n = 3 to n = 2.

39. An electron and a proton are accelerated to a common relativistic energy (i.e. $E \gg m_e c^2$, $m_p c^2$), where m_e and m_p denote the masses of the electron and proton respectively. Determine the ratio of the de Broglie wavelength of the electron to that of the proton. [Satu elektron dan proton dipecutkan kepada satu tenaga kerelatifan E yang sama, (iaitu $E \gg m_e c^2$, $m_p c^2$), di mana m_e dan m_p menandakan jisim elektron dan proton masing-masing. Tentukan nisbah jarak gelombang de Broglie elektron kepada proton.]

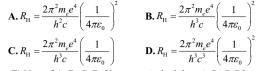
(A)
$$\frac{m_p}{m_e}$$
 (B) $\sqrt{\frac{m_p}{m_e}}$ (C) $\sqrt{\frac{m_e}{m_p}}$ (D) $\frac{m_p}{m_e}$

(E) 1

ANS (E), My own question, pg. 897.

40. How is the empirical Ryberg constant, $R_{\rm H}$, be related to the other constants of nature in the Bohr model of hydrogen atom?

[Bagaimanakah pemalar empirikal Ryberg $R_{\rm H}$ dikaitkan kepada pemalar-pemalar alam yang lain mengikut model Bohr atom hidrogen?]



(E) Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS (B), Cutnell and Johnson, pg. 910.

Part B: Structured Questions [60 marks] Instruction: Answer both questions 1 and 2 in this Part.

[Bahagian B: Soalan Struktur. 60 markah] [Arahan: Jawab kedua-dua soalan 1 dan 2 dalam Bahagian ini.]

1(a) Consider the Gedanken experiment of a moving train (the O' frame) passing by an observer called Doraemon on the ground (the O frame) with a speed of v, see figure below. The length of the train, as measured by Doraemon, is *L*. Another observer, Doraemiyan is seen by Doraemon to sit at the middle of the train, *L*/2, when Doraemiyan passes by Doraemon at time *t*=0. At that instance, two lightning bolts strike points A and B at the edges of the train such that both events appear to occur simultaneously according to Doraemon. What is the time lag between the lights from event A and event B arriving at Doraemiyan, *t_A* - *t_B*, as seen by Doraemon, where both *t*'s are measured in Doraemon's frame. Express your answer in terms of v, *L*, and the speed of light *c*. [*Hint: Do you think you should apply time-dilation or length contraction formulae here?*]

[Pertimbangkan eksperimen Gedanken di mana satu tren (rangka O') bergerak melepasi seorang pemerhati Doraemon yang berada di atas bumi (rangka O) dengan laju v, rujuk gambarajah di bawah. Panjang tren sebagaimana yang diukur oleh Doeaemon ialah L. Seorang lagi pemerhati, Doraemiyan diperhatikan oleh Doraemon sebagai duduk di tengahtengah tren, L/2, bila Doraemiyan bergerak melepasi Doraemon pada masa t = 0. Pada ketika itu, dua petir menyambar titik-titik A dan B pada pinggir tren sedemikian rupa supaya keduadua peristiwa itu kelihatan berlaku secara serentak kepada Doraemon. Apakah masa susulan di antara cahaya dari peristiwa A dan peristiwa B yang sampai kepada Doraemiyan, $t_A - t_B$, mengikut Doraemon? Kedua-dua masa t_A , t_B adalah diukur dalam rangka Doraemon. Nyatakan jawapan anda dalam sebutan v, L dan laju cahaya c. [Hint: Adakah anda perlu mengaplikasikan formular-formular pendilatan-masa dan susutan panjang?]

> A O frame B O frame

[10 marks]

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By the time $t_{\rm B}$, light from event B hits Doramiyan. Since then she has moved for a distance of $vt_{\rm B}$ to the right from Doramon. Hence, light from B fulfils the relation $ct_{\rm B} = L/2 - vt_{\rm B}$.

Likewise, by the time $t_A (> t_B)$ light from A hits Doramiyan. Since then she has moved for a distance of vt_A to the right from Doramon. Hence, light from A fulfils the relation $ct_A = L/2 + vt_A$.

 $t_{\rm B} = L/2(c+v); t_{\rm A} = L/2(c-v)$ $\Rightarrow t_{\rm A} - t_{\rm B} = L/2(c-v) - L/2(c+v) = (uL)/(c^2-v^2)$

[10 marks]

1(b) When a photoelectric surface is illuminated with light of wavelength 437 nm, the stopping potential is 1.67 V.

[Bila satu permukaan fotoelektrik disinari cahaya berjarak gelombang 437 nm, keupayaan penghenti ialah]

[5 + 5 marks]

- (i) What is the work function of the metal in eV? [Apakah fungsi kerja logam tersebut dalam unit eV?]
- (*ii*) What is the maximum speed of the ejected electrons? [Apakah laju maksimum elektron terlenting?]

Solution:

(i) $W_0 = hc/\lambda - K_{\text{max}} = 1240 \text{ nm.eV}/437 \text{ nm} - 1.67 \text{ eV} = 1.17 \text{ eV}$ (ii) $K_{\text{max}} = mv^2/2 \Rightarrow v^2 = (2K_{\text{max}} / m)^{1/2} = (2 \times 1.67 \text{ e J} / 9.11 \times 10^{-31} \text{ kg})^{1/2} = 7.66 \times 10^5 \text{ m/s}$

ANS: testgen Physics 2 by Young and Freeman, Q2.4, Chap 38

1(c) An electron has a speed of 0.95*c*. What is the the magnitude of its momentum? [5 marks] [Suatu elektron berlaju 0.95*c*. Apakah magnitud momentumnya?]

Solution:

 $\gamma = 1/\sqrt{1 - 0.95^2} = 3.20$ $p = m\gamma u = 9.1 \times 10^{-31} \times 3.2 \times (0.95 \times 3 \times 10^8) \text{Ns} = 8.3 \times 10^{-22} \text{Ns}$

Chap 37, Q54, RHW 7th ed testbank,

1(d) A 29.0 pm photon is Compton scattered by a stationary electron. What is the maximum energy loss of the photon? [Satu foton 29.0 pm diserak Compton oleh satu elektron pegun. Apakah kehilangan tenaga foton yang maksimum?]

[5 marks]



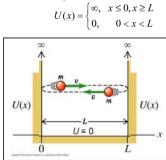
Solution:

Maximal kinetic energy loss of the photon occurs when

$$\Delta \lambda = \Delta \lambda_{\max} = 2\lambda_c = \frac{2hc}{m_e c^2} = \frac{2 \times (1240 \text{keV} \cdot \text{pm})}{522 \text{keV}} = 4.75 \text{pm}$$
$$\Delta E_{\max} = \frac{hc}{\lambda} - \frac{hc}{\lambda_{\max}} = hc \left(\frac{1}{\lambda} - \frac{1}{\lambda + \Delta \lambda_{\max}}\right)$$
$$= (1240 \text{keV} \cdot \text{pm}) \left(\frac{1}{29 \text{pm}} - \frac{1}{29 \text{pm} + 4.75 \text{pm}}\right) = 6.01 \text{ keV}$$

ANS: testgen Physics 2 by Young and Freeman , Q1.12, Chap 38 (Model answer may be incorrect)

2(a) Consider a quantum particle trapped in an infinite quantum well (with width *L*) given by [*Pertimbangkan satu zarah kuantum yang terperangkap dalam satu telaga kuantum infinit (dengan lebar L) yang diberikan oleh*]



The behaviour of a particle inside the infinite well [i.e. the region where U(x) = 0 for 0 < x < L] is governed by the 1-D time-independent Schrodinger equation $\frac{\partial^2 \psi(x)}{\partial x^2} = -B^2 \psi(x)$, where $B^2 = \frac{2mE}{\hbar^2}$. *E* is the energy of the particle. [Kelakuan zarah dalam telaga infinit (iaitu dalam rantau U(x) = 0 for 0 < x < L) diperintah oleh persamaan merdeka-masa Schrodinger 1-D $\frac{\partial^2 \psi(x)}{\partial x^2} = -B^2 \psi(x)$, di mana $B^2 = \frac{2mE}{\hbar^2}$. *E*



(i) Show that ψ(x) = A sin Bx + C cos Bx is a solution to the Schrodinger equation for the particle inside the well, where A, C are some constants.
 [Tunjukkan bahawa ψ(x) = A sin Bx + C cos Bx merupakan penyelesaian kepada persamaan Schrodinger untuk zarah dalam telaga, di mana A dan C adalah pemalar.]

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Solution: Plug
$$\psi(x) = A \sin Bx + C \cos Bx$$
 into the LHS of $\frac{\partial^2 \psi(x)}{\partial x^2} = -B^2 \psi(x)$:
 $\frac{\partial^2 \psi(x)}{\partial x^2} = \frac{\partial^2}{\partial x^2} [A \sin Bx + C \cos Bx] = \frac{\partial}{\partial x} [BA \cos Bx - BC \sin Bx]$
 $= -B^2 A \sin Bx - B^2 C \cos Bx = -B^2 [A \sin Bx + C \cos Bx]$
 $= -B^2 \psi(x) = \text{RHS of the Schroginger equation}$

 (ii) Determine the values of C and B by applying boundary conditions that must be fulfilled by the Schrodinger equation governing the particle.
 [Tentukan nilai-nilai C dan B dengan mengaplikasikan syarat-syarat sempadan yang mesti dipenuhi oleh persamaan Schrodinger yang memerintah zarah itu.]

[4 + 6 marks]

Solution:

Boundary condition (1) Plug $\psi(x = 0) = 0$ into $\psi = AsinBx + CcosBx$, we obtain $\psi(x=0) = 0 = Asin 0 + C cos 0 = C$, i.e. C = 0

[4 marks]

Hence the solution is reduced to $\psi = AsinB$ Next we apply the second boundary condition: $\psi(x = L) = 0 = Asin(BL)$ Only either A or sin(BL) must be zero but not both; A cannot be zero This means it must be sinBL = 0, or in other words $B = n \pi/L \equiv B_n$, $n = 1, 2, 3, \cdots$

[6 marks]

(iii) Hence show that the energy of the particle in the infinite well is quantized.
 [Seterusnya tunjukkan bahawa tenaga zarah dalam telaga infinit adalah terkuantumkan]
 [5 marks]

Solution

B

tl

$$\sum_{n=1}^{n} = \frac{2mE_n}{\hbar^2} = \frac{n^2\pi^2}{L^2} \Longrightarrow E_n = \frac{n^2\pi^2\hbar^2}{2mL^2}, n = 1, 2, 3...$$
 [5 marks]

2(b) What is the kinetic energy of an electron at the ground state of the hydrogen atom, given that the ground state energy of the hydrogen atom is -13.6 eV? Give your answer in unit of eV. [Apakah tenaga kinetik elektron pada keadaan bumi atom hidrogen? Diberitahu tenaga bumi atom hidrogen ialah -13.6 eV. Berikan jawapan anda dalam unit eV.]

[10 marks]

Solution: Serway and Moses, Problem 22

From the requirement that the centripetal force comes from the electrostatic force
$$\frac{mv_0^2}{r_0} = \frac{ke^2}{r_0^2}$$
,
[1 marks]

he kinetic energy of the ground state electron can be written as
$$K_0 = \frac{mv_0^2}{2} = \left(\frac{1}{2}\right)\frac{ke^2}{r_0}$$
.

[2 marks]

This gives $K_0 = \frac{ke^2}{2r_0} = 13.6 \text{ eV}$

Potential energy of the electron at ground state is $U_0 = -\frac{ke^2}{r_0}$.

[1 marks]

Hence ground state energy is $E_0 = K_0 + U_0 = \left(\frac{1}{2}\right)\frac{ke^2}{r_0} - \frac{ke^2}{r_0} = -\frac{ke^2}{2r_0} = -13.6 \text{ eV}$.

[3 marks]

[3 marks]

UNIVERSITI SAINS MALAYSIA

KSCP Academic Session 2004/2005 APRIL 2005

ZCT 104E/3 - Physics IV (Modern Physics) [Fizik IV (Fizik Moden)]

> Duration: 3 hours [Masa: 3 jam]

Please check that the examination paper consists of **XXX** pages of printed material before you begin the examination.

[Sila pastikan bahawa kertas peperiksaan ini mengandungi XXX muka surat yang bercetak sebelum anda memulakan peperiksaan ini.]

Instruction: Answer all questions. Please answer the objective questions from Part A in the objective answer sheet provided. Answer ALL structured questions from Part B. Please submit the objective answer sheet and the answers to the structured questions separately.

Students are allowed to answer all questions in Bahasa Malaysia or in English.

[<u>Arahan</u>: Jawab **SEMUA** soalan. Sila jawab soalan-soalan objektif daripada bahagian A dalam kertas jawapan objektif yang dibekalkan. Jawab kesemua soalan struktur daripada Bahagian B. Hantar kertas jawapan objektif dan jawapan kepada soalan struktur berasingan.]

[Pelajar dibenarkan untuk menjawab samada dalam bahasa Malaysia atau bahasa Inggeris.]

Data

speed of light in free space, $c = 3.00 \times 10^8 \text{ m s}^{-1}$ permeability of free space, $\mu_0 = 4\pi \times 10^{-7} \text{ H m}^{-1}$ permittivity of free space, $\varepsilon_0 = 8.85 \times 10^{-12} \text{ F m}^{-1}$ elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$ Planck constant, $h = 6.63 \times 10^{-34} \text{ J s}$ unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$ rest mass of electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$ rest mass of proton, $m_p = 1.67 \times 10^{-27} \text{ kg}$ molar gas constant, $A = 6.02 \times 10^{-23} \text{ mol}^{-1}$ Avogadro constant, $A_a = 6.02 \times 10^{-31} \text{ N m}^2 \text{ kg}^{-2}$ acceleration of free fall, $g = 9.81 \text{ m s}^{-2}$ p n 2004/2005

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Part A: Objective 25 marks

Instruction: Answer all 25 objective questions in this Part. *[Bahagian A: Objektif.]*

[Arahan: Jawab kesemua 25 soalan objektif dalam Bahagian ini.]

ANS: A, Young and Freeman study guide, pg 271

I. A massive particle has a speed of 0.95*c*. Can its energy and speed be increased by more than 500%?

[Laju suatu zarah yang berjisim ialah 0.95c. Bolehkah tenaga dan lajunya bertambah sebanyak 500%?]

A. The energy can but not the speed

- **B.** The speed can but not the energy
- **C.** Both the energy and speed can be increased by this amount
- **D.** Both the energy and speed cannot be increased by this amount
- E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: A, Modified from Young and Freeman study guide, pg 271

2. Consider a photon travelling in vacuum. Can its energy and speed be increased by more than 500%?

[Pertimbangkan suatu foton yang bergerak di dalam vakuum. Bolehkah tenaga dan lajunya bertambah sebanyak 500%?]

- **A.** The energy can but not the speed
- **B.** The speed can but not the energy
- C. Both the energy and speed can be increased by this amount
- **D.** Both the energy and speed cannot be increased by this amount
- E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: B, Modified from Young and Freeman study guide, pg 271, Example 1

3. Constancy of the speed of light in all inertial reference systems implies that *[Kemantapan laju cahaya dalam semua rangka rujukan inersia mengimplikasikan]*

A $x^{2} + y^{2} + z^{2} + c^{2}t^{2} = x'^{2} + y'^{2} + z'^{2} + c^{2}t'^{2}$

B. $x^2 + y^2 + z^2 - c^2 t^2 = x'^2 + y'^2 + z'^2 - c^2 t'^2$

C. x + y + z - ct = x' + y' + z' - ct'

D. x + y + z + ct = x' + y' + z' + ct'

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: C, Modified from Young and Freeman study guide, pg 280, Example 9

4. If a neutron spontaneously decays into a proton, an electron and a neutrino (which is massless), the decay products are observed to have a total kinetic energy of E_k . If the proton mass is M_P and the electron mass is m_e how large is the neutron mass?

[Jika suatu neutron mereput kepada satu proton, satu elektron dan satu neutrino (yang tak berjisim) secara spontan, jumlah tenaga kinetik hasil reputannya dicerap sebagai E_k . Jika jisim proton ialah M_P dan jisim elektron ialah m_e apakah jisim neutron?]

A.
$$(M_P + m_e) - \frac{E_k}{c^2}$$
 B. $\frac{E_k}{c^2} - (M_P + m_e)$ C. $M_P + m_e + \frac{E_k}{c^2}$

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D.
$$\sqrt{\left(M_P + m_e\right)^2 + \left(\frac{E_k}{c^2}\right)^2}$$

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: B, Cutnell, page 1271, QQ 39.10

5. The following pairs of energies represent the rest energy and total energy of three different particles: particle 1: *E*, 2*E*; particle 2: *E*, 3*E*; particle 3: 2*E*, 4*E*. Rank the particles according to their speed.

[Pasangan tenaga berikut mewakili tenaga rehat dan jumlah tenaga bagi tiga zarah yang berbeza: zarah 1: E, 2E; zarah 2: E, 3E; zarah 3: 2E, 4E. Aturkan zarah-zarah tersebut mengikut laju mereka.]

A. $v_3 > v_2 = v_1$ **B.** $v_2 > v_3 = v_1$ **C.** $v_1 > v_2 = v_3$
D. $v_3 > v_2 > v_1$ **E.** Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: A, Modified from Walker Test Item, pg 629, Q28

6. Observer A sees a pendulum oscillating back and forth in a relativistic train and measures its period to be *T_A*. Observer B moves together with the train and measures the period of the pendulum to be *T_B*. These two results will be such that [*Tempoh suatu bandul yang mengayun berulang-alik di dalam suatu keretapi kerelatifan diukur sebagai T_A oleh pemerhati A. Manakala pemerhati B yang gerak bersama dengan keretapi tersebut mengukur tempoh bandul tersebut sebagai <i>T_B*. Keputusan pengukuran tempoh-tempoh

tersebut mengukur tempoh bandul tersebut sebagai T_B . Keputusan pengukuran tempoh-tempoh tersebut adalah]

A. $T_A > T_B$ **B.** $T_A = T_B$ **C.** $T_A < T_B$ **D.** T_A could be greater or smaller than T_B depending on the direction of the motion **E.** Non of A, B, C, D *[Jawapan tiada dalam A, B, C, D]*

ANS: D, Walker Test Item, pg 642, Q1,Q2,Q4, Tutorial 2 Problems 1.

- 7. Which of the following statements are (is) correct? [Pilih kenyataan(-kenyataan) yang benar daripada yang berikut]
 - **I(T)** An ideal blackbody absorbs all of the light that is incident on it. [Jasad hitam yang ideal menyerap kesemua cahaya yang jatuh ke atasnya]
 - **II(T)** The distribution of energy in the blackbody radiation does not depends upon the material from which the blackbody is constructed. *[Taburan tenaga dalam pancaran jasad hitam tidak bergantung kepada jenis bahan yang membentuk jasad hitam itu.]*
 - **III(F)** The correct expression for the energy of a photon is $E = h\lambda$ [*Ekspresi yang betul bagi tenaga suatu foton ialah* $E = h\lambda$]
 - IV(T) For a blackbody, the total intensity of energy radiated over all wavelengths increases as the forth power of the temperature. [Bagi satu jasad hitam, keamatan tenaga yang dipancarkan bila sumbangan kesemua jarak gelombang dijumlahkan bertambah mengikut kuasa empat suhunya.]

A. I,II,III B. I,II C. II, III, IV D. I,II,IV

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: E, Young and Freeman study guide, page 286, Question

8. Which of the following statements are (is) correct?

[Pilih kenyataan(-kenyataan) yang benar daripada yang berikut]

- **I(T)** In the Compton Effect, there is a zero wavelength shift for forward scattering $(\theta = 0^{\circ})$ [Dalam kesan Compton, anjakan jarak gelombang sifar berlaku dalam serakan ke depan $(\theta = 0^{\circ})$]
- **II** (**T**) In the Compton Effect, no energy or momentum is transferred to the electron in the forward scattering.

[Dalam kesan Compton, tiada tenaga atau momentum dipindahkan kepada elektron dalam serakan ke depan.]

- III(T) In the Compton Effect, conservation of momentum and energy must be simultaneously satisfied. [Dalam kesan Compton, keabadian tenaga dan momentum mesti dipatuhi secara serentak.]
- IV(T) In the Compton Effect, energy and momentum are transferred to the scattered electron when θ is non zero. [Dalam kesan Compton, tenaga dan momentum dipindahkan kepada elektron terserakkan jika sudut θ bukan sifar.]

A. I,II,III B. I,II C. II, III, IV D. I,II,IV

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: B, Walker Test Item, page 646, Q25, own suggested options

9. Which of the following statements are (is) correct?

[Pilih kenyataan(-kenyataan) yang benar daripada yang berikut]

- I(F) A photon is a particle with positive charge [Foton adalah zarah yang bercas positif]
- **II (F)** A photon's mass is not necessarily zero [Jisim foton tidak semestinya sifar]
- **III(F)** Photon always move with a speed of *c* irrespective of the medium through which it is moving *[Tidak kisah medium apa yang dilaluinya, foton sentiasa bergerak dengan laju c]*
- **IV(T)** The number of photons per unit cross sectional area in a beam of light is proportional to the intensity of the light beam. [Nombor foton per unit keratan rentas dalam satu alur cahaya adalah berkadaran dengan keamatan alur cahaya itu.]

A. I,II,III B. IV C. II, III, IV D. I,II,IV

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: A, Walker Test Item, page 648, Q30

10. In photoelectric effect, which one of the following is the correct expression for the cut-off frequency of the metal in terms of its work function, W_0 ?

[Dalam kesan fotoelektric, kenyataan yang mana satukah adalah ekspresi yang betul yang menyatakan frekuensi penggal sesuatu logam dalam sebutan fungsi kerjanya?]

A. W_0 / h **B.** W_0 / c **C.** h / W_0 **D.** $(h / c) W_0$

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

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ANS: B, Cutnel, page 889, CYU 2

11. In Compton effect, an incident X-ray photon of wavelength λ is scattered by an electron, the scattered photon having a wavelength of λ'. Suppose that the incident photon is scattered by a proton instead of an electron. For a given scattering angle θ, the change λ' - λ in the wavelength of the photon scattered by the proton

[Dalam kesan Compton, suatu foton sinar-X tuju dengan jarak gelombang λ diserakkan oleh suatu elektron manakala jarak gelombang bagi foton terserak ialah λ' . Katakan foton tuju diserakkan oleh suatu proton yang manggantikan elektron. Untuk suatu sudut serakan θ yang diberikan, perubahan $\lambda' - \lambda$ dalam jarak gelombang foton terserak oleh proton adalah]

A. is greater than that scattered by the electron

- **B.** is less than that scattered by the electron
- **C.** is same as that scattered by the electron
- **D.** cannot be determined
- E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: A, Own question

12. In an electron-positron pair production by an energetic photon in the vicinity of a nucleus, the frequency of the photon λ must be

[Dalam penghasilan pasangan elektron-positron oleh suatu foton bertenaga tinggi di persekitaran suatu nucleus, frekuensi foton λ semestinya]

A. $\lambda \le h/2m_e c$ B. $\lambda \ge h/2m_e c$ C. $\lambda \le h/m_e c$ D. $\lambda \ge h/m_e c$ E. $\lambda \le h/2m_e$

13. ANS C: Young and Freeman test bank, pg. 414, Q14

In an important experiment in 1927 a beam of electrons was scattered off a crystal of nickel. The intensity of the scattered beam varied with the angles of scattering, and analysis of these results lead to confirmation of

[Dalam suatu eksperimen yang dilakukan dalam tahun 1927, suatu alur elektron diserakkan oleh suatu hablur nikel. Keamatan alur yang terserak berubah-ubah mengikut sudut ia diserakkan, dan analisis keputusan itu membawa kepada pengesahan]

- **A.** the particle nature of light
- **B.** the Bohr model of atom
- **C.** the wave nature of electrons
- **D.** the Rutherford model of the nucleus
- **E.** the quantisation of energy levels

ANS A: Young and Freeman test bank, pg. 425, Q2

14. Consider a particle in a box of width *L* and infinite height. Let the particle be in a state n = 11. What is the first value of x ($0 \le x \le L$), where the probability of finding the particle is highest? [Pertimbangkan suatu zarah dalam kotak dengan lebarL dan ketinggian infini. Biar ia berada dalam keadaan n = 11. Apakah nilai x ($0 \le x \le L$) yang pertama di mana keberangkalian menjumpai zarah terserbut adalah paling tinggi?]

A.	L/22	B. <i>L</i> /11	C.	L	D .	L/10
E.	Non of A, B, C, I) [Jawapan tiada dalam A,	, <i>B</i> ,	C, D]		

ANS B: Walker test item, pg. 654, Q65

15. Protons are being accelerated in a particle accelerator. When the speed of the proton is doubled, their de Broglie wavelength will

[Proton sedang dipecutkan oleh pemecut zarah. Bila laju proton digandakan dua kali, jarak gelombang de Broglie mereka akan]

A. increase by a factor of 2

- **B.** decrease by a factor of 2
- **C.** increase by a factor of $\sqrt{2}$
- **D.** decrease by a factor of $\sqrt{2}$

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS B: Walker student guide, pg. 506, quiz 9

16. If the minimum uncertainty in an object's position is decreased by half, what can we say about the uncertainty in its momentum?

[Jika ketidakpastian minimum bagi kedudukan suatu objek dikurangkan separuh, apa yang boleh dikatakan ke atas ketidakpastian dalam momentumnya?]

- A. The uncertainty in momentum is at most half of what it was before the change
- B. The uncertainty in momentum is at least twice what it was before the change
- **C.** The uncertainty in momentum does not change

D. The minimum uncertainty in momentum is precisely half of what it was before the change

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS A: Walker student guide, pg. 657, Q6

17. To which of the following values of *n* does the longest wavelength in the Balmer series correspond?

[Nilai n yang manakah bersepadanan dengan jarak gelombang paling panjang dalam siri Balmer?]

A. 3 **B.** 5 **C.** 1 **D.** infiniti **E.** Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS D: Young and Freeman test bank, pg. 418, Q36

18. In order for an atom to emit light, it

[Untuk memancarkan cahaya, sesuatu atom kena]

A. must be in the gaseous state [berada dalam keadaan gas]

- **B.** must be stimulated by external radiation [dirangsang oleh pancaran luar]
- C. must be in the ground state [berada dalam keadaan bumi]
- **D.** must be in an excited state *[berada dalam keadaan teruja]*
- **E.** must be fluorescent [berpendarfluor]

ANS C: Young and Freeman test bank, pg. 660, Q18,19,20

19. Which of the following statements are (is) correct?

[Pilih kenyataan(-kenyataan) yang benar daripada yang berikut]

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- A. Einstein proposed the model of the atomic structure that provides the best explanation of the observation that each atom in the periodic table has a unique sets of spectral lines. [Einstein menyarankan model struktur atom yang membekalkan penjelasan paling baik ke atas pencerapan hahawa setiap atom di dalam jadual berkala mempunyai satu set garisan spektrum yang unik.]
- **B.** According to one of the assumptions of the Bohr model, the electron in a hydrogen atom moves in an elliptical orbit about the nucleus *[Menurut salah satu anggapan model Bohr, elektron di dalam atom hidrogen berkisar di*
- *dalam orbit elips yang mengelilingi nucleus.]* C. Bohr's model of an atom includes idea from both classical and quantum physics.
- [Model atom Bohr mengandungi idea-idea daripada kedua-dua bidang fizik klasik dan fizik kuantum.]
- **D.** The plum-pudding model of atom by Thomson was verified by Rutherford's alpha scattering experiment

[Model atom 'plum-pudding' oleh Thomson telah diverifikasikan oleh eksperimen penyerakan alfa Rutherford.]

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS A: Serway. 1333, Quiz 41.5

20. Consider an electron, a proton and an alpha particle each trapped separately in identical infinite square wells. Which particle corresponds to the highest ground-state energy? [Pertimbangkan suatu elektron, suatu proton dan suatu zarah alfa yang masing-masing diperangkapkan secara berasingan di dalam telaga segiempat infinit yang identikal. Zarah yang manakan bersepadanan dengan paras tenaga bumi yang paling tinggi?]

A. the electron B. the proton C. the alpha particle

- **D.** The ground state energy is the same in all three cases **E**. Now of A, B, C, D, $U_{\text{respectively}}$
- E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS D: Serway. 1333, Quiz 41.6

21. Consider the three particles in Question 20 again. Which particle has the longest wavelength when the system is in the ground state? [Pertimbangkan semula zarah-zarah dalam Soalan 20. Zarah yang manakan mempunyai jarak gelombang yang paling panjang bila sistem berada dalam keadaan bumi?]
A. the electron B. the proton C. the alpha particle
D. All three particles have the same wavelength
E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS D: Young and Freeman test bank, pg. 663, Q22, 34, 40, 44

22. Which of the following statements are (is) correct?

[Pilih kenyataan(-kenyataan) yang benar daripada yang berikut]

- A. The kinetic energy of the electron in the first Bohr orbit of hydrogen is -13.6 eV. [Tenaga kinetik elektron dalam orbit Bohr pertama ialah -13.6 eV]
- **B.** The electron in a doubly ionised lithium atom experiences a weaker attractive force than the single electron in a hydrogen atom.
- [Elektron dalam atom lithium yang dua kali terionkan mengalami daya tarikan yang lebih lemah berbanding dengan elektron tunggal dalam atom hidrogen]
- C. In a hydrogen atom, the difference in the energy between adjacent orbit radii increases with the increasing value of n

[Dalam atom hidrogen, perbezaan tenaga di antara dua radius orbit yang berjiranan bertambah bila nilai n bertambah]

- **D.** The Bohr model correctly predicts the energy for the ground state of the hydrogen atom. [Model Bohr meranal dengan tepatnya tenaga keadaan bumi atom hidrogen]
- E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS B: Walker test item, pg. 664, Q36

23. Hydrogen atoms can emit four lines with visible colours from red to violet. These four visible lines emitted by hydrogen atoms are produced by electrons

[Atom hidrogen boleh memancarkan empat garis warna nampak daripada merah ke ungu. Empat garis nampak yang dipancarkan oleh atom hidrogen ini adalah dihasilkan oleh elektron]

A. that starts in the n = 2 level.

- **B.** that end up in the n = 2 level.
- C. that end up in the ground state.
- **D.** that start in the ground state.
- E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS D: Cutnel page 911

24. An electron in the hydrogen atom is in the n = 4 energy level. When this electron makes a transition to a lower level, the wavelength of the photon emitted is in the [Suatu elektron dalam atom hidrogen berada dalam paras n = 4. Bila elektron tersebut melakukan peralihan kepada paras tenaga yang lebih rendah, jarak gelombang foton yang terpancarkan berada dalam]

I. the Lyman series III. the Pashech series		II. the Blamer siriesIV. the Pfund series		
A. I	B. II	C. III	D. I,II,III	

E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS A: Cutnel page 934, Q 7

25. What is the longest radiation wavelength that can be used to ionized the ground-state hydrogen atom?

[Apakah jarak gelombang pancaran yang paling panjang yang boleh digunakan untuk mengiokan atom hidrogen pada keadaan bumi?]

A. *hc*/(13.6 eV)

- **B.** 2*hc*/(13.6 eV)
- **C.** 13.6 *hc*
- **D.** (13.6 eV)/hc
- E. Non of A, B, C, D [Jawapan tiada dalam A, B, C, D]

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Part B: Structured Questions [75 marks] Instruction: Answer ALL questions in this Part. [Bahagian B: Soalan Struktur. 75 markah] [Arahan: Jawab KESEMUA soalan dalam Bahagian ini.]

1. (a) Based on the physics constants data sheet provided (first page), calculate the ratio of the mass of proton to that of the electron.

[Berdasarkan lampiran data (dalam m/s pertama) pemalar-pemalar fizik yang dibekalkan, hitungkan nisbah antara jisim proton kepada jisim elektron.] [5 marks]

Solution:
$$\frac{M_P}{m_e} = \frac{1.67 \times 10^{-27}}{9.11 \times 10^{-31}} = 1833.2$$

(b) Calculate the kinetic energy of the electrons in a beam, in units of electron rest energy m_ec^2 , such that the relativistic mass of the electrons in the beam is as large is that of the proton. [Hitungkan tenaga kinetik bagi elektron-elektron dalam satu alur elektron, dalam unit tenaga rehat elektron m_ec^2 , sedemikian rupa supaya jisim kerelatifan elektron dalam alur tersebut bersamaan dengan jisim proton.)

Solution: Young and Freeman study guide, pg 281, Quiz 2,3

 $E = m'_{e}c^{2} = m_{e}c^{2} + K$ set $m'_{e}c^{2} = M_{p}c^{2} = (1833.2)m_{e}c^{2}$ $\Rightarrow K = (1833.2 - 1)m_{e}c^{2} = (1832.2)m_{e}c^{2}$

(c) What is the electric potential (in unit of Volt) that is required to accelerate the electron in (b) (from rest) ?

[Apakah beza keupayaan elektrik (dalam unit Volt) yang diperlukan untuk memecutkan elektron dalam (b) di atas (dari keadaan rehat)?]

[5 marks]

[10 marks]

[5 marks]

Solution: Young and Freeman study guide, pg 281, Quiz 2,3 $eV = K = (1832.2)m_ec^2 \Rightarrow V = (1832.2)m_ec^2 / e = 938.9$ MV

(d) If a 'moving clock' runs slower, what will the age difference between two twins if one stays on the Earth while the second makes a round trip to a point in space ten light years from Earth at a speed of 0.95*c*?

[Jika masa bagi 'jam yang bergerak' mengalir lebih perlahan', apakah perbezaaan umur di antara dua orang anak kembar jika salah satu daripada mereka tinggal di Bumi manakala yang seorang lagi menjalani satu penggembaraan dengan laju 0.95c ke satu tempat sejauh 10 tahuncahaya daripada Bumi dan kembali ke Bumi selepas penjelajahan tersebut?]

Solution: Young and Freeman study guide, pg 278, Example 7

$$\gamma = \frac{1}{\sqrt{1 - (0.95)^2}} = 3.2$$

Time taken for the round trip, according to the twin on Earth, is

 $T_E = D/v = 20 c \cdot yr/0.95c = 21.05 yr.$

Time taken for the round trip, according to the twin on ship, is $T_S = D'/\nu = D/(\nu) = 20 \text{ cyr}/(3.2 \text{ 0.95}c) = 6.58 \text{ yr}$, where $D' = 20 \text{ ly}/\gamma$ due to length contraction.

 $\Rightarrow T_E - T_S = (21.05 - 6.58) \text{ yr} = 14.47 \text{ yr}$

2. (a) A 60-W bulb is at an efficiency of 6.20%. What is the number of photons per second given off by the bulb assuming the wavelength of light to be 580 nm?

[6 marks]

Solution: Walker Test Item, page 642, Q5:

energy of 1 photon=
$$\frac{hc}{\lambda} = \frac{1240}{580}$$
 eV=2.13eV

Let number of photon per second =
$$N$$

therefore
$$N \frac{nc}{\lambda} = 2.325 \times 10^{19} \text{ eV/s}$$

 $N = \frac{2.325 \times 10^{19} \text{ eV/s}}{2.13 \text{ eV}} = 1.09 \times 10^{19} \text{ /s}$

(b) The work functions of several metals are listed below.

Metal	ϕ (in eV)
W	4.5
Ag	4.8
Cs	1.8
Cs on W	1.36

- (i) Which metals yield photoelectrons when bombarded with light of wavelength 500 nm?
- (*ii*) For those surfaces where photoemission occurs with the above light source, calculate the stopping potential in volts.
- (*iii*) For the metal tungsten calculate the threshold wavelength which would just start producing photoelectrons.

[3 + (2+2) + 2 = 9 marks]

Solution: Young and Freeman study guide, pg 287, Example 2

- (i) $E = hf = hc/\lambda = 2.48 \text{ eV}$; Cs and Cs on W yields photoelectrons
- (*ii*) For Cs: stopping potential is (2.48 eV 1.8 eV)/e = 0.68 VFor Cs on W: stopping potential is (2.48 eV - 1.36 eV)/e = 1.12 V
- (*iii*) $\lambda_t = hc/\phi = 1240 \text{ eV} \cdot \text{nm} / 4.5 \text{ eV} = 276 \text{ nm}$
- (c) A large number if 30.0 pm photons are scattered twice by stationary electrons. Find the **RANGE** of wavelength of the scattered photon in pm.

[Sejumlah besar foton-foton yang berjarak gelombang 30.0 pm diserakkan dua kali oleh satu elektron rehat. Hitungkan julat bagi jarak gelombang foton yang terserakkan dalam unit pm.] [10 marks]

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Solution: Young and Freeman test bank, pg 409, Q14:

When bombarded once, the maximal increase in the photon wavelength is given by $\Delta \lambda_{\max} = \frac{2h}{m_e c} = 2 \times 2.43 \text{pm} = 4.86 \text{pm}$ when the scattering angle $\theta = 180^\circ$. When the oncescattered photon is scattered again, the maximum shift in wavelength suffered by that photon is also $\Delta \lambda_{\max}$, making the maximal total shift in wavelength = $2 \Delta \lambda_{\max} = 2 \times 4.86 \text{ pm} = 9.72 \text{ pm}$. Hence the range of scattered photon lies between λ_n to $\lambda_n + 2 \Delta \lambda_{\max}$, i.e. 30.0 pm - 39.72 pm.

3. (a) Find the frequency of revolution of electron in n = 1 and n = 2 Bohr orbits. What is the frequency of the photon emitted when an electron in the n = 2 orbit drops to n = 1 orbit? [Hitungkan frekuensi kisaran bagi elektron dalam orbit-orbit Bohr n = 1 dan n = 2. Apakah frekuensi foton yang dipancarkan bila suatu elektron dalam orbit n=2 jatuh ke orbit n = 1?]
 [3 + 2 + 2 + 3 marks]

Solution: Bieser, pg 137/tutorial 5

From Bohr's postulate of quantisation of angular momentum, $L = (mv)r = nh/2\pi$, the velocity is related to the radius as $v = nh/2m\pi$. Furthermore, the quantised radius is given in terms of Bohr's radius as $r_n = n^2 r_0$. Hence, $v = h/2\pi mnr_0$. The frequency of revolution f = 1/T (where T is the period of revolution) can be obtained from $v = 2\pi r/T = 2\pi n^2 r_0 f$. Hence, $f = v/2\pi r = (h/2\pi mnr_0)/2\pi r = h/4\pi^2 mn^3 (r_0)^2$.

For n = 1, $f_1 = h/4 \pi^2 m (r_0)^2 = 6.56 \times 10^{15}$ Hz. For n = 2, $f_2 = h/4 \pi^2 m (2)^3 (r_0)^2 = 6.56 \times 10^{15}/8$ Hz = 8.2×10^{14} .

Photon's frequency = $\Delta E/h = 13.6 (1/1^2 - 1/2^2) \text{ eV} / h = 2.46 \text{ x } 0^{15} \text{ Hz}$

(b) Consider the case of 'particle in a box' (infinite square well). The lowest energy level of a particle (call it particle A) confined to a 1-D region of space with fixed dimension L is E_0 . If an identical particle (call it particle B) is confined to a similar region with fixed distance L/4, what is the energy of the lowest energy level of the particle B? Express your answer in terms of E_0 . [Pertimbangkan kes 'zarah di dalam kotak' (telaga segiempat infinit). Tenaga paling rendah bagi satu zarah (label ia zarah A) terkongkong di dalam satu ruang 1-D dengan dimensi L yang tetap ialah E_0 . Jika suatu zarah lain (zarah B) yang identical dengan zarah A dikongkongkan di dalam satu ruang yang serupa tapi dengan jarak tetap L/4, apakah tenaga bagi paras tenaga yang terendah bagi zarah B? Nyatakan jawapan anda dalam sebutan E_{-}]

[5 marks]

Solution: Young and Freeman test bank, pg 425, Short Questions 1: $16E_0$

$$E_0 = \frac{h^2}{8mL^2}$$

$$E'_0 = \frac{h^2}{8mL^{12}} = \frac{h^2}{8mL^{12}} = \frac{h^2}{8m(L/4)^2} = 16\frac{h^2}{8mL^2} = 16E_0$$

(c) Estimate the kinetic energy (in eV) should electrons have if they are to be diffracted from crystal with interatomic distance of the order of a few Å.

[Anggarkan tenaga kinetik (dalam unit eV) yang harus diperolehi oleh elektron-elektron jika mereka hendak dibelaukan oleh hablur yang berjarak antara-atom dalam tertib beberapa Å] [5 marks]

Solution

Serway, Mosses and Mayer, page 150, Example 4.3

For diffraction to happen, we require λ ~ interactomic distance ~ a few A

$$p = \frac{hc}{\lambda c} \sim \frac{1240 \text{eV} \cdot \text{nm}}{\text{few} (0.1 \text{nm}) \times c} = \frac{0.01124 \text{MeV}}{\text{few} \times c}$$
$$\Rightarrow K = \frac{p^2}{2m_e} \sim \left(\frac{0.0124 \text{MeV}/c}{\text{few}}\right)^2 \frac{1}{2 \times 0.5 \text{MeV}/c^2} = \frac{1.5 \times 10^{-4}}{\text{few}^2} \text{MeV}$$

(d) What is the frequency of the de Broglie waves associated with a body of rest mass m_0 moving with velocity v?

[Apakah frekuensi bagi gelombang de Broglie yang dikaitkan dengan jasad yang jisim rehatnya m_0 dan bergerak dengan laju v?]

[5 marks]

Solution: Arthur Beiser 5th edition, page 99

$$E = hf = mc^{2} = \gamma m_{0}c^{2} = \frac{m_{0}c^{2}}{\sqrt{1 - \frac{v^{2}}{c^{2}}}} \Rightarrow f = \frac{m_{0}c^{2}}{h\sqrt{1 - \frac{v^{2}}{c^{2}}}}$$

ZCT 104/3E Modern Physics Semester II, Sessi 2005/06 Test I (20 Dec 2006)

Data

Speed of light in free space, $c = 3.00 \times 10^8 \text{ ms}^{-1}$ Elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$ The Planck constant, $h = 6.63 \times 10^{-34} \text{ J s}$ Unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$ Rest mass of electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$ Rest mass of proton, $m_p = 1.67 \times 10^{-27} \text{ kg}$

- Say you put two clocks (clock A and clock B) in front of you and set them to 00.00am at standard local time. Then you ask your friend to send one of them (clock B) to ET's home some 300 million meters away. At one fine day, you decide to compare the reading of both clocks. The reading of clock A (which lies in front of you) reads 12.00 pm. Let say you can view clock B (now located at 300 million meters away) through a telescope. Which statement is correct about the reading of clock B as seen by you when peeking though the telescope?
 - A. The reading of clock B seen though the telescope is the same as the reading of clock A.
 - **B.** The reading of clock B seen though the telescope is different from the reading of clock A.
 - **C.** No conclusive statement can be made for the relation between the reading of clock B and clock A **D.** (None of **A. B. C.**)

ANS:B, My own questions

- 2. Your friend is running at a speed of *v* towards you. He throws out a ball towards you, and the speed of the ball is *u* with respect to him. What is the speed of the ball measured by you?
 - A. *u* + *v* B. *u* - *v* C. *v* - *u* D. (None of A, B, C) ANS:A. My own questions
- 3. Reconsider question 2 above. Your friend is running at a speed of v towards you. He shines a beam of light towards you. The speed of the light is *c* with respect to him. What is the speed of the light as measured by you?
 - A. c + v B. c - v C. c D. (None of A, B, C) ANS:C, My own questions
- 4. While standing beside a railroad track, we are startled by a boxcar traveling past us at half the speed of light. A passenger standing at the rear of the boxcar fires a laser pulse toward the front of the boxcar. The pulse is absorbed at the front of the box car. While standing beside the track we measure the speed of the pulse through the open side door. The measured value of the time of flight of the pulse is ______ than that measured by the rider.
 - A. greater than
 - $\boldsymbol{B.} \hspace{0.1in} \text{equal to} \hspace{0.1in}$
 - C. less than
 - **D.** (None of **A**, **B**, **C**)
 - ANS:A, My own questions

SESSI 05/06/TESTBANK

- 5. Given two events, A and B, of which space and time coordinate are respectively designated by (x_A, t_A) and (x_B, t_B) . Which of the following statements are (is) correct?
- I. Both events must be causally related
- II. Both events must not be causally related
- III. Both events may be causally related
- IV. Both events may be causally unrelated
 - **A.** I, II
 - **B.** III, IV
 - **C.** I, II, III, IV **D.** (None of **A**, **B**, **C**)

D. (None

- ANS: B
- 6. Given a species of fly has an average lifespan of τ . Let say you put 1000 of them in box A and send them to a destination at some remote destination in deep space using a rocket that travel at speed ν . The destination is located at a distance of *L* from Earth. Considering only special relativistic effect and assuming that None of the flies die of any cause other than aging, which of the following statements is (are) correct? (Lorentz factor is defined as $\gamma = [1-(\nu/c)^2]^{-1/2}$).
- I. Most of the flies would have not survived if the location of the destination $L/v > \tau$
- II. Most of the flies would survive if $(L/v) < \tau$
- III. Most of the flies would survive if $(1/\gamma) (L/\nu) < \tau$
- IV. Most of the flies would have not survived if $(1/\gamma) (L/\nu) > \tau$
 - **A.** I, IV **B.** II, III, IV
 - в. II, III, С. III. IV
 - **D.** (None of **A**, **B**, **C**)

ANS: B

- 7. Say Azmi is travelling in a mini bus moving with speed v (with respect to Earth) and Baba is sitting in Pelita Nasi Kandar restaurant. Using his own wristwatch, Azmi finds that his heart beats at a rate of N_A times per min. When Baba measures the heartbeat rate of Azmi in the Pelita frame, he found that Azmi's heart is beating at a rate of N_B times a min. What is the relation between the two reading, N_A and N_B ?
- **A.** $N_A > N_B$ **B.** $N_A < N_B$ **C.** $N_A = N_B$ **D.** (None of **A**, **B**, **C**) **ANS: A**
- 8. Consider a football, kicked lightly by David Beckham, is moving in a straight line with constant speed. Say in frame O, the momentum of the football is *P*. In a frame O' moving with a relative constant speed with respect to O, the momentum of football is *P'*. Which of the following statements are (is) true regarding *P* and *P'*?
- I. Classically, P and P' have a same numerical value.
- II. Relativistically, P and P' have a same numerical value.
- III. Classically, P and P' have a different numerical value.
- IV. Relativistically, P and P' have a different numerical value.
 - **A.** I, II
 - B. III, IV
 - C. I, II, III, IV
 - **D.** (None of \mathbf{A} , \mathbf{B} , \mathbf{C})

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9. In a given reference frame, O, the velocity of an object (which rest mass is m_0) is v_1 . The velocity of the same object in another frame, O', which moves with a relative velocity u with respect to O, is v_2 . What is the

momentum of the object in these frames? (In the following, $\gamma(v) = 1/\sqrt{1 - (v/c)^2}$).

- A. The momentum of the object in frame O is $m_0\gamma(v_1)v_1$ whereas in frame O' the momentum is $m_0\gamma(v_2)v_2$
- B. The momentum of the object in frame O' is $m_0\gamma(v_1)v_1$ whereas in frame O the momentum is $m_0\gamma(v_2)v_2$
- C. The momentum of the object in both frames is $m_0\gamma(u)u$.
- D. (None of A, B, C)

ANS: A

- 10. Which of the following statement is true regarding the linear momentum of an object?
 - A. In general the relativistic momentum is larger in magnitude than the corresponding classical momentum.
 - B. In general the relativistic momentum is smaller in magnitude than the corresponding classical momentum.
 - C. In general classical momentum and relativistic momentum has the same magnitude.
 - D. (None of **A**, **B**, **C**)

ANS: A

11. Which of the following statements is (are) true regarding the kinetic energy of an object?

- I. The kinetic energy of an object can increase indefinitely
- II. In special relativity, the kinetic energy of an object = the increase in the total relativistic energy of the object due to its motion
- III. The relativistic kinetic energy reduces to the non-relativistic form of $mv^2/2$ when $v \ll c$
- IV. The largest possible kinetic energy of an object is $mc^2/2$.

A. I, IV **B.** II, III, IV **C.** I, II, III

D. (None of **A**, **B**, **C**)

ANS: C

12. Which statements in the following is (are) true?

- I. Observer in different inertial frames can disagree about the speed of light in free space
- II. Observer in different inertial frames can disagree about the location of an event
- III. Observer in different inertial frames can disagree about the time separating two events
- IV. Proper time is the amount of time separating two events that occurs at the same location

A. II, III, IV B. II, III C. I, II, III, IV D. (None of A, B, C) ANS: A

13. Which statements in the following is (are) true?

- I. The rest energy as predicted by special relativity has no analogue in classical mechanics
- II. Work done by a force on a system is converted into mechanical energy of the system
- III. Force exerted on a system causes the momentum of the system to change at a rate proportional to the force

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IV. The change of momentum of a system causes a force to exert on the system

A. I, II B. I, II, III C. I, II, III, IV

SESSI 05/06/TESTBANK D. (None of A, B, C)

ANS: B

14. The relativistic kinetic energy of an object, in general, is

- A. greater than that defined by the classical mechanics
 B. less than that defined by the classical mechanics
 C. always equal to that defined by classical mechanics
 D. (None of A, B, C)
 ANS: A
- 15. A clock moving with a finite speed v is observed to run slow. If the speed of light were tripled, you would observe the clock to be
 - A. Even slower.
 - B. Still slow but not as much
 - C. As slow as it was
 - **D.** To start to actually run fast.
- ANS: B (Walker test bank, Chap 29, Q26)

16. Which of the following results shows the validity of the relativistic effect of time dilation?

- A. The conservation of linear momentum in electron-electron collision
- B. Bending of light near the Sun
- C. The decay of muons
- D. Null result in the Michelson-Morley experiment on Ether detection
- ANS: C (Walker test bank, Chap 29, Q27)
- 17. A spaceship travelling at constant speed passes by Earth and later passes by Mars. In which frame of reference is the amount of time separating these two events the proper time?
 - A. The Earth frame of referenceB. The spaceship frame of referenceC. Any inertial frame of reference
 - **D.** The Mars frame of reference
 - ANS: B (Walker test bank, Chap 29, Q13)

 $\mathbf{4}$

18. Boat 1 goes directly across a stream a distance *L* and back taking a time t_1 . Boat 2 goes down stream a distance *L* and back taking a time t_2 . If both boats had the same speed relative to the water, which of the following statements is true?

A. $t_2 > t_1$. **B.** $t_2 < t_1$. **C.** $t_2 = t_1$.

D. (None of **A**, **B**, **C**)

ANS: A (Serway test bank, Chap 39, Q6)

Solution: $t_1 = L/v_{\text{boat,stream}}$; $t_2 = L/[(v_{\text{boat,stream}} - (v_{\text{stream}}^2/v_{\text{boat,stream}})]$: $t_1 < t_2$

19. The speed of light is

A. $3 \times 10^8 \,\text{m/s}$

B. 3×10^6 m/s

C. 3×10^9 m/s

D. 3×10^7 m/s

ANS: A

20. The quantity which does not change in numerical value from that observed in system S when observed in system S' moving away from system S at speed v is

A. $(\Delta x)^2 - (c\Delta t)^2$ B. $m_0 v$ C. $(\gamma - 1) m_0 c^2$ D. (None of A, B, C) ANS: A (Serway test bank, Chap 39, Q33)

ZCT 104/3E Modern Physics Semester II, Sessi 2005/06 Test II (24 March 2006)

Data

Speed of light in free space, $c = 3.00 \times 10^8 \text{ ms}^{-1}$ Elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$ The Planck constant, $h = 6.63 \times 10^{-34} \text{ J s}$ Unified atomic mass constant, $u = 1.66 \times 10^{-27} \text{ kg}$ Rest mass of electron, $m_e = 9.11 \times 10^{-31} \text{ kg}$ Rest mass of proton, $m_p = 1.67 \times 10^{-27} \text{ kg}$

- 1. Which of the following statements is true regarding Rayleigh-Jeans explanation of the blackbody radiation?
 - A. The classical theory explanation of the blackbody radiation by Rayleigh-Jeans fails in the limit wavelength $\stackrel{\sim}{\to} 0$.
 - B. The classical theory explanation of the blackbody radiation by Rayleigh-Jeans fails in the limit frequency → 0.
 - C. They postulate that the energy of electromagnetic waves is quantised.
 - D. None of the above.
 - ANS: A
- 2. Which of the following statements is (are) true regarding Planck theory of the blackbody radiation?
 - I. The energy of the blackbody radiation is quantised. (T)
 - II. The average energy of blackbody radiation is given by $\varepsilon = kT$. (F)
 - III. There is no ultraviolet catastrophe. (T)

A. I Only B. II Only C. I, II D. I, III ANS:D, Tut 2 04/05, CQ 1,2

- 3. What are the flaws in Rayleigh-Jeans law for blackbody radiation?
 - I. It predicts ultraviolet catastrophe (T)
 - II. It predicts much more power output from a black-body than is observed experimentally. (T)
 - III. Blackbody radiation is universal and depends only on temperature. (Not a flaw)

A. I Only	B. II Only	C. I, II	D. I, III
ANS:C, Tut 2 04/05	, CQ 3		

4. What are the distinctive physical characteristics that exclusively differentiate a classical particle from a classical wave?

	Classical Particle	Classical Wave
I.	Completely localized	A wave can be "simultaneously everywhere" at a given
		instance in time
II.	Is has mass	No mass is associated with a classical wave.
III.	Energy is concentrated in it and is not	Energy carried by wave spreads over a (possibly infinite)
	spreading beyond the boundary that	region of space along the direction the wave propagates
	defines its physical location.	
IV.	Momentum and position can be measured	No momentum or precise location can be defined for a
	with infinite precision.	wave
A.	I, II, III, IV B. I, II, III	C. I, II, IV D. None of A, B, C.

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ANS:A, Tut 2 04/05, CQ 4

SESSI 05/06/TEST II

- 5. The Compton-scattering formula suggests that objects viewed from different angles should reflect light of different wavelengths. Why don't we observe a change in colour of objects as we change the viewing angle?
 - A. There is actually no change in the wavelength as predicted by the Compton-scattering formula.
 - B. Because the change in wavelength is too tiny to be observed by human eye.
 - C. Visible light doesn't undergo Compton scattering.
 - D. None of A, B, C.
 - ANS:B, Tut 2, 05/06, Q6
- 6. In Compton scattering, the maximum wavelength shift is in the order of
 - A. $\sim pm$ B. $\sim nm$ C. $\sim \mu m$
 - C. ∼µm
 - D. ~mm

ANS:A, $\Delta \lambda_{max} = 2 \lambda_e = 2.43 \text{pm}$. (My Own Question)

7. Compton wavelength of the electron is given by $\lambda_e = \frac{h}{m_e c}$. What will the size of the Compton wavelength of a

proton be in comparison to λ_e ?

- A. λ_{proton} shall be larger than λ_e by about 2 orders of magnitude.
- B. λ_{proton} shall be smaller than λ_e by about 2 orders of magnitude.
- C. λ_{proton} shall be of the same order of magnitude with λ_{e} .
- D. None of A, B, C

ANS:D,
$$\lambda_e = \frac{h}{m_e c}$$
; $\lambda_p = \frac{h}{m_p c} \Rightarrow \lambda_p = \lambda_e \frac{m_e}{m_p} \sim \frac{1 \text{ MeV}}{1000 \text{ MeV}} \lambda_e = 10^{-3} \lambda_e$. (My Own Question)

- 8. Which of the following statements is (are) true?
 - I. The photoelectric effect doesn't work for free electron (T)
 - II. The Compton effect doesn't work for free electron (F)
 - III. Pair production does not occurs in free space (T)
 - IV. Pair annihilation between an electron and positron does not occurs in free space (F)

A. I, II, III, IV	B. I, II, III	C. I, II, IV	D. None of A, B, C.
ANS:D, I, III are true; I	I, IV are false. (N	My Own Question)	

- 9. Which of the observed properties of the photoelectric effect fail to be accounted for by the wave nature of light?
 - I. Photoelectron is emitted almost instantaneously. (T)
 - II. The saturation photoelectric current increases as intensity increases. (F)
 - III. Stopping potential is independent of the radiation intensity. (T)
 - IV. Existence of the cut-off frequency. (T)

A. I, II, III, IV	B. II, III, IV	C. I, III, IV	D. None of A, B, C.
ANS:C, I, II are true; I	I, IV are false. (My	Own Question)	

10. Which of the following statements is (are) true?

- I. The photoelectric effect is essentially a non-relativistic phenomena. (T)
- II. The Compton effect is essentially a relativistic phenomena. (T)
- III. Pair production is essentially a non-relativistic phenomena. (F)
- IV. Pair production is essentially a relativistic phenomena. (T)

A. I, II, III, IV B. I, II, III C. I, II, IV D. None of A,	, B, C.
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SESSI 05/06/TEST II

ANS: C. (My Own Question)

11. Which of the following statements is (are) true?

- I. X-ray diffraction can be experimentally discernable if it is scattered by atoms in a crystal lattice. (T)
- II. X-ray diffraction is experimentally discernable if it is scattered by an optical diffraction grating with line density 3,000 lines per mm. (F)
- III. The energy of an X-ray photon is much larger than that of an ordinary photon in the visible part of the EM spectrum. (T)
- IV. X-rays wavelength lies approximately in the order of 400 nm ~ 700 nm. (F)

A. I, II, III, IV B. I, II, III C. I, II, IV D. None of A, B, C. ANS: (Only I, III are true) D. (My Own Question)

12. Why can't a photon undergoes pair production in free space?

- I. Because the photon doesn't has sufficient energy in free space. (F)
- II. Because the photon doesn't has sufficient momentum in free space. (F)

III. Because it is not possible to conserve both energy and moment simultaneously in free space. (T)

IV. Because it is not possible to create matter out of pure energy. (F)

A. I, II, III B. II, III, IV C. I, III, IV D. None of A, B, C. ANS:D. Only III is true. The rest is not. (My Own Question). For (I), even if the photon has sufficient energy pair production wouldn't happen as long as it is in free space. For II, 'sufficiency' in momentum is not an issue. The important issue is whether the momentum is conserved in a process, and whether the process is in vacuum. For (IV), it is possible to create matter out of pure energy from $E=mc^2$.

13. Which of the following statements is (are) true regarding electron?

- I. Electron behaves like wave in a diffraction experiment. (T)
- II. Electron behaves like particle in a photoelectric experiment. (T)
- III. Electron behaves like particle in a Compton scattering experiment. (T)
- IV. Electron can manifest both particle and wave nature in a single experiment. (F)

A. I, II, III B. I, II, III, IV C. I, III, IV D. None of A, B, C. ANS: A. (My Own Ouestion)

- 14. Consider a matter particle with rest mass m_0 , moving with a speed v. Which of the following statements is (are) true regarding its de Broglie wave?
 - I. The de Broglie wavelength of the matter particle is $\lambda = h/(m_0 v)$ regardless of whether the particle is relativistic or not (F).
 - II. The de Broglie wavelength of the matter particle is $\lambda = h/(m_0 v)$ only if it is non relativistic (T).
 - III. The de Broglie wavelength of the matter particle is not given by $\lambda = h/(m_0 v)$ if it is relativistic (T).
 - IV. If the speed v of the matter particle is relativistic, its de Broglie wavelength is larger than $h/(m_0 v)$. (F)

A. I, II, III B. II, III C. I, II, IV D. None of A, B, C. ANS: B. (My Own Question)

For IV: $\lambda_{NR} = h/(m_0 v) = h/p_{NR}$; $\lambda_R = h/(p_R)$; $\lambda_R = h/(p_R)$; $\lambda_R = \lambda_{NR} (p_{NR}/p_R) = \lambda_{NR}/\gamma \Rightarrow \lambda_R < \lambda_{NR} = h/(m_0 v)$.

- 15. Which of the statements is (are) true regarding a proton-antiproton annihilation process into photon.
 - I. The annihilation must produce at least two daughter photons. (T)
 - II. The proton-antiproton annihilation would produce photons which are much energetic than that produced by electron-positron annihilation. (T)
 - III. Each daughter photon produced must be at least of energy $2m_pc^2$ (m_p is the mass of the proton). (F)
 - IV. The magnitude of momentum of each daughter photon produced must be at least $m_p c$ (m_p is the mass of the proton). (T)

A. I, II, III, IV	B. II, III, IV	C. I, II, IV	D. None of A, B, C.
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SESSI 05/06/TEST II

- ANS: C. (My Own Question)
- 16. Consider a very weak light beam strikes a fluorescence screen with one photon in a time. The detection of the photon is displayed as a dot on the screen. In this process, the light being detected is

A. a particle B. a wave C. neither a wave nor a particle D. both wave and particle ANS: A

17. Consider a very weak electron beam strikes a fluorescence screen with one electron in a time. The detection of the electron is displayed as a dot on the screen. In this process, the electron being detected is

A. a particle B. a wave C. neither a wave nor a particle D. both wave and particle ANS: A

18. A wavepulse is a result of superposition of many different waves with a spread in wave number, Δk . The width of the wavepulse, Δx , is quantitatively related to Δk as

A. $\Delta x \propto \Delta k$ B. $\Delta x \propto 1/\Delta k$ C. Δx not related to Δk D. None of A, B, C, D ANS: B

19. Which of the following statements is (are) true?

- I. In an experiment, we use a light of certain wavelength to probe a quantum particle. If we use a light with <u>smaller</u> wavelength we will obtain a <u>less</u> precise knowledge about the position of the quantum particle and also a <u>more</u> precise knowledge on the linear momentum of the quantum particle. (F)
- II. In an experiment, we use a light of certain wavelength to probe a quantum particle. If we use a light with <u>smaller</u> wavelength we will obtain a <u>more</u> precise knowledge about the position of the quantum particle and a <u>less</u> precise knowledge on the linear momentum of the quantum particle. (T)
- III. In an experiment, we use a light of certain wavelength to probe a quantum particle. If we use a light with <u>larger</u> wavelength we will obtain a <u>more</u> precise knowledge about the position of the quantum particle and also a <u>less</u> precise knowledge on the linear momentum of the quantum particle. (F)
- IV. In an experiment, we use a light of certain wavelength to probe a quantum particle. If we use a light with <u>larger</u> wavelength we will obtain a <u>less</u> precise knowledge about the position of the quantum particle and a <u>more</u> precise knowledge on the linear momentum of the quantum particle. (T)

A. I, III B. II, IV C. I, IV D. II, III

ANS: B

- 20. The diameter of an atomic nucleus is about 10×10^{-15} m. In order to study the diffraction of photons by nuclei, the energy of the photon has to be in the range of order
 - A. $\sim eV$
 - $B.\ \sim keV$

3

C. ~ MeV D. None of A. B. C

D. None of A, B, C

ANS:D, Tut 2, 05/06, Q3

$$E = \frac{hc}{\lambda} = \frac{1240\text{nm} \cdot \text{eV}}{10 \times 10^{-15} \text{m}} = \frac{1.24 \times 10^3 \times 10^{-9} \text{m} \cdot \text{eV}}{10^{-14} \text{m}} = 1.24 \times 10^8 \text{eV} - 10^2 \text{MeV}$$

UNIVERSITI SAINS MALAYSIA

Final Exam Academic Session 2005/2006

April 2006

ZCT 104E/3 - Physics IV (Modern Physics) [Fizik IV (Fizik Moden)]

Duration: 3 hours [Masa: 3 jam]

Please check that the examination paper consists of xx pages of printed material before you begin the examination.

[Sila pastikan bahawa kertas peperiksaan ini mengandungi xx muka surat yang bercetak sebelum anda memulakan peperiksaan ini.]

Instruction:

Answer ALL questions in Section A and Section B.

Please answer the objective questions from Section A in the objective answer sheet provided. Please submit the objective answer sheet and the answers to the structured questions separately.

Students are allowed to answer all questions in Bahasa Malaysia or in English.

[Arahan: Jawab SEMUA soalan dalam Bahagian A dan Bahagian B.

Sila jawab soalan-soalan objektif daripada bahagian A dalam kertas jawapan objektif yang dibekalkan. Sila serahkan kertas jawapan objektif dan jawapan kepada soalan-soalan struktur berasingan.

Pelajar dibenarkan untuk menjawab samada dalam bahasa Malaysia atau bahasa Inggeris.]

Data

Speed of light in free space, $c = 3.00 \times 10^8$ m s⁻¹ Permeability of free space, $m_0 = 4\pi \times 10^7$ H m⁻¹ Permittivity of free space, $e_0 = 8.85 \times 10^{-12}$ F m⁻¹ Elementary charge, $e = 1.60 \times 10^{-19}$ C Planck constant, $h = 6.63 \times 10^{-34}$ J s Unified atomic mass constant, $u = 1.66 \times 10^{-27}$ kg Rest mass of electron, $m_e = 9.11 \times 10^{-31}$ kg Rest mass of proton, $m_p = 1.67 \times 10^{-27}$ kg Molar gas constant, $N_A = 6.02 \times 10^{-23}$ mol⁻¹ Avogadro constant, $N_A = 6.02 \times 10^{-23}$ mol⁻¹ Gravitational constant, $G = 6.67 \times 10^{-11}$ N m² kg⁻² SESSI 05/06/FINAL EXAM Section A: Objectives. [40 marks] [Bahagian A: Soalan-soalan objektif]

Instruction: Answer all 40 objective questions in this Section.

[Arahan: Jawab kesemua 40 soalan objektif dalam Bahagian ini.]

 While standing beside a railroad track, we are startled by a boxcar traveling past us at half the speed of light. A passenger standing at the rear of the boxcar fires a laser pulse toward the front of the boxcar. The pulse is absorbed at the front of the box car. While standing beside the track we measure the speed of the pulse through the open side door. The measured value of the speed of the pulse is ______ its speed measured by the rider.

[Kita berdiri di tepi suatu landasan keretapi. Suatu gerabak bergerak melepasi kita dengan halaju separuh halaju cahaya. Seorang penumpang yang berdiri di bahagian belakang gerabakmenembak suatu denyutan laser ke arah bahagian hadapan gerabak. Denyutan tersebut diserap pada bahagian hadapan gerabak. Ketika berdiri di tepi landasan kita mengukur laju denyutan laser tersebut menerusi pintu tepi yang terbuka. Nilai bagi laju denyutan laser yang kita ukur adalah ______ laju yang diukur oleh penumpang.]

- A. greater than [lebih besar daripada]
- B. equal to [samadengan]
- C. less than [kurangdaripada]
- D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS:B, My own questions

- 2. Refering to question No.1 above, our measurement of the distance between emission and absorption of the laser pulse is ______ the distance between emission and absorption measured by the rider. [Merujuk kepada soalan 1 di atas, ukuran yang kita lakukan ke atas jarak di antara pemancaran dan penyerapandenyutan laser adalah ______ jarak di antara pemancaran dan penyerapan yang diukur oleh penumpang tersebut.]
 - A. greater than [lebih besar daripada]
 - B. equal to [samadengan]
 - C. less than [kurangdaripada]
 - D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]
 - ANS:A, My own questions

1

3. Given two events, A and B, of which the space and time coordinate are respectively designated by (x_A, t_A) and (x_B, t_B) . If we define the space-time interval squared as $s^2 = (c\Delta t)^2 - (\Delta x)^2$, which of the following statements are (is) true?

[Diberikan dua kejadian, A dan B, yang koordinat-koordinat ruang dan masa masing-masing diberi oleh (x_A , t_A) dan (x_B , t_B). Jika kita takrifkan kuasadua selang ruang-masa sebagai $s^2 = (c\Delta t)^2 - (\Delta x)^2$, yang manakah kenyataan(-kenyataan) berikut adalah benar?]

- I. Both events may be causally related if the space-time interval squared between them is space-like. [Kedua-dua kejadian mungkin berkaitsecara sebab-akibat jika kuasadua selang ruang-masa antara mereka adalah bak ruangan.]
- II. Both events must not be causally related if the space-time interval squared between them is space-like. [Kedua-dua kejadian mesti tak berkait secara sebab-akibat jika kuasadua selang ruang-masa antara mereka adalah bak ruangan.]
- III. Both events may be causally related if the space-time interval squared between them is time-like. [Kedua-dua kejadian mungkin berkait secara sebab-akibat jika kuasadua selang ruang-masa antara mereka adalah bak masa.]
- IV. Both events must be causally related if the space-time interval squared between them is time-like. [Kedua-dua kejadian mestiberkait secara sebab-akibatjika kuasadua selang ruang-masa antara meraka adalah bakruangan.] 291

- A. I, II
- B. II, III
- C. II, III, IV
- D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]
- ANS: B
- 4. Say Azmi is travelling in a mini bus moving with a constant speed ν (with respect to Earth) and Baba is sitting in Pelita Nasi Kandar restaurant. Using his own wristwatch, Baba finds that his heart beats at a rate of M_B times per min. When Azmi measures the heartbeat rate of Baba in the mini bus frame, he found that Baba's heart is beating at a rate of M_A times a min. What is the relation between the two reading, M_A and M_B ?

[Katakan Azmi berada di dalam sebuah bas mini yang bergerak dengan laju malar v (merujuk kepada Bumi) manakala Baba sedang duduk di dalam restoran Nasi Kandar Pelita. Dengan menggunakan jam tangannya, Babamendapati jantungnya berdenyut pada kadar $M_{\rm B}$ kali per minit. Semasa Azmi mengukur kadardenyutan Baba di dalam rangka bus mini, dia mendapati jantung Baba berdenyut pada kadar $M_{\rm A}$ kali seminit. Apakah hubungan antarakedua-duabacaan $M_{\rm A}$ dan $M_{\rm B}$?]

- A. $M_{\rm A} > M_{\rm B}$
- B. $M_A < M_B$
- C. $M_{\rm A} = M_{\rm B}$

D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: B

5. Consider a football, kicked lightly by David Beckham, is moving in a straight line with a constant speed. Say in frame O, the momentum of the football is *P*. In a frame O' moving with a relative constant speed *v* with respect to O, the momentum of the football is P'. Which of the following statements are (is) true regarding *P* and P'? The Lorentz factor is defined as $\gamma = [1 - (v/c)^2]^{-1/2}$.

[Pertimbangkan sebiji bola sepak yang ditendang secara lembut oleh David Beckham dan bergerak dalam satu garis lurus dengan laju mantap. Katakan dalam rangka O, momentum bola sepak ialah P. Di dalam rangka O' yang bergerak dengan laju relatifmantap v merujuk kepada O, momentum bola sepak tersebut ialah P'. Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai P dan P'? Faktor Lorentz adalah ditakrifkan sebagai $\mathbf{g} = [1-(v/c)^2 \Gamma^{1/2}.]$

- I. Since momentum is not an invariant quantity, the numerical values of P and P' are not the same. [Oleh sebab momentum bukan kuantiti tak varian, nilai numerik P adalah tidak sama dengan nilai numerik P'.]
- II. Since momentum is an invariant quantity, the numerical values of P and P' are the same. [Oleh sebab momentum adalah suatu kuantiti tak varian, nilai numerik P adalah sama dengan nilai numerik P'.]
- III. *P* and *P'* are related by P=P' / g [P dan P' a dalah dikaitkan oleh P=P' / g]
- IV. *P* and *P'* are related by P=gP' [*P* dan *P'* adalah dikaitkan oleh P=gP']
 - A. I, III
 - B. II, IV
 - C. IONLY
 - D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]
- ANS: C [Neither III or IV is true.]
- 6. Which of the following statements is (are) true regarding the linear momentum of an object? (ν denotes the speed of the object).

[Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai momentum linear suatu objek? (vmenandai laju objek)]

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I. The relativistic momentum and the classical momentum of an object have the same numerical value when v = c

[Kedua-dua momentum kerelatifan dan momentum klasik suatu objek mempunyai nilai numerik yang sama bila vc.]

II. The relativistic momentum and the classical momentum of an object has the same numerical value when v is close to c

[Kedua-dua momentum kerelatifan dan momentum klasik suatu objek mempunyai nilai numerik yang sama bila v mendekati c.]

III. The ratio of relativistic momentum to classical momentum of an object approaches infinity when v approaches c

 $[\ensuremath{\bar{N}}\xspace{issues} is summarized with the second state of the second$

IV. The ratio of relativistic momentum to classical momentum of an object approaches 0 when v is tiny compared to c.

[Nisbah momentum kerelatifan kepada momentum klasik suatu objek menokok ke sifar bila v adalah kecil berbanding denganc.]

- A. I, III, IV
- B. II, IV
- C. I, III
- D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: C

- 7. Which of the following statements is (are) true regarding the kinetic energy of an object? [Yang manakah kenyataan(-kenyataan) berikut adalah benarmengenai tenagakinetik suatu objek?]
- I. In classical mechanics *per se*, the kinetic energy of an object can increase without limit. [Dengan hanyamempertimbangkan mekanikklasik, tenaga kinetik suatu objek boleh bertambah tanpa limit.]
- II. In special relativity, the kinetic energy of an object can increase without limit. [Dalam kerelatifan, tenaga kinetik suatu objek boleh bertambah tanpa limit.]
- III. In special relativity, the kinetic energy of an object cannot increase without limit. [Dalam kerelatifan, tenaga kinetik suatu objek tidak boleh bertambah tanpa limit.]
- IV. A proton accelerated by a potential difference of 1 keV is non-relativistic. [Suatu proton yang dipecutkan oleh beza keupayaan 1 keVadalah tak kerelatifan]
 - A. I, III, IV
 - B. III, IV
 - C. I, II, IV
 - D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: C

- 8. The relativistic kinetic energy of an object, in general, is [Tenaga kinetik kerelatifan suatu objek, secara amnya, adalah]
 - A. greater than that defined by the classical mechanics by a factor of γ [*lebih besar daripada yang ditakrifkan oleh mekanik klasik sebanyak suatufactor* γ]
 - B. less than that defined by the classical mechanics by a factor of γ [lebih kecil daripada yang ditakrifkan oleh mekanik klasik sebanyak suatu factor γ]
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- C. always equal to that defined by classical mechanics
- [sama dengan yang ditakrifkan oleh mekanik klasik]
- D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: D

- 9. Captain Jirk reports to headquarters that he left the planet Senesca 1.88×10⁴ seconds earlier. Headquarters sends back the message: "Was that spaceship proper time?" It will be the spaceship proper time if it was [Kaptan Jirk melapor kepada pusat kawalan bahawa dia telah meninggalkan planet Senesca sejak 1.88 ´10⁴ saat yang lalu. Pusatkawalan hantar balik mesej: "Adakah masa yang dilaporkan itu masa wajar kapal angkasa?" Ia adalah masa wajar kapal angkasa jika ianya]
 - A. measured by one clock fixed at one spot on Senesca. [diukur oleh suatu jam yang dipasangkan pada suatu titik di atas Senesca.]
 - B. measured by one clock fixed at one spot on the spaceship. [diukur oleh suatu jam yang dipasangkan pada suatu titik di dalam kapal angkasa.]
 - C. measured by a clock on Senesca at departure and by a clock on the spaceship when reporting. [diukur oleh suatu jam di atas Senesca semasa bertolak dan diukur oleh satu lagi jam yang dipasangkan di dalam kapal angkasa semasa melakukan laporan.]
 - D. measured by a clock on the spaceship when departing and by a clock on Senesca when reporting. [diukur oleh suatu jam di dalam kapal angkasa semasa bertolak dan diukur oleh satu lagi jam di atas Senesca semasa melakukan laporan.]

(ANS: B, Q31, Chap 39, Serway test bank)

- 10. Which of the following statements is (are) true regarding the speed of light? [Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai laju cahaya?]
- I. The speed of light in free space (i.e. vacuum) is a fundamental constant. [Laju cahaya di dalam ruang bebas (iaitu vakuum) adalah suatu pemalar asas.]
- II. The speed of light in free space (i.e. vacuum) is the same when measured in different frame of reference. [Laju cahaya di dalam ruang bebas (iaitu vakuum) adalah sama jika diukur di dalam rangka rujukan yang berlainan.]
- III. The speed of light is the same when measured in different medium. [Laju cahaya adalah sama bila diukur di dalam medium yangberlainan.]
- IV. The speed of light is the not same when measured in different medium. [Laju cahaya adalah tidak sama jika diukur di dalam medium yang berlainan.]
 - A. I, II, III
 - B. I, II
 - C. I, II, IV
 - D. (None of A, B, C)

ANS: C

- 11. When two particles collide relativistically, [Bila dua zarah berlanggar secara kerelatifan,]
- I. the total energy is conserved. [jumlah tenaga adalah terabadikan.]
- II. the total momentum is conserved. [jumlah momentum adalah terabadikan.]
- III. the total kinetic energy is conserved. [jumlah tenaga kinetik adalahterabadikan.]
 - A. I, II, III B. II, III

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- C. I, II
- D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]
- ANS: C
- 12. Which of the following statements is (are) true regarding the decay of a pion (initially at rest) into a neutrino (assumed massless) and a muon: $p \rightarrow n + m$.

[Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai reputan suatu pion (dalam keadaan rehat pada mulanya) kepada suatu neutrino (dianggap tanpa jisim) dan suatu muon: $\mathbf{p} \rightarrow \mathbf{n} + \mathbf{m}$?]

- I. The decay is possible only if the mass of pion is larger than the mass of muon. [Reputan adalah mingkin hanya jika jisim pion adalah lebih besar daripada jisim muon.]
- II. The momentum of neutrino and the momentum of muon have the same magnitude. [Momentum neutrino dan momentum muon mempuyai magnitud yang sama.]
- III. The kinetic energy of neutrino is the same as that of the muon. [Tenaga kinetik neutrino adalah sama dengan tenaga kinetik muon.]
- IV. The decay is possible only if the mass of pion is equal to the mass of muon. [Reputan adalah mingkin hanya jika jisim pion adalah sama dengan jisim muon.]
 - A. I, III B. II, III, IV
 - C. I, II
 - D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: C

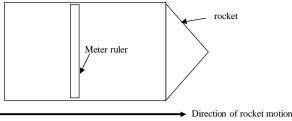
- 13. Which of the following statements is (are) true regarding Lorentz transformation? [Yang manakah kenyataan(-kenyataan) berikutadalah benar mengenai transformasi Lorentz?]
- I. It relates the spatial and temporal coordinate $\{x, t\}$ in one frame to that measured in another frame $\{x', t'\}$. [*Iamengaitkan koordinat-koordinat ruangan dan masa* $\{x, t\}$ *dalam satu rangka dengan* $\{x', t'\}$ yang diukur dalam rangka lain.]
- II. It relates the velocity of an object u_x measured in one frame to that measured in another frame u_x' . [Iamengaitkan halaju suatu objek u_x yang diukur dalam satu rangka dengan u_x' yang diukurkan dalam rangka lain.]
- III. It predicts length contraction. [Iameramalkanpengecutanpanjang.]
- IV. It predicts time dilation. [Iameramalkan pendilatan masa.]
 - A. I, III
 - B. I, II, III, IV
 - C. II, III, IV
 - D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: B

5

14. Consider a meter ruler carried in a rocket moving in a direction perpendicular to the length of the ruler, see figure below.

[Pertimbangkan suatu pembaris meter yang dibawa oleh suatu roket yang bergerak dalam arah yang berserenjang dengan panjang pembaris, rujuk gambarajah.]

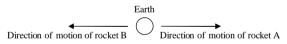


- I. The length of the ruler is 1 m when measured by an observer in the rocket frame. [Panjang pembaris adalah 1 m bila diukur oleh seorang pemerhati di dalam rangka roket.]
- II. The length of the ruler is less than 1 m when measured by an observer in the rocket frame. [Panjang pembaris adalah kurang daripada 1 m bila diukur oleh seorang pemerhati di dalam rangka roket.]
- III. The length of the ruler is less than 1 m when measured by an observer in the lab frame. [Panjang pembaris adalah kurang daripada 1 m bila diukur oleh seorang pemerhati di dalam rangka makmal.]
- IV. The length of the ruler is 1 m when measured by an observer in the lab frame. [Panjang pembaris adalah 1 m bila diukur oleh seorang pemerhati di dalam rangka makmal.]
 - A. I, III
 - B. II, III
 - C. II, IV
 - D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: D (I, IV are true. IV is true because the rule's length is perpendicular to the direction of motion.)

15. Consider two rockets moving in opposit directions away from Earth. See figure below. Rocket A is moving away from Earth at a speed of 0.5*c* while rocket B with a speed of 0.51*c*. Which of the following statements is (are) true?

[Pertimbangkan dua roket yang bergerak dalam dua arah bertentangan, masing-masing menjauhi Bumi. Rujuk gambarajah. Roket A bergerak menjauhi Bumi dengan laju 0.5c manakala roket B dengan laju 0.51c. Yang manakahkenyataan(-kenyataan) berikut adalah benar?]



- I. The magnitude of the relative velocity of rocket A with respect to rocket B is less than 1.01 c. [Magnitud halaju relatif roket A merujuk kepada roket B adalah kurang daripada 1.01c.]
- II. The magnitude of the relative velocity of rocket A with respect to rocket B is less than c. [Magnitud halaju relatif roket A merujuk kepada roket B adalah kurang daripada c.]
- III. The magnitude of the relative velocity of rocket A with respect to rocket B is equal to c. [Magnitud halaju relatif roket A merujuk kepada roket B adalah sama dengan c.]
- IV. The magnitude of the relative velocity of rocket A with respect to rocket B is equal to 1.01 c. [Magnitud halaju relatif roket A merujuk kepada roket B adalah sama dengan 1.01c.]
 - A. I, II
 - B. I, III C. II, IV

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D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] ANS: A

- 16. Which of the following statements is (are) true regarding waves? [Yang manakah kenyataan(-kenyataan) berikutadalah benarmengenai gelombang?]
- I. Wave pulse can be formed by superpositioning many waves with different wavelengths and frequencies. [Denyutan gelombangdapat dibentukkandenganmengsuperposisikangelombang-gelombangyang berjarak gelombang dan berfrekuensi yang berlainan.]
- II. A 1-D wave with sharp wavelength and frequency can be completely localised. [Lokasi suatugelombang 1-D dengan jarak gelombang dan frekuensi tajam boleh ditentukan sepenuhnya.]
- III. A 1-D wave packet is relatively more 'localised' then a 1–D wave with sharp wavelength and frequency. [Lokasi suatu bungkusan gelombang 1-D adalah lebih tentu secara relatifberbanding dengan gelombang 1-D berjarak gelombang dan berfrekuensi tajam.]
- IV. In general, the velocity of an envelope of a group wave is less than that of the phase wave. [Secara amnya, halaju sampul bagi gelombang kumpulan adalah lebih kecil berbanding dengan halaju gelombang fasanya.]
 - A. I, II
 - B. I, III, IV
 - C. II, IV
 - D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: B

- 17. Which of the following statements is (are) true regarding waves and particles? [Yang manakah kenyataan(-kenyataan) berikutadalah benar mengenai gelombang dan zarah?]
- I. Waves interfere but matter does not. [Gelombang berinterferens manakalazarahtidak.]
- II. Waves interfere, so does matter [Gelombangberinterferens, begitu juga bagi zarah.]
- III. Classically, the energy carried by the EM waves is continuous. [Secara klasik, tenaga yang dibawa oleh gelombang EM adalah selanjar.]
- IV. Classically, the energy carried by the EM waves is discrete. [Secara klasik, tenaga yang dibawa oleh gelombang EM adalah diskrit.]
 - A. I, III B. I, IV
 - C. II, IV
 - D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: A (I, III)

- 18. Which of the following statements is (are) true regarding black body radiation? [Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai sinaran jasad hitam?]
- I. The spectrum distribution of black bodies is universal and depends only on temperature. [Taburan spektrum jasad hitam adalah universal dan bergantung semata-mata pada suhu.]
- II. The deviation of any real surface from the behaviour of an ideal black body is parametrised by the emmissivity parateter, e.
 [Sisihan mana-mana permukaan benar daripada kelakuan jasad hitam yang ideal adalah diparameterkan oleh parameter emmissiviti, e.]
- III. A black body in thermal equilibrium absorbs and emit radiation at the same rate.

[Suatu jasad hitam yang berada dalam keseimbangan terma menyerap dan memancarkan sinaran pada kadar yang sama.]

- IV. A black body in thermal equilibrium only emit radiation but not absorbing any. [Suatu jasad hitam yang berada dalam keseimbangan terma hanya memancarkan sinaran tapi tidak menyerap apa-apasinaran.]
 - A. I, II, III
 - B. I, II, IV
 - C. II, III

D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] ANS: A (I, II, III)

- 19. Which of the following statements is (are) true regarding the Rayleigh-Jeans law of black body radiation? [Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai hukum sinaran jasad hitam Rayleigh-Jeans?]
- I. It predicts that the intensity of radiation shoots to infinity when wavelength approaches zero. [Ia meramalkan bahawa keamatan sinaran menembak ke infiniti jika jarak gelombang menokok ke sifar.]
- II. It assumes that the black body radiates electromagnetic waves at all wavelength. [Iamenganggap bahawa jasad hitam memancarkan gelombang elektromagnetpada semua jarak gelombang.]
- III. It assumes that the average energy of each wavelength in a black body is proportional to the frequency. [Ia menganggap bahawa tenaga min bagi setiap jarak gelombang dalam jasad hitam adalah berkadar denganfrekuensi.]
- IV. It assumes that the average energy of each wavelength in a black body is proportional to the temperature. [Iamenganggap bahawa tenaga min bagi setiap jarak gelombang dalam jasad hitam adalah berkadar dengan suhu.]
 - A. I, II, III
 - B. I. II. IV
 - C. I ONLY
- D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] ANS: B (I, II, IV)
- 20. Which of the following statements is (are) the assumption(s) made by Planck in deriving his theory of black body radiation?

[Yang manakahkenyataan(-kenyataan) berikut adalah ang gapan yang dibuat oleh Planck semasa menerbitkan teori sinaran jasad hitamnya?]

- I. That the oscillator of the black body only absorbs and emits radiation with energy of discrete values. [Bahawapengayun di dalam jasad hitam hanyamenyerap dan memancarkan sinaran dengan tenaga bernilai diskrit.]
- II. That the average energy per standing wave in the Planck oscillator, $\langle e \rangle$ is not only temperature dependent but also frequency dependent.

 $[Bahawa tenaga min untuk setiap gelombang pegun dalam pengayun Planck, \langle e \rangle, bukan sahaja bergantung kepada suhu malah juga bergantung kepada frekuensi.]$

- III. That black body radiation is not electromagnetic in nature. [Bahawa tabii sinaran jasad hitam adalah bukanelektromagnetik.]
- IV. That the black body only radiates at the long wavelength region but not in the ultraviolet limit.

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[Bahawa jasad hitam hanya memancar dalam rantau jarak gelombang panjang tapi tidak memancar dalam limit ultraungu.]

- A. I, II, III
- B. I, II, IV
- C. II ONLY
- D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: D (I, II)

- 21. Which of the following statements are (is) true [Yang manakah kenyataan(-kenyataan) berikutadalah benar?]
- I. $hc = 1240 \text{ eV} \cdot \text{nm}$ (Planck constant × speed of light)
- II. $m_e = 0.5 \text{ eV}/c^2$ (electron's mass)
- III. $m_{\rm proton}$ 938 MeV/ c^2 (Proton's mass)
- IV. $a_0 = 0.53$ Å (Bohr's radius)
 - A. I, II, IV
 - B. I, III, IV
 - C. I, II, III, IV

D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: B (I, III, IV)

- 22. Which of the following statements are (is) true regarding photoelectric effect? [Yang manakah kenyataan(-kenyataan) berikutadalah benar mengenai kesan fotoelektrik?]
- I. The maximum photoelectron energy is directly proportional to the frequency of the incident light. [Tenaga kinetikmaksimum fotoelektron adalah berkadar terus dengan frekuensi cahaya tuju.]
- II. The maximum photoelectron energy is a linear function of the frequency of the incident light. [Tenaga kinetikmaksimum fotoelektron adalah suatu fungsi linear frekuensi cahaya tuju.]
- III. The maximum photoelectron energy depends on the material from which the photoelectron emits. [Tenaga kinetikmaksimum fotoelektron bersandar pada jenis bahan daripada mana fotoelektron dipancarkan.]
- IV. The maximum photoelectron energy depends on the intensity of the incident radiation. [Tenagakinetikmaksimumfotoelektron bersandar pada keamatan sinaran tuju.]
 - A. II, III, IV
 - B. II, III
 - C. I, II, III

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D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: B (II, III) (Beiser, Chap 2, Ex. 3)

- 23. Which of the following statements are (is) true regarding light and electron? [Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai cahaya dan elektron?]
- I. The wave aspect of light was discovered earlier than its particle aspect. (T) [Aspek gelombang bagi cahaya ditemui lebih awal daripada aspekzarahnya.]
- II. The wave aspect of electron was discovered earlier than its particle aspect. (F) [Aspek gelombang bagi elektron ditemui lebih awal daripada aspekzarahnya.]

- III. The particle aspect of light was discovered earlier than its wave aspect. (F) [Aspek zarah bagi cahaya ditemui lebih awal daripada aspekgelombangnya.]
- IV. The particle aspect of electron was discovered earlier than its wave aspect. (T) [Aspek zarah bagi elektron ditemui lebih awal daripada aspekgelombangnya.]
 - A. I, IV
 - B. II, III
 - C. I, II
 - D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]
- ANS: A (I, IV, Beiser, Chap 2, Ex. 4)
- 24. Which of the following statements are (is) true? [Yang manakah kenyataan(-kenyataan)berikutadalah benar?]
- I. It is impossible for a photon to give up all of its energy to a free electron. [Adalah tidak mungkin bagi suatu foton memberikan kesemua tenaganya kepada suatu elektron bebas.]
- II. It is impossible for a photon to give up all of its momentum to a free electron. [Adalah tidak mungkin bagi suatu foton memberikan kesemua momentumnya kepada suatu elektron bebas.]
- III. It is impossible for a photon to give up all of its energy to an atom. [Adalah tidak mungkin bagi suatu foton memberikan kesemua tenaganya kepada suatu atom.]
- IV. It is impossible for a photon to give up all of its momentum to an atom. [Adalah tidak mungkin bagi suatu foton memberikan kesemua momentumnya kepada suatu atom.]
 - A. I, IV
 - B. III, IV
 - C. I, II
 - D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: C (I, II, Beiser, Chap 2, Ex. 19)

- 25. Which of the following are (is) true regarding the photoelectric effect? [Yang manakah kenyataan(-kenyataan)berikutadalah benar mengenai kesan fotoelektrik?]
- I. The existence of a cutoff frequency in the photoelectric effect favours a particle theory for light rather than a wave theory.

[Kewujudan frekuensiambang dalam kesan fotoelektrik menyebelahi teori zarah bagi cahaya berbanding dengan teori gelombang.]

II. The existence of a cutoff frequency in the photoelectric effect favours a wave theory for light rather than a particle theory.

[Kewujudan frekuensi ambang dalam kesan fotoelektrik menyebelahi teori gelombang bagi cahaya berbanding dengan teori zarah.]

III. The almost immediate emission of a photoelectron in the photoelectric effect favours a particle theory for light rather than a wave theory.

[Pancaran fotoelektron yang lebih kurang serentak menyebelahi teori zarah bagi cahayaberbanding dengan teorigelombang.]

IV. The almost immediate emission of a photoelectron in the photoelectric effect favours a wave theory for light rather than a particle theory. [Pancaran fotoelektron yang lebih kurang serentak menyebelahi teori gelombang bagi cahaya berbanding dengan teori zarah.]

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- A. I, III
- B. I, IV C. II, IV
 - II, IV
- D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: A (I, III, Serway, Moses and Moyer, Chap 3, Question. 7)

- 26. Which of the following are (is) true regarding X-rays? [Yang manakah kenyataan(-kenyataan) berikutadalah benar mengenai sinaran-X?]
- I. X-rays might be reasonably be called 'the inverse photoelectric effect'. [Adalah munasabah untuk sinaran-X dikenali sebagai 'kesan fotoelektrik songsangan']
- II. In X-rays production, part or all of the energy of a photon is converted into the kinetic energy of a fast moving electron.
 [Dalam penghasilan sinaran-X, sebahagian atau keseluruhan tenaga suatu foton ditukarkan kepada tenaga kinetik elektron yang pantas bergerak.]
- III. In X-rays production, part or all of the energy of a fast moving electron is converted into a photon. [Dalampenghasilan sinaran-X, sebahagian atau keseluruhan tenaga kinetik suatu elektron yang pantas bergerak ditukarkan kepada suatu foton.]
- IV. The penetrative character of X-rays through matter is partly due to its short wavelength. [Salah satu sebab bagi ciripenembusan sinaran-X melalui jirim adalah kerana jarak gelombang nyayang pendek.]
 - A. I, III
 - B. I, II, IV
 - C. II, IV
 - D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: D (I, III, IV, Beiser, Chap 2.5, pg. 68)

27. The figure below shows the x-ray spectrum of a metal target from a x-ray tube. Which of the following statements are (is) true?

[Gambarajah berikut memaparkan spektrum sinaran-X daripada sasaran logam suatu tiub sinaran-X. Yang manakah kenyataan (-kenyataan) berikut adalah benar?]

- I. The broad continuous spectrum is well explained by classical electromagnetic theory. [Spektrum selanjaryang lebaradalah diterangkan dengan baiknya
- II. The existence of I_{\min} in the spectrum shows proof of the photon theory. [Kewujudan I_{\min} dalam spektrum menunjukkan bukti bagi teori foton.]
- III. I_{\min} is found to be independent of target composition.

 $[Didapati\,l_{\min}\,adalah\,merdeka\,daripada\,komposisis asaran.]$

IV. l_{\min} depends only on the tube voltage.

oleh teori electromagnet klasik.]

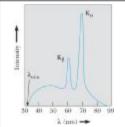
[Didapati l_{\min} hanya bergantung kepada voltan tiub.]

- A. I, III, IV
- B. I, II, III, IV

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- C. II, IV
- D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: B (I, II, III, IV, Serway, Moses and Moyer, Chap 3, pg. 88)



28. Consider a Compton scattering experiment in which the incident radiation with various wavelength λ is aimed at a block of graphite target. The scattered radiation are observed and their Compton shifts are measured at an angle of $\theta = 90^{\circ}$. Which of the following are (is) true?

 $[Pertimbangkan suatu eksperimen serakan Compton. Sinaran tuju dengan berbagai-bagai jarak gelombang 1 dikenakan ke atas sasaran blok grafit. Sinaran terserak dicerap dan anjakan Compton mereka diukur pada sudut <math>\theta = 90^{\circ}$. Yang manakah kenyataan(-kenyataan) berikut adalah benar?]

- I. Regardless of the incident radiation wavelength used, the same Compton shift, ΔI , is observed. [Anjakan Compton yang sama, ΔI , akan didapati tidak kisah apa nilai λ yang digunakan.]
- II. The fractional change in wavelength, $\Delta\lambda\lambda\lambda$, is the same for different λ . [Nisbah perubahan dalam jarak gelombang, $\Delta\lambda\lambda\lambda$, adalah sama untuk semua nilai λ .]
- III. Compared with the energy of a X-ray photon, the binding energy of an electron to the graphite atom in the target is negligible. [Berbandingdengantenaga foton sinaran-X, tenaga ikatan elektron kepada atom grafit di dalam sasaran

[Berbanding dengantenaga foton sinaran-X, tenaga ikatan elektron kepada atom grafit di dalam sasa adalahterabaikan.]

- A. I, III
- B. II, III
- C. I, II, III

D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: A (I, III, Serway, Moses and Moyer, Chap 3, Example 3.8)

- 29. Which of the following statements are (is) true regarding Compton scattering? [Yang manakah kenyataan(-kenyataan)berikut adalah benar mengenai serakan Compton?]
- I. The Compton effect could not be accounted for by classical theories. (T) [Kesan Compton tidakboleh diterangkan oleh teori-teori klasik.]
- II. The Compton effect could not be accounted for if not treated relativistically. (T) [Kesan Compton tidak boleh diterangkan jika tidak dirawat secara kerelatifan.]
- III. The Compton effect could still be accounted for if not treated relativistically. (F) [Kesan Compton boleh diterangkan walaupun tidak dirawat secara kerelatifan.]
 - A. L.III
 - B. IONLY
 - C. I, II
 - D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: C (My own question)

30. Consider a photon with initial wavelength λ being scattered off by a particle with mass *m*. The Compton shift $\Delta\lambda$ of the radiation at a given angle

 $[Pertimbangkan suatu foton berjarak gelombang awal 1 diserak kan oleh suatu zarah dengan jisim m. Anjakan Compton \Delta \lambda sinaran tersebut pada suatu sudut tertentu]$

- A. would be smaller for a larger *m*, [*adalah lebih kecil bagi nilai m yang lebih besar*]
- B. would be larger for a larger *m*. [adalah lebih besar bagi nilai m yang lebih besar]
- C. would remain unchanged for a larger *m*. [*tidak akan berubah walaupun bagi nilai m yang lebih besar.*]

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D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: A (My own question)

31. Radiation interacts with matter chiefly through photoelectric effect, Compton scattering and pair production. The relative importance of the interactions shift from ______ to _____ to _____ to _____ when energy of the photon increases.

[Sinaran berinteraksi dengan jirim terutamanya melalui kesan-kesan fotoelektrik, serakan Compton dan penghasilan pasangan. Kepentingan relatif interaksi-interaksi tersebut berubah dari _______ke ke ke bila tenaga foton bertambah. J

- A. Compton scattering, Photoelectric effect, Pair production
- B. Pair production, Compton scattering, Photoelectric effect
- C. Pair production, Photoelectric effect, Compton scattering
- D. Photoelectric effect, Compton scattering, Pair production

ANS: D (My own question)

32. Heisenberg's uncertainty principle [PrinsipketidakpastianHeisenberg]

- I. is seldom important on macroscopic level [jarang menjadi mustahak pada tahap makroskopik.]
- II. is frequently very important on the microscopic level. [sering menjadi mustahak pada tahap mikroskopik.]
- III. implies that one can simultaneously measure the position and momentum of a particle with zero uncertainties. [mengimplikasikan bahawa seseorang dapat mengukur secara serentak kedudukan dan momentum sesuatu zarah dengan sifar ketidak pastian.]
- IV. implies that one cannot simultaneously measure the position and momentum of a particle with any certainty. [mengimplikasikanbahawa seseorang tidak dapat mengukur kedudukan dan momentum sesuatu zarah dengan apa jua kepastian.]
- A. I, II, III
- B. I, II, IV
- C. I, II D. (Nor

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D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: C (Taylor et al., Chap. 6, pg. 191)

- 33. Which of the following is (are) true according to Heisenberg's time-energy uncertainty relation $\Delta E \Delta t \ge \mathbf{h}/2$? [Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai hubungan ketidak pastian masatenaga Heisenberg $\Delta E \Delta t \ge \mathbf{h}/2$?]
 - I. For a quantum particle that exists for a short period of Δt , the particle must have a large uncertainty ΔE in its energy.

[Bagi suatu zarah kuantum yang wujud untuk suatu selang masa Δt yang singkat, zarah tersebut mestimempunyai ketidak pastian tenaga ΔE yang besar.]

II. For a quantum particle that has a large uncertainty of ΔE in its energy, it must exists only for a short period of Δt

[Bagi suatu zarah kuantum yang mempunyai ketidak pastian tenaga ΔE yang besar, ia mesti hanya wujud untuk suatu selang masa Δt yang singkat.]

- III. If a quantum particle has a definite energy, then $\Delta E = 0$, and Δt must be infinite. [Jika suatu zarah kuantum mempunyai tenaga yang pasti, maka $\Delta E = 0$ dan Δt mestilah menjadi infinit.]
- IV. If a quantum particle does not remain in the same state forever, Δt is finite and ΔE cannot be zero. [Jika suatu zarah kuantum tidak berkekal pada keadaan yang sama untuk selama-lamanya, maka Δt adalah finit, dan ΔE tidak boleh jadi sifar.]
- A. I, II, III
- B. II, III, IV
- C. I, II, III, IV
- D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]
- ANS: C (Taylor et al., Chap. 6, pg. 193)

kenvataan)berikutadalahbenar?1

- 34. Consider a quantum particle confined in an infinite potential well of width L. Its states are characterised by the non-zero quantum integer n. Which of the following statements is (are) true? [Pertimbangkan suatu zarah kuantum yang terkongkong di dalam telaga segiempat infinit selebar L. Keadaannya adalah dicirikan oleh nombor kuantum integer bukan sifar n. Yang manakah kenyataan(-
 - I. The allowed energies of the particle are discrete [Tenaga yang diizinkan zarah itu adalah diskrit.]
 - II. There allowed energy levels are farther and farther apart as the quantum number *n* increases. [*Paras tenaga yang diizinkan menjadi makin terpisah bila nombor kuantum n makin menambah.*]
 - III. The energy level of the particle's state E_n increases without limit as $n \mathbf{a} \infty$. [Paras tenaga zarah, E_n , menambah tanpa batas bila $n \mathbf{a} \infty$.]
 - IV. The number of nodes of the wave function of the particle increases with *n*. [Bilangan nod fungsi gelombang zarah bertambah bila n bertambah.]
 - A. I, II, IV
 - B. I, III, IV
 - C. II, III, IV
 - D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]
- ANS: D (All are true, Taylor et al., Chap. 6, pg. 210, 211)
- 35. Consider the Bohr's model of hydrogen-like atom. Its states are characterised by the non-zero quantum integer *n*. Which of the following statements is (are) true?

[Pertimbangkan atom bak hidrogen model Bohr. Keadaannya adalah dicirikan oleh nomborkuantum integer bukan sifar n. Yang manakah kenyataan(-kenyataan) berikut adalah benar?]

- I. The allowed energies of the electron in the atom are discrete at low values of *n* [Paras tenaga yang diizinkan bagi elektron dalam atom adalah diskrit bagi nilai n yang kecil.]
- II. The allowed energies of the electron in the atom becomes quasi continous at large values of *n*. [Paras tenaga yang diizinkan bagi elektron dalam atom menjadi kuasi-selanjar untuk nilai n yang besar.]
- III. The allowed energy levels are farther and farther apart as the quantum number *n* increases. [Paras tenaga yang diizinkan menjadi makin terpisah bila nombor kuantumn makin menambah.]
- IV. The energy level, E_n , increases without limit as $n \mathbf{a} \propto$. [Parastenaga, E_n , menambah tanpa batas bila $n \mathbf{a} \sim$.]

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- A. I, II, III
- B. I, II, IV
- C. I, II
- D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: C (Only I, II is true. My own question)

36. Consider the Bohr's model of hydrogen-like atom. Its states are characterised by the non-zero quantum integer *n*. Which of the following statements is (are) true?

[Pertimbangkan atom bak hidrogen model Bohr. Keadaannya adalah dicirikan oleh nombor kuantum integer bukan sifar n. Yang manakah kenyataan(-kenyataan) berikut adalah benar?]

- I. The larger the value of *n* the larger the electron's velocity becomes. [Halaju elektron menjadi makin besar bila nilai n majadi makin besar.]
- II. The electron's linear momentum has only allowed values of multiples of h/2p. [Linear momentum elektron hanya mengambil nilai-nilai diizinkan yang merupakang and aan h/2p.]
- III. The orbit of the electron becomes larger for a larger value of *n*. [Orbit elektron menjadi makin besar bila nilai n majadi makin besar.]
- IV. The electron breaks away from the hydrogen's attractive potential when *n* approaches infinity. [Elektron terputus daripada keupayaan tarikan hidrogen bilan menokok ke infiniti.]
- A. I, II
- B. III, IV
- C. II, III, IV
- D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]
- ANS: B (For I, $v_n = \frac{ke^2}{vh}$, hence I is false. Taylor et al., pg 152, 153. My own question)
- 37. Consider the Bohr's model of hydrogen-like atom. Its states are characterised by the non-zero quantum integer *n*. Which of the following statements is (are) true?

[Pertimbangkan atom bak hidrogen model Bohr. Keadaannya adalah dicirikan oleh nombor kuantum integer bukan sifar n. Yang manakah kenyataan(-kenyataan) berikut adalah benar?]

- I. The ground state energy is -13.6 eV. [Tenagabuminyaialah -13.6 eV.]
- II. The ground state energy is 13.6 eV. [Tenaga buminya ialah 13.6 eV]
- III. The ground state energy is 0. [Tenaga buminya ialah 0]
- IV. The difference in the energy level between state *n* and *n*+1 becomes infinity when $n \mathbf{a} \infty$. [*Perbezaan tenaga di antara paras n dan n*+1 *menjadi infiniti bila n* $\mathbf{a} \infty$.]
- A. I, IV
- B. III, IV
- C. II, IV
- D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: D (Only I is true.)

38. Consider Balmer's formula $\frac{1}{l} = R_{\rm H} \left(\frac{1}{n'^2} - \frac{1}{n^2} \right)$ (n > n', both integers), where $R_{\rm H}$ is the Rydberg constant. In Bohr's model, the theoretical value of $R_{\rm H}$ is given by the expression [PertimbangkanformulaBalmer $\frac{1}{l} = R_{\rm H} \left(\frac{1}{n'^2} - \frac{1}{n^2} \right)$, (n > n', kedua-duanyainteger), dengan $R_{\rm H}$ pemalar Rydberg. Dalam model Bohr, nilai teori $R_{\rm H}$ adalahdiberikan oleh]

A. 13.6 eV/(*hc*) B. $\frac{1}{4pe_0} \frac{e^2}{a_0hc}$ (*a*₀ is the Bohr's radius)

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C. me^4

 $\overline{4pe_0^2 ch^3}$

D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: A (Taylor et al, Chap 5.7, Eq. 5.26)

39. A particle in an infinite square well with length *L* is known to be in the ground state. The spatial coordinate of the particle in the infinite square well is constrained by $0 \ge x \ge L$. The probability to find the particle is highest in interval of ______.

[Diketahui suatu zarah di dalam telaga segiempat infinit berada dalam keadaan bumi. Koordinat ruangan zarah dalam telaga segiempat infinit adalah dikongkong oleh $0 \ge x \ge L$. Kebarangkalian untuk menemui zarah tersebut adalah tertinggi di dalam selang ______.]

- A. $L/2 \pm 0.001L$
- B. $L/4 \pm 0.001L$
- C. $L/8 \pm 0.001L$
- D. $L/16 \pm 0.001L$

ANS: A (my own question)

40. Which of the following statements is true?

[Yang manakah kenyataan(-kenyataan) berikutadalah benar?]

I. A quantum particle initially confined in an infinite square well cannot possibly escape from the well when excited (T)

[Suatu zarah kuantum yang pada asalnya terkongkong di dalam telaga segiempat infinit tidak mungkin terlepas daripada telaga bila diujarkan.]

- II. A quantum particle initially confined in an infinite square well can possibly escape from the well when excited (F) [Suatu zarah kuantum yang pada asalnya terkongkong di dalam telaga segiempat infinit mungkin terlepas daripada telaga bila diujarkan.]
- III. A quantum particle initially confined in an finite square well cannot possibly escape from the well when excited (F) [Suatu zarah kuantum yang pada asalnya terkongkong di dalam telaga segiempat finit tidak

mungkin terlepas daripada telaga bila diujarkan.]

IV. A quantum particle initially confined in an finite square well can possibly escape from the well when excited (T)

[Suatu zarah kuantum yang pada asalnya terkongkong di dalam telaga segiempat finit mungkin terlepas daripada telaga bila diujarkan.]

- A. II, IV
- B. II, III
- C. I, III
- D. I, IV
- ANS: D (my own question)

Section B: Structural Questions. [60 marks] [Bahagian B: Soalan-soalan Struktur]

Instruction: Answer ALL THREE (3) questions in this Section. Each question carries 20 marks. [Arahan: Jawab KESEMUA TIGA (3) soalan dalam Bahagian ini. Setiap soalan membawa 20 markah].

1. [20 marks]

Consider a completely inelastic head-on collision between two balls (with rest mass m_0 each) moving toward the other at a common velocity v with respect to a given frame S. Assuming that the resultant mass is at rest after the collision (with a value of M), find the following quantities. Express your answers in

terms of c, m_0 and g where $g = 1/\sqrt{1 - (v/c)^2}$.

[Pertimbangkan satu perlanggaran tak kenyal penuh antara dua bola (masing-masing berjisim m₀) yang bergerak mengarah ke satu sama lain dengan halaju v merujuk kepada satu rangka S. Anggapkan bahawa jisim terhasil selepasperlanggaran berkeadaan rehat (dan bernilai M) dalam rangka S, hitungkan kuantiti-kuantiti berikut. Nyatakan jawapan anda dalam sebutan-sebutan c, m₀ dan **g** dengan $\mathbf{g} = 1/\sqrt{1-(v/c)^2}$.]

- I. What is the total rest energy of the system before collision in S? Apakah jumlah tenaga rehat sistem tersebut sebelum perlanggaran dalam rangka S?] [2 marks]
- II. What is the total relativisitic energy of the system before collision in S? Apakah jumlah tenaga kerelatifan sistem tersebut sebelum perlanggaran dalam rangka S?] [2 marks]
- III. Express the resultant rest mass M in terms of c, m_0 and g. [Nyatakan jisim rehat M dalam sebutan c, m_0 dan g.]

[3 marks]

IV. What is the magnitude of the change of the kinetic energy in S? [Apakah magnitud perubahan tenaga kinetik sistem tersebut dalam rangka S?]

[3 marks]

b) Now consider the same inelastic collision process in an inertial frame S' such that one of the mass remains at rest while the other mass collides with it head-on. Let K and K' be the total kinetic energy of the system before and after the collision in frame S'. Find the following quantities. Express your answers in terms of c, m_0 , g, K and K'.

[Sekarang pertimbangkan proses perlanggaran yang sama di dalam satu rangka inersia S' yang mana salah satu daripada jisim berada pada keadaan rehat manakala yang satu lagi melanggarnya secara muka lawan muka. Biar K dan K' masing-masing mewakili tenaga kinetik sistem tersebut sebelum dan selepas perlanggaran di dalam rangka S'. Hitungkankuantiti-kuantitiberikut. Nyatakan jawapan anda dalam sebutan-sebutan c, m₀, g, K dan K'.]

- I. What is the total relativistic energy of the system, before the collision in S'? [Apakahjumlah tenaga kerelatifan sistem tersebut sebelumperlanggaran dalam rangka S'?] [2 marks]
- II. What is the total relativistic energy of the system after the collision in S'? Apakah jumlah tenaga kerelatifan sistem tersebut selepas perlanggaran dalam rangka S'?] [2 marks]
- III. What is the magnitude of the change of the kinetic energy in S[?] [Apakahmagnitud perubahan tenaga kinetik dalam rangka S[?]]

[3 marks]

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IV. Does the magnitude of the change of the kinetic energy frame-dependent? [Adakah magnitud perubahan tenaga kinetik bersandar pada rangka?]

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[3 marks]

Solution

a)

b)

- I. In frame S, total rest energy of the system before collision = $2m_0c^2$ [2 marks] II. In frame S, total relativistic energy of the system before collision = $2\gamma m_0 c^2$ [2 marks] III. Due to conservation of energy, total energy before collision = total energy after collision: $2\gamma m_0 c^2 = M c^2$. Therefore, $M = 2\gamma m_0$. [3 marks] IV. In frame S, the magnitude of change in total rest energy of the system after collision = The magnitude of change in kinetic energy of the system = $Mc^2 - 2m_0c^2 = (M - 2m_0)c^2 = 2m_0c^2(\gamma - 1)$ [3 marks] I. In frame S', total energy of the system before collision = $2m_0c^2 + K$ [2 marks] II. In frame S', total energy of the system after collision = $Mc^2 + K' = 2\gamma m_0 c^2 + K'$. [2 marks] III. Due to conservation of total energy, $2m_0c^2 + K = 2\gamma m_0 c^2 + K'$, hence the magnitude of the change of the kinetic energy of the system = $|K' - K| = |2m_0c^2 - 2\gamma m_0c^2| = 2(\gamma - 1)m_0c^2$. [3 marks] V. No. The change of the kinetic energy in both frame are the same and equals $2(\gamma - 1)m_0c^2$. [3 marks] 2. [20 marks]
 - a) A positron collides head on with an electron and both are annihilated. Each particle had a kinetic energy of 1.00 MeV. Find the wavelength of the resulting photons. Express your anwer in unit of pm. [Suatu positron berlanggar muka sama muka dengan suatu elektron, dan kedua-dua zarah memusnah-habis, Kedua-dua zarah masing-masing bertenaga kinetik 1.00 MeV. Hitungkan jarak gelombang foton yang terhasil. Nyatakan jawapan anda dalam unit pm.]

[5 marks]

b) How much energy must a photon have if it is to have the momentum of a proton with kinetic energy 10 MeV?

[Apakah tenaga suatu foton yang momentumnya samadengan momentum suatu proton yang bertenagakinetik 10 MeV?]

[5 marks]

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- What is the value of electron's Compton wavelength, λ_{e} ? Expressed your answer in terms of pm. *c*) [Apakah nilai jarak gelombang Compton bagi elektron? Nyatakan jawapan anda dalam sebutan pm.] [4 marks]
- d) Find the wavelength of an x-ray photon which can impart a maximum energy of 50 keV to an electron. [Hint: You may need to consider the corresponding recoil angle of the scattered photon for a *maximum transfer of its energy to the recoil electron.*] [Hitungkan jarak gelombang suatu foton sinaran-X yang dapat memberikan tenaga maksimum

bernilai 50 keVkepada suatu elektron.]

Solution

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(]

c)

a) Total energy of the positron + electron before annihilation = rest energies of the electron-positron pair + their kinetic energy $E = E_{+} + E_{-} = 2m_{e}c^{2} + K_{+} + K_{-} = 2m_{e}c^{2} + 2K = 2(0.51 \text{ MeV} + 1.00 \text{ MeV}) = 2(1.51 \text{ MeV})$

[Petuniuk: Anda mungkin perlu mempertimbangkan sudut sentakan foton terserak bagi perpindahan

Total energy of the photon pair after annihilation =

$$2E_{\gamma}=2\frac{hc}{l}=2\left(\frac{1240\text{eV}\cdot\text{nm}}{l}\right)=2\left(\frac{1.24\times10^{-3}\,\text{MeV}\cdot10^{-9}\,\text{m}}{l}\right)$$

tenaganya secara maksimum kepada elektron yang tersentak.]

$$I = \frac{hc}{m_e c^2 + K} = \frac{1.24 \times 10^{-3} \text{MeV} \times 10^{-9} \text{m}}{1.511 \text{ MeV}} = 0.82 \text{ pm}.$$

(Beiser Chap 2, Ex. 39, pg. 91)

[6 marks]

b) A proton with this kinetic energy is nonrelativistic, and its momentum is given by $p^2 = 2m_P K$. The energy of a photon with this momentum is

$$pc = \sqrt{2m_pc^2 K} = \sqrt{2(938 \text{ MeV})(10 \text{ MeV})} = 137 \text{ MeV}$$
 140 MeV.
Beiser Chap 2, Ex. 26, pg. 90)

[5 marks]

$$I_e = \frac{h}{m_e c} = \frac{hc}{m_e c^2} = \frac{1240 \text{ eV} \cdot \text{nm}}{0.51 \text{ MeV}} = \frac{1240 \text{ eV} \cdot \text{nm}}{0.51 \text{ MeV}} = 2.43 \text{ pm}$$
[4 marks]

d) Let the incident wavelength be λ and the scattered wavelength of the photon be λ' . A maximal change in the wavelength corresponds to maximum energy transfer to the electron. This happens when $\phi = 180^\circ$. Hence, $\Delta I_{\text{max}} = I_e \left[1 - \cos(180^\circ) \right] = 2I_e$; where I_e is the Compton wavelength of the electron. $\Rightarrow I'_{\text{max}} = \Delta I_{\text{max}} + I = 2I_e + I$. The maximal change in the photon's energy = maximal kinetic energy transferred to the electron, i.e. $K_{\max} = \frac{hc}{l} - \frac{hc}{l'_{\max}} = hc \left(\frac{l'_{\max} - l}{ll'_{\max}}\right) = hc \left(\frac{\Delta l_{\max}}{l(l + \Delta l_{\max})}\right) = hc \left(\frac{2l_e}{l(l + 2l_e)}\right).$ Rearranging, we get a quadratic equation for λ : $I(I+2I_e) = \left(\frac{2I_ehc}{K_{max}}\right) = \left(\frac{2 \times 2.43 \text{pm} \times 1240 \text{ nm} \cdot \text{eV}}{50 \text{ keV}}\right) = 120.5 \text{pm}^2$ $\Rightarrow l^2 + 2l_1 l - 120.5 \text{pm}^2 = 0$ $\Rightarrow l = \frac{-2l_e \pm \sqrt{(2l_e)^2 + 4(120.5 \text{pm}^2)}}{2} = -2.43 \text{pm} \pm \sqrt{(2.43 \text{pm})^2 + (120.5 \text{pm}^2)} = +8.81 \text{pm}$ (Beiser Chap 2, Ex. 32, pg. 90) [6 marks]

- 3. [20 marks]
 - a) How much energy is required to remove an electron in the n=2 state from a hydrogen atom? [Apakah tenaga yang diperlukan untuk membebaskan suatu elektron dalam keadaan n = 2 daripada atomhidrogen?]

[5 marks]

b) Find the quantum number that characterises the Earth's orbit around the sun. The Earth's mass is 6.0×10^{24} kg, its orbital radius is 1.5×10^{11} m, and its orbital speed is 3.0×10^{4} m/s. [Hint: Assume that the angular momentum of the Earth about the Sun is quantised in a manner similar to Bohr's hidrogen-like atom.]

[Hitungkan numbor kuantum yang mencirikan orbit Bumi mengelilingi Matahari. Diberikan jisim bumi 6.0×10^{24} kg, radius orbitnya 1.5×10^{11} m, dan laju orbitnya 3.0×10^4 m/s.] [Petunjuk: Anggap bahawa momentum sudut Bumi sekitar Matahari adalah dikuantumkan mengikut cara seperti dalam atom bak hidrogen Bohr.]

[5 marks]

c) In terms of ground state energy E₀, h and n, what is the frequency of the photon emitted by a hydrogen atom, ν, in going from the level n + 1 to the level n?
[Dalam sebutan tenaga bumi E₀, h dan n, nyatakanfrekuensifoton, n, yang dipancarkan oleh suatu atom hidrogen yang beralih dari paras n+1 ke paras n.]

[7 marks]

d) What is value of the frequency of the photon in (c) above in the limit $n \grave{a} \infty$. [*Apakah nilai frequensi bagi foton dalam* (c) *di atas dalam limit* $n \grave{a} \infty$.]

[3 marks]

Solution 3.

a) The n = 2 energy is $E_2 = E_0/2^2 = E_0/4 = -13.6 \text{ eV}/4 = -3.40 \text{ eV}$, so an energy of 3.40 eV is needed. (Beiser, Chap 4, Ex. 22, pg. 158)

[5 marks]

b) With the mass, orbital speed and orbital radius of the Earth known, the Earth's orbital angular momentum is known, and the quantum number that would characterise the Earth's orbit about the Sun would be the angular momentum divided by h

$$n = \frac{L}{\mathbf{h}} = \frac{mvr}{\mathbf{h}} = \frac{(6.0 \times 10^{24} \text{ kg})(3.0 \times 10^4 \text{ m/s})(1.5 \times 10^{11} \text{ m})}{(1.055 \times 10^{-34} \text{ J} \cdot \text{s})} = 2.6 \times 10^{74}$$

(Beiser, Chap 4, Ex. 11, pg. 158)

[5 marks]

c) The frequency v of the photon emitted in going from n+1 level to the level n is given by

$$n = \frac{E_{n+1} - E_n}{h} = \frac{1}{h} \left(\frac{E_0}{(n+1)^2} - \frac{E_0}{(n)^2} \right) = \frac{E_0}{h} \left(\frac{n^2 - (n+1)^2}{n^2 (n+1)^2} \right) = -\frac{2E_0}{h} \left(\frac{n + \frac{1}{2}}{n^2 (n+1)^2} \right)$$

(Beiser, Chap 4, Ex. 29, pg. 159)

[7 marks]

e) In the limit $n\mathbf{\dot{a}} \propto$, the frequency $\mathbf{v} \mathbf{\dot{a}} 0$

[3 marks]

UNIVERSITI SAINS MALAYSIA

Second Semester Examination Academic Session 2005/2006

Jun 2006

ZCT 104E/3 – Physics IV (Modern Physics) [Fizik IV (Fizik Moden]

Duration: 3 hours [Masa : 3 jam]

Please ensure that this examination paper contains **TWENTY EIGHT** pages before you begin the examination.

[Sila pastikan bahawa kertas peperiksaan ini mengandungi **DUA PULUH LAPAN** muka surat yang bercetak sebelum anda memulakan peperiksaan ini.]

Instruction:

Answer ALL questions in Section A and Section B.

Please answer the objective questions from Section A in the objective answer sheet provided. Please submit the objective answer sheet and the answers to the structured questions separately.

Students are allowed to answer all questions in Bahasa Malaysia or in English.

[Arahan: Jawab SEMUA soalan dalam Bahagian A dan Bahagian B.

Sila jawab soalan-soalan objektif daripada bahagian A dalam kertas jawapan objektif yang dibekalkan. Sila serahkan kertas jawapan objektif dan jawapan kepada soalan-soalan struktur berasingan.

Pelajar dibenarkan untuk menjawab samada dalam bahasa Malaysia atau bahasa Inggeris.]

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Data

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Speed of light in free space, $c = 3.00 \times 10^8 \text{ m s}^{-1}$ Permeability of free space, $\mu_0 = 4\pi \times 10^{-7} \text{ H m}^{-1}$

Permittivity of free space, $\varepsilon_0 = 8.85 \times 10^{-12} \text{ F m}^{-1}$

Unified atomic mass constant, $u = 1.66 \times 10^{-27}$ kg Rest mass of electron, $m_e = 9.11 \times 10^{-31}$ kg

Gravitational constant, $G = 6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$

Elementary charge, $e = 1.60 \times 10^{-19} \text{ C}$ Planck constant, $h = 6.63 \times 10^{-34} \text{ J s}$

Rest mass of proton, $m_{\rm p} = 1.67 \times 10^{-27} \, \rm kg$

Molar gas constant, = $8.31 \text{ J K}^{-1} \text{ mol}^{-1}$ Avogadro constant, $N_{\text{A}} = 6.02 \times 10^{23} \text{ mol}^{-1}$

Acceleration of free fall, $g = 9.81 \text{ m s}^{-2}$

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[ZCT 104E]

Section A: Objectives. [20 marks] [Bahagian A: Soalan-soalan objektif]

Instruction: Answer all 20 objective questions in this Section.

[Arahan: Jawab kesemua 20 soalan objektif dalam Bahagian ini.]

1. Which of the following statements is (are) true regarding the Bohr model of hydrogen-like atom?

[Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai model Bohr untuk atom bak-hidrogen?]

- I. It predicts the ionization energy for hydrogen. (T) [Ia meramalkan tenaga pengionan untuk hydrogen.]
- II. It cannot account for the spectra of more complex atoms. (T) [*Ia tidak dapat menerangkan spektrum atom-atom yang lebih kompleks.*]
- III. It is unable to predict many subtle spectral details of hydrogen and other simple atoms such as energy level splittings due to spin-orbital interactions. (T) [*Ia gagal untuk meramalkan banyak butir-butir halus hidrogen dan atom-atom ringkas lain seperti belahan paras-paras tenaga disebabkan oleh interaksi spin-orbit.*]
- IV. The notion of electrons in well-defined orbits around the nucleus is consistent with the uncertainty principle. (F) [Fikiran bahawa elektron mengelilingi nukleus dalam orbit yang tepat tertakrif adalah konsisten dengan prinsip ketidakpastian.]

A. I, II, III B. II, IIV C. I, II, III, IV D.(None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: A. Serway pg. 1359, modified.

2. Which of the following statements is (are) true regarding the spectrum of hydrogen atom, according to the Bohr model?

[Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai spektrum atom hidrogen menurut model Bohr?]

- I. The Balmer series emission spectrum of a hydrogen atom lies in the visible region of the electronmagnetic spectrum. [Spektrum pancaran siri Balmer atom hidrogen terletak dalam rantau nampak spektrum elektromagnetik.]
- II. The Lyman series emission spectrum of a hydrogen atom lies in the ultraviolet region of the electronmagnetic spectrum. [Spektrum pancaran siri Lyman atom hidrogen terletak dalam rantau ultraungu spektrum elektromagnetik.]

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III. The Paschen series emission spectrum of a hydrogen atom lies in the infrared region of the electronmagnetic spectrum. [Spektrum pancaran siri Paschen atom hidrogen terletak dalam rantau infra merah spektrum elektromagnetik.]

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IV. The Balmer series absorption spectrum of a hydrogen atom lies in the visible region of the electronmagnetic spectrum. [Spektrum serapan siri Balmer atom hidrogen terletak dalam rantau nampak spektrum elektromagnetik.]

A. I, II, III, IV B. I, II, III C. II, IV D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] ANS: A (ALL)

3 Which of the following statements is (are) true regarding the wave function of a quantum particle?

[Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai fungsi gelombang bagi suatu zarah kuantum?]

- I. The wavefunction is directly measurable. [Fungsi gelombang dapat diukur secara terus.]
- II. The square of the wavefunction is a measure of the probability of observing the quantum particle within a region in space. *[Kuasadua fungsi gelombang merupakan satu sukatan kebarangkalian untuk memerhatikan zarah kuantum di dalam suatu rantau ruangan.]*
- III. The square of the wavefunction is a measure of the energy of the quantum particle. [Kuasadua fungsi gelombang merupakan satu sukatan untuk tenaga zarah kuantum.]
- IV. The wavefunction of a free particle is zero everywhere. [Fungsi gelombang suatu zerah bebas adalah sifar di mana-mana.]

A. I, III B. II, IV C. I ONLY D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

ANS: D, II only. [My own question.]

- 4. Which of the following statements is (are) true regarding the linear momentum of an object? [Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai momentum linear agi suatu objek?]
 - I. The object's momentum is dependent on its speed. [Momentum objek bersandar kepada lajunya.]
 - II. The object's momentum is dependent on the frame in which it is being measured. [Momentum objek bersandar kepada rangka dalam mana ia diukur.]

- III. In special theory of relativity, there is an upper limit to the magnitude of an object's linear momentum.
 [Dalam teori kerelatifan wujudnya limit atas ke atas magnitud momentum linear suatu objek.]

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IV. In non-relativistic theory of classical mechanics, there is no upper limit to the magnitude of its linear momentum. [Dalam teori mekanik klasik bukan kerelatifan tidak wuiud limit atas ke atas magnitud

[Dalam teori mekanik klasik bukan kerelatijan tidak wujud limit atas ke atas magnitud momentum linear suatu objek.]

A. I, III B. I, II, IV C. I ONLY D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] ANS: B [My own question.]

- 5. Which of the following statements is (are) true regarding the kinetic energy of an object? [Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai tenaga kinetik suatu objek?]
 - I. The kinetic energy of an object is the energy associated with the motion of the object. [Tenaga kinetik suatu objek adalah tenaga yang berkaitan dengan pergerakan objek.]
 - II. In special theory of relativity, the kinetic energy of an object cannot be larger than its rest energy.
 [Dalam teori kerelatifan, tenaga kinetik suatu objek tidak boleh melebihi tenaga

rehatnya.]

- III. The relativistic expression of kinetic energy reduces to that of the classical theory of machanics in the limit $v \ll c$. [Ungkapan tenaga kinetik keretatifan terturun kepada ungkapan mekanik teori klasik dalam limit $v \ll c$.]
- IV. The classical expression of kinetic energy reduces to that of the special theory of relativity in the limit $v \ll c$. [Ungkapan tenaga kinetik klasik terturun kepada ungkapan kerelatifan dalam limit $v \ll c$.]

A. I, II, III B. I, II, IV C. I, III D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] ANS: C [My own question.]

6. Consider a proton and an electron, both moving at a common speed, v. Let K_p and K_e denote the the proton and electron's kinetic energy respectively. Which of the following statements is (are)?

[Pertimbangkan suatu proton dan suatu elektron, kedua-duanya bergerak dengan laju yang sama, v. Biar K_p dan K_e masing-masing menandakan tenaga kinetik proton dan elektron. Yang manakah kenyataan(-kenyataan) berikut adalah benar?]

- I. $K_{\rm p} = (m_{\rm p}/m_{\rm e})K_{\rm e}$ for v << c. $[K_{\rm p} = (m_{\rm p}/m_{\rm e})K_{\rm e}$ untuk v << c.]
- II. $K_p = (m_p/m_e)K_e$ for v close to c. $[K_p = (m_p/m_e)K_e$ untuk v mendekati c.]

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- III. $K_p > K_e$ for all values of v < c. $[K_p > K_e$ untuk semua nilai v < c.]
- IV. The ratio of K_p/K_e depends on the magnitude of v. [nisbah K_p/K_e bergantung kepada magnitud v.]

A. I, II, III B. IV only C. II, III D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] **ANS: A [IV is false. My own question.]** $\frac{\gamma m_p c^2}{\gamma m_e c^2} = \frac{K_p + m_p c^2}{K_e + m_e c^2} \Rightarrow \frac{K_p}{K_e} = \frac{m_p}{m_e}$

7. Let say you have found a map revealing a huge galactic treasure at the opposite edge of the Galaxy 200 ly away. Is there any chance, from the relativistic point of view, for you to travel such a distance from Earth and arrive at the treasure site by traveling on a rocket within your lifetime of say, 60 years?

[Katakan anda telah menjumpai satu peta yang membongkar harta karun galaktik sejauh 200 tahun cahaya di sebelah sisi Galaksi yang bertentangan. Dari segi teori kerelatifan, adakah wujud apa-apa peluang supaya anda dapat menjelajahi jarak tersebut dari Bumi dengan menaiki roket dan sampai ke tempat harta karun dalam masa hayat anda, katakan 60 tahun?]

- A. No, it is impossible to reach the treasure site within our lifespan of 60 years because it takes a minimum of 200 year of traveling time to reach there.
 [Tidak. Adala tidak mungkin untuk sampai ke tempat harta karun dalam masa hayat 60 tahun kerana tempoh penjelajahan untuk sampai ke sana adalah sekurang-kurangnya 200 tahun.]
- B. No, it is impossible to reach the treasure site within our lifespan of 60 years because we can't travel faster than the speed of light.
 [Tidak. Adala tidak mungkin untuk sampai ke tempat harta karun dalam masa hayat 60 tahun kerana kita tidap mungkin bergerak lebih pantas daripada laju cahaya.]
- C. Yes, it is possible to reach the treasure site within our lifespan of 60 years because theory of relativity allows the rocket to travel faster than the speed of light. [Ya. Adala mungkin untuk sampai ke tempat harta karun dalam masa hayat 60 tahun kerana teori kerelatifan membenarkan roket bergerak lebih pantas daripada laju cahaya.]
- D. Yes, it is possible to reach the treasure site within our lifespan of 60 years because the traveling time to reach there could be significantly smaller than 200 years due to relativistic effect.

[Ya. Adala mungkin untuk sampai ke tempat harta karun dalam masa hayat 60 tahun kerana tempoh penjelajahan untuk sampai ke sana boleh jadi jauh lebih singkat daripada 200 tahun disebabkan oleh kesan kerelatifan.]

ANS: D [My own question, pg. 1 in lecture note]

- 8. Which of the following statements is (are) true according to the special theory of relativity? [Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai teori kerelatifan?]
 - I. A massless particle must always travel at the speed of light. [Suatu zarah tanpa jisim mesti sentiasa bergerak dengan laju cahaya.]

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 II. A particle with non-zero mass must always travel at the speed smaller than that of light.
 [Suatu zarah dengan jisim bukan sifar mesti sentiasa bergerak dengan laju yang

[Suatu zarah dengan jisim bukan sifar mesti sentiasa bergerak dengan laju yang kurang daripada laju cahaya.]

- III. The length of a moving object along its direction of motion is shorter than that measured at rest. [Panjang suatu objek dalam arah gerakannya adalah lebih pendek daripada panjangnya yang diukur semasa ia rehat.]
- IV. The rest mass of an object is greater when it is moving than at rest. [Jisim rehat bagi suatu objek adalah lebih besar semasa ia bergerak berbanding dengan jisim rehatnya semasa ia rehat .]

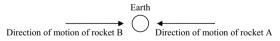
A. I, III, IV B. I, II, IV C. I, II, III D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] ANS: C [My own question.]

- 9. When two particles collide relativistically, [Bila dua zarah berlanggar secara kerelatifan,]
 - I. the total rest energy is conserved. [jumlah tenaga rehat adalah terabadikan.]
 - II. the total rest mass is conserved. [jumlah jisim rehat adalah terabadikan.]
 - III. the total kinetic energy is an invariant. [jumlah tenaga kinetik adalah tak varian.]

A. I, II, III B. II, III C. I, II D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] ANS: D. None of I, II, III is true.

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10. Consider two rockets moving in opposit directions towards the Earth. See figure below. Rocket A is moving towards Earth at a speed of 0.5*c* (relative to Earth) while rocket B with a speed of 0.51*c* (relative to Earth). Which of the following statements is (are) true? [Pertimbangkan dua roket yang bergerak dalam dua arah bertentangan, masing-masing menghadap ke Bumi. Rujuk gambarajah. Roket A bergerak menuju ke arah Bumi dengan laju 0.5*c* (relatif kepada Bumi) manakala roket B dengan laju 0.51*c* (relatif kepada Bumi). Yang manakah kenyataan(-kenyataan) berikut adalah benar?]



I. The magnitude of the relative velocity of rocket A with respect to rocket B is less than 1.01 c.

[Magnitud halaju relatif roket A merujuk kepada roket B adalah kurang daripada 1.01c.]

- II. The magnitude of the relative velocity of rocket A with respect to rocket B is less than c. [Magnitud halaju relatif roket A merujuk kepada roket B adalah kurang daripada c.]
- III. The magnitude of the relative velocity of rocket A with respect to rocket B is equal to c.

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[Magnitud halaju relatif roket A merujuk kepada roket B adalah sama dengan c.]

IV. The magnitude of the relative velocity of rocket A with respect to rocket B is equal to 1.01 c.

[Magnitud halaju relatif roket A merujuk kepada roket B adalah sama dengan 1.01c.]

- A. I, II B. I, III C. IV only D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] ANS: A [PYQ, 05/06 Final, Q15, modified]
- 11. For a blackbody, the total intensity of energy radiated over all wavelengths, *I*, is expected to rise with temperature according to the *Stefan's law*: $I = \sigma T^*$, where σ is the Stefan's constant. How does the total intensity of thermal radiation vary when the temperature of a black body is doubled?

[Bagi suatu jasad hitam, jumlah keamatan tenaga terpancarkan untuk semua jarak gelombang, I, dijangka akan meningkat jika suhu meningkat, menurut hukum Stefan, $I = \sigma T^4$, di mana σ adalah pemalar Stefan. Bagaimanakah jumlah keamatan pancaran terma berubah bila suhu jasad hitam menjadi dua kali lebih besar?]

- A. The total intensity of thermal radiation increase by 2 times. [Jumlah keamatan pancaran terma bertambah sebanyak 2 kali.]
- B. The total intensity of thermal radiation increase by 4 times. [Jumlah keamatan pancaran terma bertambah sebanyak 4 kali.]
- C. The total intensity of thermal radiation increase by 16 times [Jumlah keamatan pancaran terma bertambah sebanyak 16 kali.]
- D. The total intensity of thermal radiation remains the same. [Jumlah keamatan pancaran terma adalah sama.]

ANS:C, Tut 2 04/05, P1

12. In the spectral distribution of blackbody radiation, the wavelength λ_{max} at which the intensity reaches its maximum value decreases as the temperature is increased, in inverse proportional to the temperature: $\lambda_{max} \propto 1/T$. This is called the *Wein's displacement law*. It explains the observation that when a blackbody is heated up to 1800K it starts to glow and appears dim red. According to Wein's law, when the temperature continue to increase, the colour would change from dim red towards blue and then white hot. What is the change of the apparent colour to human eye when temperature drops from 450K to 370 K?

[Dalam taburan spektrum pancaran jasad hitam, jarak minimum λ_{max} pada mana keamatan mencapai nilai maksimumnya akan berkurang bila suhu dinaikkan mengikut $\lambda_{max} \propto 1/T$. Ini

dipanggil hukum sesaran Wein. Ia menerangkan cerapan bahawa semasa suatu jasad hitam dipanaskan kepada 1800K, ia mula berbara dan kelihatan merah pudar. Menurut hukum Wein, jika suhu terus meningkat, warnanya akan berubah daripada merah pudar kepada biru dan kemudiannya panas putih. Apakah perubahan warna ketara kepada mata manusia bila suhu jatuh daripada 450K kepada 370 K?]

- A. It changes from red hot to blue hot. [Ia berubah daripada merah panas kepada biru panas.]
- B. It changes from red hot to dark. [Ia berubah daripada merah panas kepada hitam.]
- C. Its apparent colour doesn't change. [Warna ketaranya tidak berubah.]

[ZCT 104E]

[ZCT 104E]

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D. It changes from white hot to red hot. [Ia berubah daripada putih panas kepada merah panas.]

ANS:C, http://library.wolfram.com/webMathematica/Astronomy/Blackbody.jsp

- (BB at temperature lower than 1800 K doesn't appear to have any 'colour' to our human eye.)
- 13. Which of the following statements is (are) true regarding X-rays? [Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai sinaran-X?]
 - I. X-ray can be used to determine the geometry of the lattice of a crystal. (T) [Sinaran-X boleh digunakan untuk menentukan geometri kekisi sesuatu hablur.]
 - II. X-rays can be produced by bombarding a metal target with electrons accelerated by an electric potential field of 10,000 V. (T) [Sinaran-X boleh dihasilkan dengan menghentam suatu sasaran logam dengan elektron yang dipecutkan oleh suatu medan keupayaan elektrik 10,000 V.]

III. Tungsten and molybdenum, two types of material usually used as target material in an Xrays tube, give off different λ_{min} of X-rays when the X-ray tube is operating at a common potential V. (F) [Tungsten dan molibdenum, dua jenis bahan yang biasanya digunakan sebagai bahan

sasaran dalam tiub sinaran-X, mengeluarkan λ_{min} sinaran-X yang berbeza semasa tiub sinaran-X beroperasi pada keupayaan yang sama.]

IV. X-rays behave like wave in Braggs diffraction of X-ray by a crystal lattice. (T) [Sinaran-X berkelakuan seperti gelombang dalam belauan sinaran-X Braggs oleh kekisi bablur.]

A. I, II, III, IV B. I, II, III C. I, II, IV D. None of A, B, C. **ANS: C.** (My Own Question)

- 14. Which of the following statements is (are) true regarding light? [Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai cahaya?]
 - I. Light behaves like wave in a diffraction experiment. (T) [Cahaya berkelakuan seperti gelombang dalam eksperimen belauan.]
 - II. Light behaves like particle in a photoelectric experiment. (T) [Cahaya berkelakuan seperti zarah dalam eksperimen fotoelektrik.]
 - III. Light behaves like particle in a Compton scattering experiment. (T) [Cahaya berkelakuan seperti zarah dalam eksperimen serakan Compton.]
 - IV. Light can manifest both particle and wave nature in a single experiment. (F) [Cahaya boleh memperlihatkan kedua-dua tabii zarah dan gelombang dalam satu eksperimen yang sama.]

- 10 -A. I, II, III B. II, III, IV C. I, III, IV D. None of A,B, C. ANS: A. (My Own Question)

- 15. Which of the following statements is (are) true regarding photoelectric effect? [Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai kesan fotoelektrik?]
 - I. The photoelectric effect requires special theory of relativity for an explaination. *[Kesan fotoelektrik memerlukan teori kerelatifan untuk penerangannya.]*
 - II. In a typical photoelectric effect experiment the energy involved is usually relativistic. [Dalam suatu eksperimen kesan fotoelektrik yang tipikal, tenaga yang terlibat biasanya adalah relativistik.]
 - III. The probability of photoelectric effect to occur in a metal target would diminish when the energy of the striking photon becomes increasingly relativistic. [Kebarangkalian kesan fotoelektrik berlaku di dalam sararan logam akan menyusut bila tenaga foton yang menghentum menjadi semakin relativistik.]
 - IV. The saturation photoelectric current increases as the energy of incident photons increases (with the radiation fixed at a constant intensity). [Arus fotoelektrik tepu bertambah semasa tenaga foton tuju bertambah (dengan sinaran ditetapkan pada keamatan malar).]

A. I, II, III, IV B. I, II, III C. I, II, IV D. None of A, B, C. ANS: D. Only III is true.

.../12 -

16. Consider a matter particle with rest mass m_0 , moving with a speed ν . Which of the following statements is (are) true regarding its de Broglie wave? Take $\gamma = \frac{1}{\sqrt{1-(\nu/r)^2}}$.

[Pertimbangkan suatu zarah jirim berjisim rehat m_0 , bergerak dengan laju v. Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai gelombang de Broglienya? Ambil $\gamma = \sqrt[Y]{|I-(y/c)|^2}$.]

- I. The de Broglie wavelength of the matter particle is $\lambda = h/(\gamma m_0 v)$ regardless of whether the particle is relativistic or not (T). [Jarak gelombang de Broglie zarah jirim ialah $\lambda = h/(\gamma m_0 v)$, tidak kira samada zarah tersebut adalah dalam keadaan kerelatifan atau tidak].
- II. The de Broglie wavelength of the matter particle is $\lambda = h/(\gamma m_0 v)$ even if v is non relativistic (T). [Jarak gelombang de Broglie zarah jirim ialah $\lambda = h/(\gamma m_0 v)$ walaupun zarah tersebut adalah dalam keadaan bukan kerelatifan.]
- III. The de Broglie wavelength of the matter particle is $\lambda = h/(m_0 v)$ if v is non-relativistic (T).

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[Jarak gelombang de Broglie zarah jirim ialah $\lambda = h/(m_0 v)$ jika zarah tersebut adalah dalam keadaan bukan kerelatifan.]

IV. If the matter particle is relativistic, the de Broglie wavelength is larger than $h/(\gamma m_0 v)$. (F) [Jika zarah jirim adalah dalam keadaan kerelatifan, jarak gelombang de Broglie zarah adalah lebih besar daripada $\lambda = h/(\gamma m_0 v)$.]

A. I, II, III B. II, III C. II, III, IV D. None of A, B, C. ANS: A. (My Own Question, modified from PYQ 05/06 Test II, Q14) For both cases of relativistic and non-relativistic, their dB wavelengths are correctly given by $\lambda = h/(\gamma m_0 v)$.

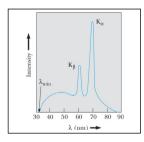
- 11 -

- 17. Which of the following statements are (is) true [Yang manakah kenyataan(-kenyataan) berikut adalah benar?]
 - I. $hc \approx 1240 \text{ keV} \cdot \text{nm}$ (Planck constant × speed of light)
 - II. $m_e \approx 511 \text{keV} / c^2 \text{ (electron's mass)}$
 - III. $\gamma = 1/\sqrt{1 \left(\frac{v}{c}\right)^2} \approx 1$ for the typical speed v of a car on the PLUS highway.
 - IV. $a_0 \approx 0.53$ pm (Bohr's radius)

A. I, II, IV B. II, III C. I, II, III, IV D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] ANS: B. PYQ 05/06 Final, Q21, modified.

18. The figure below shows the x-ray spectrum of a metal target from a x-ray tube. Which of the following statements are (is) true? [Gambarajah berikut memaparkan spektrum sinaran-X daripada sasaran logam suatu tiub]

[Gambarajan berikut memaparkan spektrum sinaran-A daripada sasaran logam suatu tiub sinaran-X. Yang manakah kenyataan(-kenyataan) berikut adalah benar?]



I. The broad continuous spectrum cannot be explained by classical electromagnetic theory. [Spektrum selanjar yang lebar tidak dapat diterangkan oleh teori elektromagnet klasik.]

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- II. The existence of λ_{\min} in the spectrum can well be explained in terms of classical theories. [Kewujudan λ_{\min} dalam spektrum dapat diterangkan dengan baiknya oleh teori-teori klasik.]
- III. λ_{\min} is dependent on the energy of the borbarding electrons. [λ_{\min} adalah bersandar pada tenaga elektron yang menghentum sasaran logam.]

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IV. The broad continuous spectrum demonstrates a proof for the photon theory for X-rays. [Spektrum selanjar yang lebar memperlihatkan bukti kepada teori foton untuk sinaran-X.]

A. I, III, IV B. I, II, III, IV C. III Only D. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] ANS: C. PYQ 05/06 Final, Q27, modified.

- 19. Which of the following statements are (is) true regarding a quantum particle in an (ideal) infinite squre well? [Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai zarah kuantum di dalam telaga segiempat infinit (yang ideal)?]
 - I. The rest energy of the particle is equal to the zero point energy. [Tenaga rehat zarah adalah sama dengan tenaga titik sifar.]
 - II. The zero point energy tends to zero if the width of the well increase indefinitely. [Tenaga titik sifar menokok kepada sifar jika lebar telaga bertambah tak terhingga.]
 - III. On theory, the largest allowed energy level of the particle in the well is infinity. [Secara teori, paras tenaga terizinkan yang tertinggi bagi zarah dalam telaga ialah infiniti.]
 - IV. The zero point energy tends to zero if the temperature of the particles tends to absolute zero. [Tenaga titik sifar menokok kepada sifar jika suhu zarah menokok kepada sifar.]

A. II, III	B. II, III, IV	C. I, II, III
D. (None of A, B, C) $[J]$	lawapan tidak terdapat dalam piliha	n-pilihan A, B, C]
ANN: A [My own question]		

20. Consider a photon of wavelength λ undergoes pair creation process into a pair of particlesantiparticles, each with rest mass *m*. If one of the particles is measured to have kinetic energy of K_1 , what is the kinetic energy of the other particle?

[Pertimbangkan suatu foton dengan jarak gelombang λ yang melakukan penghasilan berpasangan kepada suatu pasangan zarah-antizarah, dengan jisim rehat mereka m. Jika tenaga kinetik salah satu zarah diukur sebagai K_1 , apakah tenaga kinetik bagi zarah yang satu lagi?]

A.
$$\frac{hc}{\lambda} - K_1 - 2mc^2$$
 B. $\frac{hc}{\lambda} + K_1 + 2mc^2$ C. $\frac{hc}{\lambda} + K_1 - 2mc^2$

D. $\frac{hc}{\lambda} - K_1 + 2mc^2$ ANS: A. [My own question]

Section B: Structural Questions. [80 marks] [Bahagian B: Soalan-soalan Struktur]

Instruction: Answer ALL FOUR (4) questions in this Section. Each question carries 20 marks. [Arahan: Jawab KESEMUA EMPAT (4) soalan dalam Bahagian ini. Setiap soalan membawa 20 markah].

1. [20 marks]

(a) Derive the theoretical Rydberg constant in the Bohr model. Show that it is given by: [Terbitkan pemalar Rydberg secara teori dalam model Bohr. Tunjukkan bawaha ia diberikan oleh:]

$$R_{\infty} = \frac{2\pi^2 \left(ke^2\right)^2 \left(m_e c^2\right)}{\left(hc\right)^3}, \text{ where } k = \frac{1}{4\pi\varepsilon_0}.$$

(b) Determine, in Angstroms [Hitungkan, dalam unit Angstroms]

- (i) the shortest and, [jarak gelombang yang terpendek, dan]
- the longest wavelengths of the Lyman series of hydrogen.
 [jarak gelombang yang terpanjang untuk hidrogen dalam siri Lyman.]

Solution

(a) Schaum series Modern Physics, pg. 104, 105

Mechanical stability:

$$\frac{ke^2}{r^2} = \frac{mv^2}{r} \Longrightarrow kv^2 = (mvr)v \qquad \text{Eq(1)}$$

Quantization of orbital momentum:

$L = pr = (mv)r = n\hbar$	Eq(2)
$Eq(2) \rightarrow Eq(1)$:	
$ke^2 = n\hbar \Rightarrow v = \frac{ke^2}{\hbar}$	Eq. (3)

$$\begin{array}{l} n\hbar \\ \text{Eq(3)} \rightarrow \text{Eq(2):} \\ r = \frac{n\hbar}{m\nu} = \frac{n\hbar}{m}\frac{n\hbar}{ke^2} = \frac{n^2\hbar^2}{mke^2} \\ \text{Eq. (4)} \end{array}$$

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[10/20]

[5/20]

[5/20]

Total energy:

2.

$$E = K + V = \frac{mv^2}{2} - \frac{ke^2}{r} \qquad Eq. (5)$$

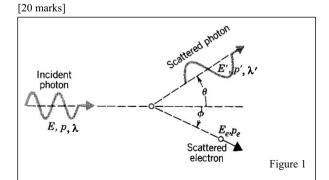
$$Eq.(3), Eq(4) \rightarrow Eq(5);$$

$$E = \frac{m}{2} \left(\frac{ke^2}{n\hbar}\right)^2 - m \left(\frac{ke^2}{n\hbar}\right)^2 = -\frac{m}{2} \left(\frac{ke^2}{n\hbar}\right)^2 = \frac{E_0}{n^2};$$
where ground state energy is $E_0 = -\frac{m}{2} \left(\frac{ke^2}{\hbar}\right)^2$.
Energy of photon during transition from n_i to n_i is
$$\frac{hc}{\lambda} = \Delta E = E_i - E_f = \frac{E_0}{n_i^2} - \frac{E_0}{n_f^2} = -E_0 \left(\frac{1}{n_f^2} - \frac{1}{n_i^2}\right)$$

$$\Rightarrow \frac{1}{\lambda} = -\frac{E_0}{hc} \left(\frac{1}{n_f^2} - \frac{1}{n_i^2}\right) = R_* \left(\frac{1}{n_f^2} - \frac{1}{n_i^2}\right)$$
(b) Schaum series Modern Physics, pg. 107, Q11.1.
In Lyman series, emission wavelengths are given by
$$\Rightarrow \frac{1}{\lambda} = -\frac{E_0}{hc} \left(\frac{1}{1^2} - \frac{1}{n_i^2}\right) = \frac{13.6eV}{1240eV \cdot nm} \left(1 - \frac{1}{n_i^2}\right)$$
(i) For shortest wavelength, $n = \infty$.

$$\frac{1}{\lambda_{shortest}} = \frac{13.6eV}{1240eV \cdot nm} \left(1 - \frac{1}{2}\right) = \left(\frac{3}{4}\right) \frac{13.6eV}{1240eV \cdot nm} \Rightarrow \lambda_{shortest} = \left(\frac{4}{3}\right) \frac{1240eV \cdot nm}{13.6eV} = 121.6nm$$

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- 15 -

(a) Consider figure 1. A photon with initial energy *E*, momentum *p* and wavelength λ is scattered by an initially stationary electron of rest mass m_e . The scattered angle, energy, momentum and wavelength of the scattered photon are as indicated in the figure. So are the energy and momentum of the recoiled electron.

[Pertimbangkan rajah 1. Suatu foton dengan tenaga awal E, momentum p dan jarak gelombang λ , diserakkan oleh suatu elektron (berjisim rehat m_e) yang pada awalnya dalam keadaan rehat. Sudut serakan, tenaga, mementum dan jarak gelombang foton yang terserak adalah seperti yang ditunjukkan di dalam rajah. Begitu juga bagi tenaga, sudut dan momentum elektron yang tersentak.]

(i) Write down the conservation of momentum for the above process. [Tuliskan keabadian momentum untuk pross tersebut.]

[4/20]

[ZCT 104E]

(ii) Write down the conservation of energy for the above process. [Tuliskan keabadian tenaga untuk proses tersebut.]

[6/20]

- **(b)** X-rays of wavelength $\lambda_0 = 0.200\ 000$ nm are Compton scattered from a block of material. [Sinaran-X dengan jarak gelombang $\lambda_0 = 0.200\ 000$ nm diserakkan secara Compton daripada suatu blok jirim.]
 - (i) If the scattered x-rays are observed at an angle of 45° to the incident beam, what is the Compton shift?

[Jika sinaran-X yang terserak dicerap pada sudut 45° kepada sinaran tuju, apakah anjakan Comptonnya?]

[5/20]

(ii) What is the Compton shift of the x-rays photon if x-rays of wavelength 0.520 000 nm is used instead?
 [Apakah anjakan Compton foton jika sinaran-X berjarak gelombang λ₀=0.520 000 nm digunakan?]

[2½/20]

 $[2\frac{1}{2}/20]$

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(iii) If the detector is moved so that the scattered x-rays are detected at a larger angle of say, 60° . Does the wavelength of the scattered x-rays increase or decrease as the angle increases?

[Jika pengesan digerakkan supaya sinaran-X terserak dikesan pada suatu sudut yang lebih besar, katakan 60°. Adakah jarak gelombang terserak akan bertambah atau berkurang?]

ANS:

(a) Lecture note page 55.

(I) Mom conservation in y: $p'\sin\theta = p_{\rho}\sin\phi$

Mom conservation in $x: p - p' \cos\theta = p_{\rho} \cos\phi$

(II) Conservation of total relativistic energy:

$$cp + m_{\rho}c^2 = cp' + E_{\rho}$$

(b) Serway, pg. 1300, example 40.4

(I) $\Delta \lambda = \frac{h}{m_{c}c} (1 - \cos 45^\circ) = 7.10 \times 10^{-13} \,\mathrm{m}.$

(II) same., 7.10×10^{-13} m. (III) scattered wavelength increases.

3. [20 marks]

(a) A proton or a neutron can sometimes "violate" conservation of energy emitting and then reabsorbing a pi meson, which has a mass of 135 MeV/c². This is possible as long as the pi meson is reabsorbed within a short enough time Δt consistent with the uncertainty principle. Consider p→ p + π.

[Suatu proton atau neutron kadang-kala akan 'mencanggah' keabadian tenaga dengan memancar dan kemudiannya menyerap balik suatu meson pi yang berjisim 135 MeV/c². Ini adalah mungkin selagi meson pi tersebut diserap balik dalam suatu selang masa singkat Δt yang konsisten dengan prinsip ketidakpastian. Pertimbangkan p \rightarrow p + π .]

(i) By what amount ΔE is energy conservation violated? (Ignore any kinetic energies.)

[Seberapa bankyakah ketidakpastian tenaga ΔE yang telah mencanggahi keabadian tenaga? (Abaikan tenaga kinetik.)]

[4/20]

(ii) For how long a time Δt can the pi meson exist?

[Untuk berapa lamakah \Delta t yang boleh meson pi wujud?]

(iii) Assuming pi meson to travel at very nearly the speed of light, how far from the proton can it go?

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[Andaikan meson pi itu bergerak pada laju yang amat menyamai laju cahaya, berapa jauhkah daripada proton itu yang dapat pi meson pergi?]

[2/20]

(b) By treating it non-relativistically, find the de Broglie wavelength of a proton with kinetic energy 1.00-MeV.

[Dengan pertimbangan secara tak-relativistik, hitungkan jarak de Broglie suatu proton yang tenaga kinetiknya 1.00-MeV.]

[10/20]

Solution

(a) (Krane, P22, pg. 133)

- $\Delta E = m_{\pi}c^2 = 135 \,\mathrm{MeV} = 2.16 \times 10^{-9} \,\mathrm{J}.$ (i)
- $\Delta t \ge \frac{\hbar}{2\Lambda E} = 2.40 \times 10^{-24} \,\mathrm{s}.$ (ii)
- distance = $c \Delta t \le 0.73 \times 10^{-15}$ m. (iii)

(b) (Beiser, Ex. 6, pg. 117)

3-6: The proton's kinetic energy is only about 0.1% of its rest energy, so a nonrelativistic calculation will suffice. The wavelength is

$$\begin{split} \lambda &= \frac{h}{p} = \frac{h}{\sqrt{2\,m\,\text{KE}}} = \frac{hc}{\sqrt{2\,(mc^2)\,\text{KE}}} \\ &= \frac{1.240 \times 10^{-12}\,\text{MeV}\cdot\text{m}}{\sqrt{2\,(939.3\,\text{MeV})\,(1.00\,\text{MeV})}} = 2.86 \times 10^{-14}\,\text{m} \end{split}$$

Note the conversion of units in the product hc in the above calculation.

4. [20 marks]

- (a) Consider a relativistic object of momentum, p, total energy, E, and rest mass, m_0 . [Pertimbangkan suatu objek relativistik dengan momentum p, jumlah tenaga E, dan *jisim rehatnya* m_0 .]
 - (i) Write down the equation relating the magnitude of relativistic momentum, total energy, and the rest mass this object. [Tuliskan persamaan yang menghubung-kaitkan magnitud momentum relativistik, jumlah tenaga dan jisim rehat objek tersebut.]

[3/20]

(ii) Sketch the graf of E vs. p. Lable and indicate on your graph the value of rest energy E_0 .

[Lakarkan graf E lawn p. Lable dan tunjukkan pada lakaran anda nilai tenaga rehat, $E_{0.}$]

[ZCT 104E]

[3/20]

(iii) What is the momentum of the object when the momentum is such that pc equal to half of the object's total energy? Express your answer in terms of m_0 and c. [Apakah momentum objek tersebut jika momentumnya adalah sedemikian rupa sehingga pc bersamaan dengan separuh daripada jumlah tenaga objek tersebut? Ungkapkan jawapan anda dalam sebutan mo dan c.1 [3/20]

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What is the corresponding speed, v in (iii)? (iv) [Apakah laju yang berkaitan dalam (iii)?] [5/20]

(b)

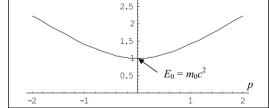
A meter stick moves with a velocity of 0.6c relative to you along the direction of (i) its length. How long will it take for the meter stick to pass you? [Suatu pembaris meter bergerak dalam arah panjang pembaris tersebut pada halaju 0.6c relatif kepada anda. Berapa lamakah masa yang diambil pembaris meter itu untuk melepasi anda?]

[6/20]

Ans: (a) My own question.

(i)

$E^2 = m_0^2 c^4 + p^2 c^2$ Ε (ii) 4 r 3.5 2.5 1.5



(iii)

 $E^{2} = m_{0}^{2}c^{4} + p^{2}c^{2}$ $(2pc)^2 = m_0^2 c^4 + p^2 c^2$ $3p^2c^2 = m_0^2c^4$ $p = m_0 c / \sqrt{3}$

(iv)

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 $p = \gamma m_0 v$ $p^2 = \gamma^2 v^2 m_0^2$ $\frac{m_0^2 c^2}{3} = \frac{v^2 m_0^2}{1 - (v/c)^2}$ v = c/2.

(b) Schaum's series Modern Physics, pg. 27, Q6.1. The length of the meter stick as measured by you is improper length, given by $L = L_0 \sqrt{1 - (v/c)^2} = (1m) \sqrt{1 - (0.6)^2} = 0.8m$ The time for the meter stick to pass you is then found from Distance = velocity × time $0.8 m = 0.6c \times \Delta t$ $\Delta t = 4.44 \times 10^{-9} s.$

- 000 O 000 -

ZCT 104/3E Modern Physics Semester II, Sessi 2006/07 Open Book Quiz I (22 Dec 2007) Duration: 30 min

Name:

Matrics No:

INSTRUCTION: Answer both following questions. Note that question 2 is printed at the opposite page. Each question carries 10 marks.

1. Derive time dilation effect $\Delta \tau = \Delta t / \gamma$ by using the Lorentz transformation formula, where $\Delta \tau$ is the

proper time interval, Δt the improper time interval, and γ is the Lorentz factor, $\gamma = -$

ANS

Lorentz transformation: $x' = \gamma(x - vt), t' = \gamma\left(t - \frac{v}{c^2}x\right).$

Say two events are happening at the same point one after another in the primed frame, which is moving with a constant velocity v with respect to an unprimed frame. The proper time between these two events is $\Delta \tau = t'_2 - t'_1$. By definition, these two events are happening in the same point in the primed frame, hence $x'_2 - x'_1 = 0$.

The temporal interval of these two events as observed in the unprimed frame, $\Delta t = t_2 - t_1$, according to LT, could be related to $\Delta \tau = t'_2 - t'_1$ via LT as

 $\Delta \tau = t_2' - t_1' = \gamma \left(t_2 - \frac{v}{c^2} x_2 \right) - \gamma \left(t_1 - \frac{v}{c^2} x_1 \right) = \gamma \left(t_2 - t_1 \right) - \frac{\gamma v}{c^2} (x_2 - x_1) = \gamma \Delta t - \frac{\gamma v}{c^2} (x_2 - x_1),$

where x_2 and x_1 are the event sites as observed in the unprimed frame. Within the temporal interval of Δt , the primed frame has moved through a distance of $v\Delta t$ (as observed by an observer in the unprimed frame), which is equal to the displacement of the two event sites from the unprimed frame point of view: $(x_2 - x_1) = v\Delta t$.

Hence,
$$\Delta \tau = \gamma \Delta t - \frac{\gamma v}{c^2} (v \Delta t) = \gamma \Delta t - \frac{\gamma v^2}{c^2} \Delta t = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} \Delta t \left(1 - \frac{v^2}{c^2}\right) = \Delta t \sqrt{1 - \frac{v^2}{c^2}} = \Delta t / \gamma$$
.

Hence we recover time dilation formula: $\Delta \tau = \Delta t / \gamma$

2. An object of rest mass M decays into two daughter objects of rest mass m_1 and m_2 respectively. Calculate the kinetic energy for each of the daughter masses respectively in terms of M, m_1 and m_2 .

ANS

By conservation of energy: total energy before decay = total energy after decay: $E = E_1 + E_2$,

where $E = Mc^2 E_1 = K_1 + m_1c^2$, $E_2 = K_2 + m_2c^2$

SESSI 06/07/Quiz 1

$$\Rightarrow Mc^{2} = (K_{1} + K_{2}) + (m_{1} + m_{2})c^{2}$$
 Eq(1)

For daughter mass 1:

$$E_1^2 = p_1^2 c^2 + m_1^2 c^4$$
. Eq. (2)

Likewise, for daughter mass 2: $E_2^2 = p_2^2 c^2 + m_2^2 c^4$ Eq. (3) Due to conservation of momentum: $|\vec{p}_2| \equiv p_2 = |\vec{p}_1| \equiv p_1 \equiv p$

Eq. (3) - Eq. (2):

$$E_2^2 - E_1^2 = (m_2^2 - m_1^2)c^4$$

 $\Rightarrow (E_2 - E_1)(E_2 + E_1) = (m_2^2 - m_1^2)c^4$
Eq. (4)

Substitute
$$E_1 = K_1 + m_1c^2$$
, $E_2 = K_2 + m_2c^2$ and $E_1 + E_2 = E = Mc^2$ into Eq. (4),

$$\Rightarrow \left[(K_2 - K_1) + (m_2 - m_1)c^2 \right] (Mc^2) = (m_2^2 - m_1^2)c^4$$

$$\Rightarrow (K_2 - K_1) = \left(\frac{m_2^2 - m_1^2}{M} \right) c^2 - (m_2 - m_1)c^2$$
Eq. (5)

We can then solve for K_1 and K_2 from Eq. (5) and Eq. (1):

Eq. (5) + Eq. (6):

$$\Rightarrow 2K_2 = Mc^2 - (m_1 + m_2)c^2 + \left(\frac{m_2^2 - m_1^2}{M}\right)c^2 - (m_2 - m_1)c^2$$

$$\Rightarrow K_2 = \frac{1}{2} \left[M - m_2\left(2 - \frac{m_2}{M}\right) - \frac{m_1^2}{M}\right]c^2$$

Eq. (5) - Eq. (6):

$$\Rightarrow 2K_1 = Mc^2 - (m_1 + m_2)c^2 - \left(\frac{m_2^2 - m_1^2}{M}\right)c^2 + (m_2 - m_1)c^2$$

$$\Rightarrow K_1 = \frac{1}{2}\left[M - 2m_1 - \left(\frac{m_2^2 - m_1^2}{M}\right)\right]c^2 = \frac{1}{2}\left[M - m_1\left(2 - \frac{m_1^2}{M}\right) - \left(\frac{m_2^2}{M}\right)\right]c^2$$

1

SESSI 06/07/Quiz 2

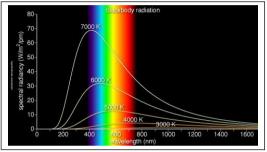
ZCT 104/3E Modern Physics Semester II, Sessi 2006/07 Open Book Quiz 2 (5 Feb 2007) **Duration: 30 min**

Name:

Matrics No:

INSTRUCTION: Answer the following question. Write your answer at the back of this question paper. (5 + 5 = 10 marks.)

A typical spectral distribution of radiation energy of a blackbody for several temperatures is as shown.



The shift of the peak of the curve was found to obey the empirical relationship, $\lambda_{n}T = \text{constant}$, (Wein's displacement law)

where the symbol λ_{c} refers to the value of the wavelength corresponding to the peak of the curve. The *total* power radiated per unit area (i.e. its intensity) of a blackbody is found to be empirically related to its absolute temperature by

$I(T) = \sigma T^4$, (the Stefan-Boltzman law)

where $\sigma = 5.6699 \times 10^{-8}$ watts m⁻² degree⁻⁴ (Stefan constant). The radiance, $R(\lambda, T)$ is the power radiated per unit area per unit wavelength interval at a given wavelength λ and a given temperature T. I(T) and $R(\lambda,T)$

are related by the integral $I(T) = \int R(\lambda, T) d\lambda$. Wein proposed an empirical form for the radiance $R(\lambda, T)$ by

constructing a mathematical function to fit the experimental blackbody curve, knows as the Wein's law:

$$R(\lambda,T) = \frac{ae^{-b/\lambda T}}{\lambda^5}$$
 (Wein's law)

The quantities a and b are not derived but are simply curve-fitting parameters.

Ouestion:

From Wien's law as given above, derive the constant in the displacement law, and (5 marks) *(i)* (ii) derive the Stefan constant (5 marks) in terms of *a* and *b*.

Hint: You may need
$$\int_{0}^{\infty} \frac{e^{-\frac{1}{x}}}{x^5} dx = 6$$
 or $\int_{0}^{\infty} x^3 e^{-x} dx = 6$.

SESSI 06/07/Ouiz 2

Solution

(i)

1

$$R(\lambda,T) = \frac{ae^{-b/\lambda T}}{\lambda^{5}}$$

$$\frac{d}{d\lambda}R(\lambda,T) = a\left[\frac{b}{T}\left(\frac{1}{\lambda^{2}}\right)\lambda^{5}e^{-b/\lambda T} - 5\lambda^{4}e^{-b/\lambda T}\right]/\lambda^{10} \qquad (Eq. 1)$$
Minimize $R(\lambda,T)$ with respect to λ , we will get λ_{0} .

$$\frac{\mathrm{d}}{\mathrm{d}\lambda}R(\lambda,T)\Big|_{\lambda} = 0 \qquad (2 \text{ marks})$$

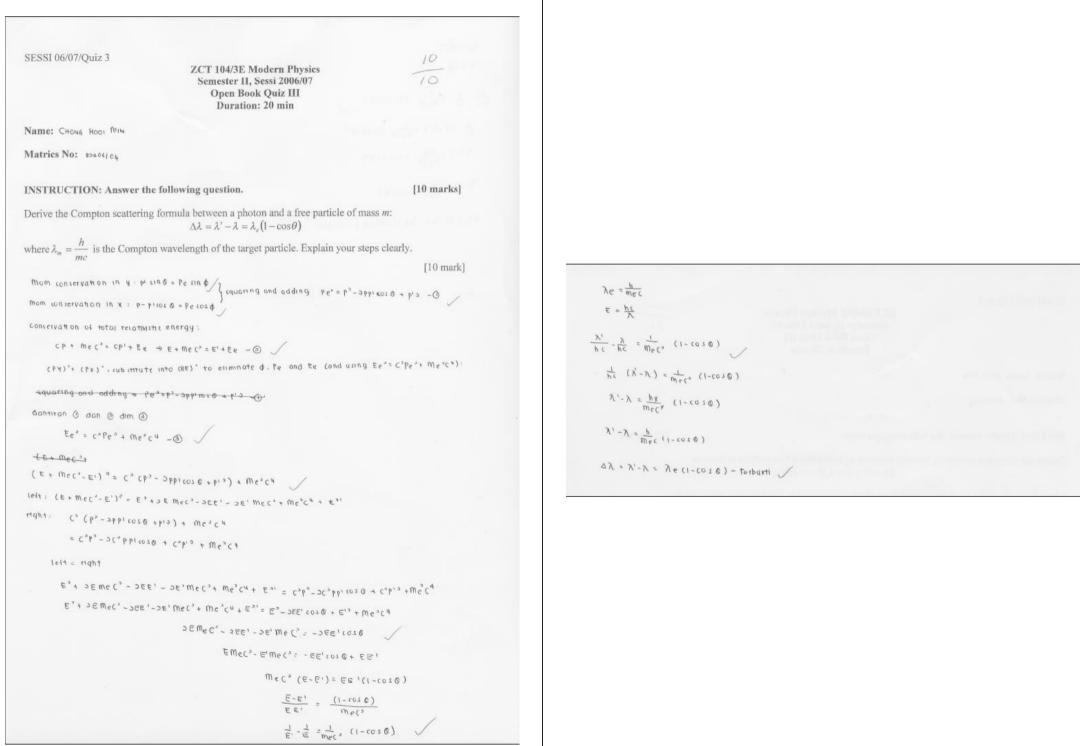
Setting Eq. 1 to zero, we get $\frac{b}{T}\lambda_{\rm p}{}^{3}e^{-b/\lambda_{\rm p}T} = 5\lambda_{\rm p}{}^{4}e^{-b/\lambda_{\rm p}T}$ $\Rightarrow \lambda_{\rm p} T = b/5$

(show working, 2 marks) (correct answer: 1 marks)

ii) Stafan-Boltzman law:
$$I(T) = \sigma T^4$$

Substitute Wein's law, $R(\lambda, T) = \frac{ae^{-b/\lambda T}}{\lambda^5}$, into the definition of $I(T) = \int_0^\infty R(\lambda, T) d\lambda$, we get
 $I(T) = \int_0^\infty R(\lambda, T) d\lambda = \int_0^\infty \frac{ae^{-b/\lambda T}}{\lambda^5} d\lambda$. (1 marks)
Define $x = \frac{b}{\lambda T} \Rightarrow dx = -\frac{b}{T} \frac{1}{\lambda^2} d\lambda$
 $I(T) = a \left(\frac{T}{b}\right)^4 \int_0^\infty x^3 e^{-x} dx = 6a \left(\frac{T}{b}\right)^4$ (show working, 3 marks)
 $\Rightarrow I(T) = 6a \left(\frac{T}{b}\right)^4 \equiv \sigma T^4 \Rightarrow \sigma \equiv \frac{6a}{b^4}$ (correct answer, 1 mark)

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ZCT 104/3E Modern Physics Semester II, Sessi 2006/07 Open Book Quiz IV Duration: 30 min

Name:

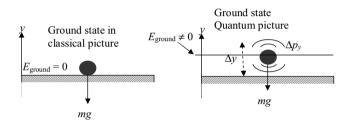
Matrics No:

INSTRUCTION: Answer the following question.

[10 marks]

A particle under gravity

A particle falls under gravity towards an impenetrable floor.



According to classical mechanics, the ground state (the state of least energy) is one in which the particle is at rest on the floor. Let us measure the distance vertically from the floor and call it y. Thus, we know the position of the particle in its ground state (y = 0) and also its momentum ($p_y=0$). This contradicts the uncertainty principle. In the quantum picture, we know that a particle cannot rest on the floor even under the pull of gravity. Even in the lowest energy state, the particle bounces up and down with a range Δy and Δp_y according to the Uncertainty principle. See the picture above.

(i) Write down the uncertainty relation that relates Δy and Δp_y .

[2 marks]

The potential energy of the particle is

$$V(y) = mgy \text{ if } y > 0,$$

= +\infty \expression if y < 0

(ii) What is the approximate energy of the particle at the ground state? (*Hint: The ground state* energy is the sum of the potential energy and the kinetic energy. You should express the energy estimate in terms of Δy .)

[4 marks]

(iii) Estimate the order of Δy in terms of *m* (*Hint: To obtain the estimate of* Δy , you simply minimise the answer obtained in (ii) with respect to Δy)

[4 marks]

1

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SESSI 06/07/Quiz 4

ZCT 104/3E Modern Physics Semester II, Sessi 2006/07 Open Book Quiz IV Duration: 30 min

Name:

(i)

Matrics No:

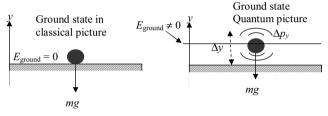
INSTRUCTION: Answer the following question.

[10 marks]

Particle under gravity

A particle under gravity

A particle falls under gravity towards an impenetrable floor.



According to classical mechanics, the ground state (the state of least energy) is one in which the particle is at rest on the floor. Let us measure the distance vertically from the floor and call it y. Thus, we know the position of the particle in its ground state (y = 0) and also its momentum ($p_y=0$). This contradicts the uncertainty principle. In the quantum picture, we know that a particle cannot rest on the floor even under the pull of gravity. Even in the lowest energy state, the particle bounces up and down with a range Δy and Δp_y according to the Uncertainty principle. See the picture above.

Write down the uncertainty relation that relates Δy and Δp_y . [2 marks]

ANS: The ground state will differ from the classical solution by having an uncertainty in position of Δy and momentum Δp_y where

 $\Delta p_y \sim \hbar / (2\Delta y)$. (2 marks) (Note: never mind if the factor 2 is missing since this is an estimate anyway)

(ii) Then the energy is approximately

$$E \sim \frac{\left(\Delta p_{y}\right)^{2}}{2m} + mg\Delta y = \frac{\hbar^{2}}{8m(\Delta y)^{2}} + mg\Delta y$$

[4 marks]

2

Note: Deduct half the marks if relativistic form of kinetic energy K = pc is used instead of non-

relativistic one (i.e. $K = \frac{p_y^2}{2m} \sim \frac{(\Delta p_y)^2}{2m}$). The question is obviously to be treated non-relativistically as we are talking about a 'rest' particle, of which motion is not expected to be fluctuating violently. (The violent the motion is the more relativistic it will be.)

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SESSI 06/07/Quiz 4

(iii) Minimizing the energy with respect to Δy ,

$$\frac{dE}{d(\Delta y)} = -\frac{\hbar^2}{8m} (\Delta y)^{-3} + mg = 0$$

$$\Rightarrow (\Delta y) = \left(\frac{\hbar^2}{8m^2g}\right)^{1/3} = \frac{1}{2} \left(\frac{\hbar^2}{m^2g}\right)^{1/3} \sim \left(\frac{\hbar^2}{m^2g}\right)^{1/3} \sim 10^{-23} \left(\frac{kg}{m}\right)^{2/3} m$$

Note: IF the candidate uses relativistic expression for the energy in (ii), i.e.

$$E = p_y c + mg\Delta y \sim \frac{nc}{2\Delta y} + mg\Delta y, \text{ and minimise it as per}$$
$$\frac{d}{d(\Delta y)} \left[\frac{\hbar c}{2\Delta y} + mg\Delta y \right] = -\frac{\hbar c}{2(\Delta y)^2} + mg = 0$$

to get

$$\frac{\hbar c}{2(\Delta y)^2} = mg \Rightarrow \Delta y = \left(\frac{\hbar c}{2mg}\right)^{1/2} \sim \left(\frac{\hbar c}{g}\right)^{1/2} \left(\frac{\mathrm{kg}}{m}\right)^{1/2} \mathrm{m} \sim 10^{-27} \left(\frac{\mathrm{kg}}{m}\right)^{1/2} \mathrm{m}$$

only half of 4 marks shall be given.

SESSI 06/07/Quiz 5

ZCT 104/3E Modern Physics Semester II, Sessi 2006/07 Open Book Quiz V Duration: 30 min

Name:

Matrics No:

INSTRUCTION: Answer the following question.

[12 marks]

Four possible transitions for a hydrogen atom are listed here.

(i) $n_i = 2$; $n_f = 5$ (ii) $n_i = 5$; $n_f = 3$

(iv) $n_i = 4; n_f = 7$

- (a) For which transitions does the atom emit photon? [2 marks]
- (b) Which transition emits the shortest wavelength? Show your argument and steps of calculation clearly. [4 marks]

(iii) $n_i = 7$; $n_f = 4$

- (c) For which transitions does the atom gain energy? [2 marks]
- (d) For which transition does the atom gain most energy? Show your argument and steps of calculation clearly. [4 marks]

(Serway, M & M. Q11, pg. 145)

Solution

For atom emitting photon, $\frac{1}{\lambda} = R\left(\frac{1}{n_t^2} - \frac{1}{n_i^2}\right) \Rightarrow \lambda = \frac{1}{R}\left(\frac{n_t^2 n_i^2}{n_i^2 - n_t^2}\right)$ with $n_t < n_i$; For atom absorbing photon, $\frac{1}{\lambda} = R\left(\frac{1}{n_i^2} - \frac{1}{n_t^2}\right) \Rightarrow \lambda = \frac{1}{R}\left(\frac{n_t^2 n_i^2}{n_t^2 - n_i^2}\right)$ with $n_t > n_i$

(a) (ii), (iii) emit photon. [2 marks. 1 for each correct answer. No mark deduced for wrong answer.]

(b) Test the emitted photons' wavelength $\lambda(n_i, n_f)$ for (ii), (iii) in turn: For (ii), $\lambda(n_i = 5, n_f = 3) = \frac{1}{R} \left(\frac{(3)^2 (5)^2}{(5)^2 - (3)^2} \right) = \frac{1}{R} \left(\frac{225}{25 - 9} \right) = \frac{1}{R} \left(\frac{225}{16} \right) \approx \frac{14.06}{R}$ For (iii) $\lambda(n_i = 7, n_f = 4) = \frac{1}{R} \left(\frac{(4)^2 (7)^2}{(7)^2 - (4)^2} \right) = \frac{1}{R} \left(\frac{784}{49 - 16} \right) = \frac{1}{R} \left(\frac{784}{33} \right) \approx \frac{23.8}{R}$.

Hence, (ii) emits the shortest wavelength.

[1 mark for showing the correct use of $\frac{1}{\lambda} = R\left(\frac{1}{n_t^2} - \frac{1}{n_i^2}\right) \Rightarrow \lambda = \frac{1}{R}\left(\frac{n_t^2 n_i^2}{n_i^2 - n_t^2}\right)$ with $n_f < n_i$] [2 marks for showing $\lambda(n_i = 5, n_f = 3) \approx \frac{14.06}{R}$ and $\lambda(n_i = 7, n_f = 4) \approx \frac{23.8}{R}$ correctly.]

[1 mark for stating the correct answer, "(ii) emits the shortest wavelength"]

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3

[4 mark]

1

SESSI 06/07/Quiz 5

(c) Atoms in (i), (iv) gain energy. [2 marks. 1 for each correct answer. No mark deduced for wrong answer.]

(d) Test the absorbed photons' wavelength $\lambda(n_i, n_f)$ for (i), (iv) in turn:

For (i),
$$\lambda(n_i = 2, n_f = 5) = \frac{1}{R} \left(\frac{(2)^2 (5)^2}{(7)^2 - (4)^2} \right) = \frac{1}{R} \left(\frac{100}{49 - 16} \right) = \frac{1}{R} \left(\frac{100}{33} \right) \approx \frac{3.03}{R}$$

For (iv), $\lambda(n_i = 4, n_f = 7) = \frac{1}{R} \left(\frac{(4)^2 (7)^2}{(7)^2 - (4)^2} \right) = \frac{1}{R} \left(\frac{784}{49 - 16} \right) = \frac{1}{R} \left(\frac{784}{33} \right) \approx \frac{23.8}{R}$

Hence, atom in (i) gains most energy since the shorter the wavelength of a photon, the larger the energy it has.

[1 mark for showing the correct use of $\frac{1}{\lambda} = R\left(\frac{1}{n_i^2} - \frac{1}{n_f^2}\right) \Rightarrow \lambda = \frac{1}{R}\left(\frac{n_i^2 n_i^2}{n_i^2 - n_i^2}\right)$ with $n_f > n_i$.] [2 marks for showing $\lambda(n_i = 2, n_f = 5) \approx \frac{3.03}{R}$ and $\lambda(n_i = 4, n_f = 7) \approx \frac{23.8}{R}$ correctly]

[1 mark for stating the correct answer, "(i) gains most energy"]

2

-1-

UNIVERSITI SAINS MALAYSIA

Second Semester Examination Academic Session 2006/2007

April 2007

ZCT 104E/3 – Physics IV (Modern Physics) [Fizik IV (Fizik Moden]

Duration: 3 hours [Masa : 3 jam]

Please ensure that this examination paper contains **XXX** pages before you begin the examination.

[Sila pastikan bahawa kertas peperiksaan ini mengandungi XXX muka surat yang bercetak sebelum anda memulakan peperiksaan ini.]

Instruction:

Answer ALL questions in Section A and Section B.

Please answer the objective questions from Section A in the objective answer sheet provided. Please submit the objective answer sheet and the answers to the structured questions separately.

Students are allowed to answer all questions in Bahasa Malaysia or in English.

[Arahan: Jawab SEMUA soalan dalam Bahagian A dan Bahagian B.

Sila jawab soalan-soalan objektif daripada bahagian A dalam kertas jawapan objektif yang dibekalkan. Sila serahkan kertas jawapan objektif dan jawapan kepada soalan-soalan struktur berasingan.

Pelajar dibenarkan untuk menjawab samada dalam bahasa Malaysia atau bahasa Inggeris.]

SESSI 06/07/Final Exam

- 2 -

Data

Speed of light in free space, $c = 3.00 \times 10^8$ m s⁻¹ Permeability of free space, $\mu_0 = 4\pi \times 10^{-7}$ H m⁻¹ Permittivity of free space, $\varepsilon_0 = 8.85 \times 10^{-12}$ F m⁻¹ Elementary charge, $e = 1.60 \times 10^{-19}$ C Planck constant, $h = 6.63 \times 10^{-34}$ J s Unified atomic mass constant, $u = 1.66 \times 10^{-27}$ kg Rest mass of electron, $m_e = 9.11 \times 10^{-31}$ kg Rest mass of proton, $m_p = 1.67 \times 10^{-27}$ kg Molar gas constant, $a = 6.02 \times 10^{23}$ mol⁻¹ Avogadro constant, $N_A = 6.02 \times 10^{23}$ mol⁻¹ Gravitational constant, $G = 6.67 \times 10^{-11}$ N m² kg⁻² Acceleration of free fall, g = 9.81 m s⁻²

- 3 -

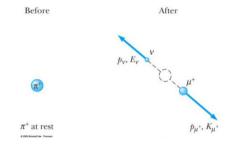
[ZCT 104E]

Section A: Objectives. [40 marks] [Bahagian A: Soalan-soalan objektif]

Instruction: Answer all 40 objective questions in this Section. [Arahan: Jawab kesemua 40 soalan objektif dalam Bahagian ini.]

Question 1 - 3 are based on the decay of a π meson into a muon and a massless neutrino shown in the figure below. The rest mass of the muon is m_{μ} , and the kinetic energy of the muon is measured to be K_{μ} , p_{μ} denotes the momentum of the muon. m_{π} denotes the rest mass of π meson.

[Soalan 1-3 adalah berdasarkan pereputan satu meson π kepada satu muon dan satu neutrino tanpa jisim, sepertimana ditunjukkan dalam gambarajah di bawah. Diketahui jisim rehat muon ialah m_{μ} dan tenaga kinetik muon yang terukur ialah K_{μ} . p_{μ} menandakan momentum muon. m_{π} menandakan jisim rehat meson π .]



 $\mathbf{D}.m_{c}^{2}$

- *I*. How is the energy of the muon E_{μ} related to the momentum of the muon? [Bagaimanakah tenage muon E_{μ} dikaitkan dengan momentum muon?] **A.** $E_{\mu}^2 = p_{\mu}^2 c^2 - m_{\mu}^2 c^4$ **B.** $E_{\mu} = p_{\mu}c + m_{\mu}c^2$ **C.** $E_{\mu} = p_{\mu}c$ **D.** $E_{\mu}^2 = p_{\mu}^2 c^2 + m_{\mu}^2 c^4$ **E.** None of A. B. C. D [Jawapan tiada dalam A. B. C. D]
- 2. What is the kinetic energy of the π meson? [Apakah tenaga kinetik meson π ?]

ANS:D

A. $K_{\mu} + m_{\mu}c^2$ **B.** 0 **C.** K_{μ} **E.** None of A, B, C, D [Jawapan tiada dalam A, B, C, D] **ANS:B.**

3. What is the momentum of the neutrino? [Apakah momentum neutrino?]

A.
$$p_v = \frac{1}{c} \sqrt{K_{\mu} (2m_{\mu}c^2 + K_{\mu})}$$

B. $p_v = \frac{1}{c} \sqrt{(2m_{\mu}^2 c^4 + K_{\mu}^2)}$
C. $p_v = K_v / c$
D. 0

C. $p_v = K_{\mu}/c$

E. None of A, B, C, D [Jawapan tiada dalam A, B, C, D] ANS:A.

4 -4. Which of the following statements is (are) true regarding the spectrum of hydrogen atom, according to the Bohr model?

[Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai spektrum atom hidrogen menurut model Bohr?]

- I. The Lyman series emission spectrum of a hydrogen atom lies in the visible region of the electronmagnetic spectrum. (F) [Spektrum pancaran siri Lyman atom hidrogen terletak dalam rantau nampak spektrum elektromagnetik.]
- II. The Balmer series emission spectrum of a hydrogen atom lies in the ultraviolet region of the electronmagnetic spectrum. (F) [Spektrum pancaran siri Balmer atom hidrogen terletak dalam rantau ultraungu spektrum elektromagnetik.]
- III. The Paschen series emission spectrum of a hydrogen atom lies in the ultraviolet region of the electronmagnetic spectrum. (T) [Spektrum pancaran siri Paschen atom hidrogen terletak dalam rantau ultra ungu spektrum elektromagnetik.]
- IV. Not all of the emission spectrum of a hydrogen atom lies in the visible region of the electronmagnetic spectrum. (T) [Bukan kesemua spektrum pancaran siri atom hidrogen terletak dalam rantau nampak spektrum elektromagnetik.]

A. I, II, III, IV D. III, IV E. (None of A, B, C) /Jawapan tidak terdapat dalam pilihi

C. II, IV

E. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] ANS: D (Only III, IV are true)

5. Which of the following statements is (are) true regarding the kinetic energy and momentum of an object?

[Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai tenaga kinetik dan momentum suatu objek?]

- I. The kinetic energy of an object is the energy associated with the motion of the object. (T) [Tenaga kinetik suatu objek adalah tenaga yang berkaitan dengan pergerakan objek.]
- II. The kinetic energy of an object cannot be larger than its total energy. (T) [Tenaga kinetik suatu objek tidak boleh melebihi jumlah tenaganya.]
- III. The relativistic expression of momentum reduces to that of the classical theory of machanics in the limit $v \ll c$. (T) [Ungkapan momentum keretatifan terturun kepada ungkapan mekanik teori klasik dalam limit $v \ll c$.]

- IV. The classical expression of kinetic energy has to be supplanted by that of the special theory of relativity when v approaches c from below. (T) [Ungkapan tenaga kinetik klasik harus digantikan oleh ungkapan kerelatifan jika v menokok ke c dari bawah.]
- A. I, II, III B. II, IV C. I, II, III, IV

D. I, III, IV

E. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] ANS: C IMv own question.]

6. Consider a proton and an electron, both moving at a common momentum, p. Let K_p and K_e denote the proton and electron kinetic energies respectively. Which of the following statements is (are) true?

[Pertimbangkan suatu proton dan suatu elektron, kedua-duanya bergerak dengan momentum yang sama, p. Biar K_p dan K_e masing-masing menandakan tenaga kinetik proton dan elektron. Yang manakah kenyataan(-kenyataan) berikut adalah benar?]

- I. $K_{\rm p} = K_{\rm e}$ for v < c. $[K_{\rm p} = K_{\rm e} untuk v < c.](F)$
- II. $K_p \neq K_e$ in general. $/K_p \neq K_e$ pada amnya./(T)
- III. $K_p > K_e$ for all values of v < c. $[K_p > K_e$ untuk semua nilai v < c.](F)
- IV. $K_e > K_p$ for $v \ll c$. $[K_e > K_p$ untuk $v \ll c$.](T)

A. II only B. I, IV C. II, III D. II, IV E. (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C] ANS: D

Note: In the limit v<<c, $\frac{K_p}{K_e} = \frac{p^2 / 2m_p}{p^2 / 2m_e} \Rightarrow \frac{K_p}{K_e} = \frac{m_e}{m_p} \Rightarrow K_p = \frac{m_e}{m_p} K_e < K_e$

- 7. Which of the following statements is (are) true according to the special theory of relativity? [Yang manakah kenyataan(-kenyataan) berikut adalah benar menurut teori kerelatifan?]
 - I. A massless particle can travel at the speed lower than the speed of light. [F] [Suatu zarah tanpa jisim mungkin bergerak dengan laju yang kurang daripada laju cahaya.]
 - II. A particle with non-zero mass does not necessarily travel at the speed smaller than that of light. [F] [Suatu zarah dengan jisim bukan sifar tidak semestinya bergerak dengan laju yang

kurang daripada laju cahaya.]

- III. The rest mass of a moving object changes when it is moving. (F) [Jisim rehat suatu objek berubah bila ia bergerak.]
- IV. It requires an infinite amount of energy to accelerate a massive object to the speed of light. (T) [Tenaga yang infinit diperlukan untuk memecutkan suatu zarah kepada laju cahaya..]

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8. When two particles collide relativistically, [Bila dua zarah berlanggar secara kerelatifan,]

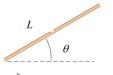
c

- I. the total momentum is conserved. [jumlah momentum adalah terabadikan.](T)
- II. the total kinetic is conserved. [jumlah tenaga kinetik adalah terabadikan.](F)
- III. the total kinetic energy is an invariant. [jumlah tenaga kinetik adalah tak varian.](F)
- IV. the total rest mass is conserved. [jumlah jisim rehat adalah terabadikan.](F)
- A.
 I, III
 B. I Only
 C. III, IV

 D.
 I, II, III, IV

 E.
 (None of A, B, C) [Jawapan tidak terdapat dalam pilihan-pilihan A, B, C]

 ANS: D.
- 9. In its rest frame, a rod has a proper length of L and is orientated at an angle of θ= 45° with the x-axis. The rod then move at a speed of u = c/2 in the x-direction. [Dalam rangka rehatnya, suatu rod dengan panjang lazim L diorientasikan pada suatu sudut θ = 45° merujuk kepada paksi-x. Ia kemudian bergerak pada laju u = c/2 dalam arah x.]



Direction of motion

What is the length of the rod as observed in the improper frame? [Apakah panjang rod tersebut dalam rangka tak lazim?]

A.
$$L$$
 B. $\frac{\sqrt{7}}{4}L$ **C.** $\frac{3}{4}L$ **D**

E. None of A, B, C, D [Jawapan tiada dalam A, B, C, D] **ANS:B**

10. In Question 9, what is the inclination angle of the rod with respect to the *x*-axis as observed in the improper frame?

[Dalam solaan 9, apakah sudut di antara rod dengan paksi-x dalam rangka tak lazim?]

A.
$$\tan^{-1}\left(\frac{\sqrt{7}}{8}\right)$$
 B. $\tan^{-1}\left(\frac{\sqrt{3}}{2}\right)$ C. $\tan^{-1}(1)$
D. $\tan^{-1}\left(\frac{2}{\sqrt{3}}\right)$
E. None of A, B, C, D [Jawapan tiada dalam A, B, C, D]
ANS:D

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11. What measurement(s) do two observers in relative motion always agree on? [Apakah ukuran(-ukuran) yang sentiasa disetujui oleh dua orang pemerhati yang berada dalam pergerakan relatif]

-7-

- I The speed of an electron moving in medium water. [Laju suatu elektron dalam medium air.](F)
- II The time interval between two events. [Selang masa antara dua kejadian.](F)
- **III** The number of particles. [bilangan zarah.](T)
- **IV** The density of an object. [Ketumpatan suatu objek](F)

A. II, IIIB. I, II, IVC. II, III, IVD. I, IIE. None of A, B, C, D [Jawapan tiada dalam A, B, C, D]Solution: only III is true

12. The units of the work function are those of: [Unit bagi fungsi kerja adalah sama dengan unit bagi ...]

> A. energy B. power C. momentum D. angular momentum E. frequency Solution: A

13. The S.I. units of 1-D wavefunction are those of: [Unit bagi fungsi gelombang 1D adalah sama dengan unit bagi ...]

A. $1/\sqrt{\text{length}}$ B. $1/\sqrt{\text{energy}}$ C. $1/\sqrt{\text{momentum}}$ D. $1/\sqrt{\text{frequency}}$

Solution: A

14. The light intensity incident on a metallic surface produces photoelectrons with a maximum kinetic energy of 2 eV. The light intensity is doubled. Determine the maximum kinetic energy of the photoelectrons (in eV).

[Keamatan cahaya yang menujui suatu permukaan logam menghasilkan fotoelektron dengan tenaga kinetik maksimum 2 eV. Keamatan cahaya digandaduakan. Tentukan tenaga kinetik maksimum fotoelektron terhasil (dalam eV).]

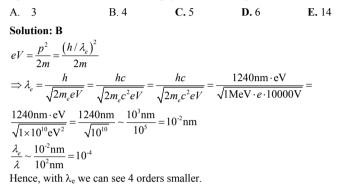
E. $1/\sqrt{\text{mass}}$

A. 4 **B.**2 **C.** $\sqrt{2}$ **D.**3 **E.**16 **Solution: B**

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- 8 15. Microscopes are inherently limited by the wavelength of the light used. How much smaller (in order of magnitude) can we "see" using an electron microscope whose electrons have been accelerated through a potential difference of 10 000 V than using red light (100 nm)?

[Secara tabiinya mikroskop dihadkan oleh jarak gelombang cahaya yang digunakan. Berbanding dengan penggunaan cahaya merah (100 nm), betapa kecilkah (dalam magnitud tertib) yang boleh kita 'nampak' dengan menggunakan mikroskop elektron yang elektronnya dipecutkan melalui suatu beza keupayaan 10 000 V?]



16. Which of the following statements is (are) true about photon?

[Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai foton?]

- **I.** A photon will either be absorbed or otherwise when interacts with matter. [*Suatu foton akan terserap atau tidak dalam interaksinya dengan jirim*]. [*T*]
- II. Photons have mass. [foton mempunyai jisim.] [F]
- III. Photons have electric charge. [foton mempunyai cas electrik.] [F]
- **IV.** Photons can be accelerated via an electric field. [*foton boleh dipecutkan oleh suatu medan elektrik.*][F]

A. II, III **B.** I, II, IV **C.** II, III, IV **D.** I, II E. None of A, B, C, D *[Jawapan tiada dalam A, B, C, D]*

Solution: E, Only I is true Solution: Young and Freeman, pg. 1485, Q38

17. Which of the following statements is (are) true about the nature of light?

[Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai tabii cahaya?]

 Effects due to the photon nature of light are generally more important at the lowfrequency end of the electromagnetic spectrum (radio waves). [Kesan-kesan disebabkan oleh tabii foton dalam cahaya secara amnya adalah lebih penting pada hujung frekuensi rendah spektrum elektromagnet (gelombang radio)]. [F]

II. Effects due to the photon nature of light are generally more important at the high-frequency end of the electromagnetic spectrum (x-rays and gamma rays).
 [Kesan-kesan disebabkan oleh tabii foton dalam cahaya secara amnya adalah lebih penting pada hujung frekuensi tinggi spektrum elektromagnet (sinaran-X dan sinaran gamma).] [T]

-9-

- III. Effects due to the wave nature of light are generally more important at the low-frequency end of the electromagnetic spectrum (radio waves).
 [Kesan-kesan disebabkan oleh tabii gelombang dalam cahaya secara amnya adalah lebih penting pada hujung frekuensi rendah spektrum elektromagnet (gelombang radio)]. [T]
- IV. Effects due to the wave nature of light are generally more important at the high-frequency end of the electromagnetic spectrum (x-rays and gamma rays).
 [Kesan-kesan disebabkan oleh tabii gelombang dalam cahaya secara amnya adalah lebih penting pada hujung frekuensi tinggi spektrum elektromagnet (sinaran-X dan sinaran gamma).] [F]

A. II, III B. I, IV C. I, III D. II, IV E. None of A, B, C, D *[Jawapan tiada dalam A, B, C, D]* Solution: A

18. The total energy (kinetic plus potential) of the hydrogen atom is negative. What significance does this have?

[Jumlah tenaga (kinetik serta keupayaan) atom hidrogen adalah negatif. Apakah kepentingannya?]

- A. The hydrogen atom is ionized. [*Atom higrogen diionkan*.]
- **B.** The angular momentum of the electron is quantized. [*Momentum sudut elektron terkuantumkan.*]
- **C.** The electron is bonded by the hydrogen atom's electric field. [*Elektron adalah terikat oleh medan elektrik atom hidrogen.*]
- D. The hydrogen atom is a free particle. [Atom hidrogen adalah zarah bebas.]
- E. None of A, B, C, D [Jawapan tiada dalam A, B, C, D]

Solution: C

 A double ionized lithium atom (Li⁺⁺) is one that has had two of its three electrons removed. The ground state energy of the Li⁺⁺ is _____ times the ground state energy of the hydrogen atom.

[Suatu atom lithium yang berganda terionkan ialah atom yang dua daripada tiga elektronnya disingkirkan. Keadaan dasar Li^{++} adalah _____ kali tenaga dasar hidrogen.]

A.2	B. 4	C.8	D. 9
E.32			

Solution: D. Note: $E_n = -\frac{Z^2}{n^2}E_0$

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- 10 -
- 20. In photoelectric effect experiment, which of the following will increase the maximum kinetic energy of the photoelectron? [Dalam eksperimen kesan fotoelektrik, yang manakah berikut akan menambahkan tenaga kinetik maksmum fotoelektron?]
 - I. Use the light of greater intensity. [Guna cahaya yang keamatannya lebih tinggi]. [F]
 - II. Use the light of greater frequency. [Guna cahaya yang frekuensinya lebih tinggi]. [T]
 - III. Use the light of greater wavelength. [Guna cahaya yang jarak gelombangnya lebih tinggi]. [F]
 - IV. Use metal surface with a smaller work function. [Guna permukaan logam yang fungsi kerjanya lebih rendah]. [T]

A. II, III	B. I, IV	C. I, III	D. II, IV
E. None of A, E	B, C, D [Jawapan tiada	ı dalam A, B, C, D]	
Solution: D			

- 21. Which of the following associations with experiments is (are) true? [Yang manakah perhubungan-perhubungan dengan eksperimen berikut adalah benar?]
 - I. The Davisson-Gremer experiment shows that electrons do behave like waves. [T] [*Eksperimen Davisson-Germer menunjukkan bahawa elektron berlagak seperti* gelombang.]
 - II. The Frank-Hertz experiment shows that atoms do behave like waves. [F] [Eksperimen Frank-Hertz menunjukkan bahawa atom-atom berlagak seperti gelombang.]
 - III. The Compton scattering experiment show that electrons behave like waves. [F] [Eksperimen Compton menunjukkan bahawa elektron berlagak seperti gelombang.]
 - IV. The Young double slit experiment using electron as the source shows that electrons do behave like waves. [T]
 [Eksperimen dwi-celah Young yang menggunakan elektron sebagai punca menunjukkan bahawa elektron berlagak seperti gelombang.]

A. II, III	B. I, IV	C. I, III	D. II, IV
E. None of A, B	, C, D [Jawapan tiad	a dalam A, B, C, D]	

ANS: B

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- 22. Say a beam of light has an intensity of *I* (i.e. the total energy per unit area per unit time) and frequency ν . What is the photon density, *n* (i.e. the number of photon per unit volume), of the light beam?

[Katakan keamatan satu alur cahaya ialah I (iaitu jumlah tenaga per unit permukaan per unit masa) dan frekuensinya ialah v. Apakah ketumpatan foton n (iaitu bilangan foton per unit isipadu) dalam alur cahaya tersebut?]

A. $(hc v)^2/l^2$ B. hc v/l C. l/(hc v) D. $l^2/(hc v)^2$ E. None of A, B, C, D [Jawapan tiada dalam A, B, C, D]

ANS: C

23. A particle of mass m is confined to a one-dimensional box of width L and infinite height. The particle's wavelength at state n is given by

[Suatu zarah yang terperangkap dalam suatu kotak satu dimensi dengan lebar L dan ketinggian infiniti. Jarak gelombang zarah tersebut pada keadaan n ialah]

A. 2L/nB. n/2LC. $2L/n\hbar$ D. $n\hbar/2L$ E. None of the aboveANS: A

24. The kinetic energy of the particle in Question 23 is given by

[Tenaga kinetik zarah dalam Soalan 23 ialah]

A.
$$n^{2} \frac{\hbar^{2}}{8m\pi L^{2}}$$
 B. $n^{2} \frac{\hbar^{2}}{8mL^{2}}$ **C.** $n^{2} \frac{\pi^{2} h^{2}}{2mL^{2}}$
D. $n^{2} \frac{\hbar^{2}}{2mL^{2}}$
E. None of the above

ANS: B

25. If the infinitely high potential box in Question 23 is replaced by one with a finite height, how would the wavelength of the particle at a given state *n* be modified as compared to the answer in Question 23?

[Jika keupayaan kotak yang infinit dalam Soalan 23 digantikan dengan kotak yang tinggi keupayaannya finit, bagaimanakah jarak gelombang zarah pada suatu keadaan n akan dimodifikasikan bila berbanding dengan jawapan untuk Soalan 23?]

- A. The wavelength would be longer than that in Question 23. [Jarak gelombang akan menjadi lebih panjang daripada jarak gelombang dalam Soalan 23.]
- B. The wavelength would be shorter than that in Question 23. [*Jarak gelombang akan menjadi lebih pendek daripada jarak gelombang dalam Soalan* 23.]
- C. The wavelength would be the same as that in Question 23. [Jarak gelombang adalah sama seperti jarak gelombang dalam Soalan 23.]

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D. The wavelength could be longer or shorter than that in Question 23, depending on the state n.

[Jarak gelombang akan menjadi lebih panjang atau lebih pendek daripada jarak gelombang dalam Soalan 23, bergantung kepada keadaan n.]

E. None of the above.

ANS: A

26. Following Question 25, how would the kinetic energy of the particle at a given state *n* be modified as compared to the answer in Question 24?

[Menurut Soalan 25, bagaimanakah tenaga kinetik zarah pada suatu keadaan n akan dimodifikasikan bila berbanding dengan jawapan untuk Soalan 24?]

- A. The kinetic energy would be larger than that in Question 24.
- B. The kinetic energy would be smaller than that in Question 24.
- C. The kinetic energy would be the same as that in Question 24.
- D. The kinetic energy could be larger or smaller than that in Question 24, depending on the state *n*.
- E. None of the above

ANS: B

27. If the finite potential box in Question 25 is in turn replaced by one with a width larger than L, how would the wavelength of the particle at a given state n be modified as compared to the answer in Question 25?

[Jika kotak yang berkeupayaan finit dalam Soalan 25 digantikan dengan kotak yang lebarnya lebih besar daripada L, bagaimanakah jarak gelombang zarah pada suatu keadaan n akan dimodifikasikan bila berbanding dengan jawapan untuk Soalan 25?]

- A. The wavelength would be longer than that in Question 25.
- B. The wavelength would be shorter than that in Question 25.
- C. The wavelength would be the same as that in Question 25.
- D. The wavelength could be longer or shorter than that in Question 25, depending on the state
- *n*. E. None of the above

28. Following Question 27, how would the kinetic energy of the particle at a given state *n* be modified as compared to the answer in Question 26?

[Menurut Soalan 27, bagaimanakah tenaga kinetik zarah pada suatu keadaan n akan dimodifikasikan bila berbanding dengan jawapan untuk Soalan 26?]

- A. The kinetic energy would be larger than that in Question 26.
- B. The kinetic energy would be smaller than that in Question 26.
- C. The kinetic energy would be the same as that in Question 26.
- D. The kinetic energy could be larger or smaller than that in Question 26, depending on the state *n*.
- E. None of the above

ANS: B

ANS: A

[ZCT 104E]

- 29. What are the features of a X-rays curve as produced from a X-ray tube?
 - I. The spectrum is continuous.
 - II. The existence of a minimum wavelength for a given accelerating potential V, below which no x-ray is observed.
 - III. Increasing V decreases the minimum wavelength.
 - IV. There exists an upper limit in the wavelength of the X-ray produced.

 A. II, III
 B. I, IV
 C. I, II, III
 D. I, II, III, IV

 E. None of A, B, C, D [Jawapan tiada dalam A, B, C, D]
 ANS: C

30. Which of the following statements is (are) true?

[Yang manakah kenyataan(-kenyataan) berikut adalah benar?]

I. In photoelectricity the whole photon is directly absorbed by the free electron in the metal surface.

[Dalam kesan fotoelektrik keseluruh foton diserap secera terus oleh elektron bebas dalam permukaan logam.] [F]

- II. In photoelectricity the whole photon is first absorbed by the atom in the metal surface. [Dalam kesan fotoelektrik keseluruh foton terdahulunya diserap oleh atom dalam permukaan logam.] [T]
- III. In X-ray production by electron bombardment on a metal target, the kinetic energy of the bombarding electron is converted to the X-ray photon energy via Bremsstrahlung. [Dalam penghasilan sinar-X oleh penghentaman elektron ke atas sasaran logam, tenaga kinetik elektron yang menghentam ditukarkan kepada tenaga foton sinar-X melalui Bremsstrahlung.] [T]
- IV. In the X-ray production using the X-ray tube, the energy of the X-ray photon is converted to the kinetic energy of the electron via Bremsstrahlung.
 [Dalam penghasilan sinar-X dalam tiub sinar-X, tenaga foton ditukarkan kepada tenaga kinetik elektron melalui Bremsstrahlung.] [F]

A. II, IV	B. I, IV	C. II, III	D. I, III
E. None of A, B, C, D [Jawapan tiada dalam A, B, C, D]			
ANS: C		_	

31. Which of the following statements is (are) true?

[Yang manakah kenyataan(-kenyataan) berikut adalah benar?]

A photon can materialize into an electron plus a positron in the absence of any electric field.
 [Suatu foton boleh bertukar menjadi jirim satu elektron serta satu positron dalam ketidakhadiran medan elektrik.] [F]

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- II. A photon can materialize into either a single electron OR a single positron in the presence of a strong electric field.
 [Suatu foton boleh bertukar menjadi jirim satu elektron tunggal atau satu positron tunggal dalam kehadiran medan elektrik kuat.] [F]
- III. An electron-positron pair can annihilate into a single photon.
 [Suatu pasangan elektron-positron boleh menghabisbinasa menjadi satu foton tunggal.]
 [F]
- IV. An electron-positron pair can annihilate into two photons. [Suatu pasangan elektron-positron boleh menghabisbinasa menjadi dua foton.] [T]

A. II, IVB. I, IVC. II, IIID. I, IIIE. None of A, B, C, D [Jawapan tiada dalam A, B, C, D]ANS: E (Only IV is true)

32. Which of the following statements is (are) true regarding the interactions between photons with matter?

[Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai interaksi foton dengan jirim?]

- I. The probability (cross section) of a photon undergoes a given channel of interaction with matter depends on the photon energy. [Kebarangkalian (keratan rentas) suatu foton menjalani mana-mana saluran interaksi dengan jirim bergantung kepada tenaga foton.] [T]
- II. The probability (cross section) of a photon undergoes a given channel of interaction with matter depends on the atomic number of the absorbing material.
 [Kebarangkalian (keratan rentas) suatu foton menjalani mana-mana saluran interaksi dengan jirim bergantung kepada nombor atom bahan penyerap.] [T]
- III For a fixed atomic number, the photon-material interactions at low energy are dominated by photoelectric effect.
 [Pada suatu nombor atom yang tertentu, interaksi di antara foton dengan jirim pada tenaga rendah dikuasai oleh kesan fotoelektrik.] [T]
- IV. Pair production begins to show up when the photon energy approaches, but not yet exceed, the value of 1.02 MeV. [Penghasilan pasangan mula muncul semasa tenaga foton menhampiri, tapi belum melebihi, nilai 1.02 MeV.] [F]
- A. I, III, IV
 B. I, II, IV
 C. II, III
 D. I, II, III

 E. None of A, B, C, D [Jawapan tiada dalam A, B, C, D]
 D. I, II, III
 D. I, II, III

[ZCT 104E]

ANS: D

33. A relativistic electron has a de Broglie wavelength of λ . Find its kinetic energy.

[Jarak gelombang de Broglie suatu elektron kerelatifan ialah λ . Dapatkan tenaga kinetiknya.]

- 15 -

A.K = $((hc/\lambda)^2 - m_e^2 c^4)^{\frac{1}{2}} + m_e c^2$. B.K = $((hc/\lambda)^2 + m_e^2 c^4)^{\frac{1}{2}} + m_e c^2$. C.K = $((\lambda/hc)^2 + m_e^2 c^4)^{\frac{1}{2}} - m_e c^2$. D.K = $((hc/\lambda)^2 + m_e^2 c^4)^{\frac{1}{2}} - m_e c^2$. E. None of the above ANS: D

34. In the Davisson-Gremer experiment, the electron is accelerated via an electric potential of V. The wavelength of the electron, λ , in terms of V is given by the expression

[Dalam eksperimen Davisson-Gremer, elektron dipecutkan oleh keupayaan elektrik V. Jarak gelombang elektron, λ , dalam ungkapan V, adalah diberikan oleh]

A. $\lambda = (2eVm_e)^{1/2}/h$ B. $\lambda = h^{1/2}/(2eVm_e)$ C. $\lambda = h/(2eVm_e)$ D. $\lambda = h/(2eVm_e)^{1/2}$ E. None of the above ANS: D

Questions 35 - 37 are based on Figure 1. [Soalan 35 - 37 adalah berdasarkan gambarajah 1.]

35. Figure 1 shows three group waves. Which of the group waves has the largest spatial spread, Δx ?

[Gambarajah 1 menunjukkan 3 gelombang kumpulan. Yang mana satukah mempunyai sebaran ruagan Δx yang terbesar?] (ANS: C)

36. Which of the group waves has the largest spread in wavelength, $\Delta \lambda$?

[Yang mana satukah mempunyai sebaran jarak gelombang $\Delta\lambda$ yang terbesar?] (ANS: A)

37. Which of the group waves has the largest spread in wave number, Δk ?

[*Yang mana satukah mempunyai sebaran nombor gelombang* Δk *yang terbesar*?] (ANS: A)

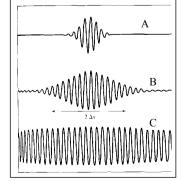
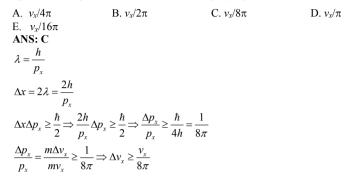


Figure 1

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38. Assume that the uncertainty in the position of a particle is equal to two times its de Broglie wavelength. What is the minimal uncertainty in its velocity?[*Anggap bahawa ketidakpastian dalam kedudukan suatu zarah adalah bersamaan 2 kali jarak gelombang de Broglienya. Apakah ketidakpastian mimimum dalam halajunya*?]

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- 39. Which of the following statements is (are) true? [Yang manakah kenyataan(-kenyataan) berikut adalah benar?]
 - I. The length scale characterizing atomic physics is $\sim A$. [Skala panjang yang mencirikan fizik atom ialah $\sim \mathring{A}$.] [T]
 - II. The velocity scale characterizing special relativistic effect is $\sim c$. [*Skala halaju yang mencirikan kesan kerelatifan khas ialah* $\sim c$] [*T*]
 - III. The length scale characterizing Compton scattering is ~ pm. [Skala panjang yang mencirikan serakan Compton ialah ~ pm] [T]
 - IV. The energy scale characterizing pair creation is ~ MeV. [Skala tenaga yang mencirikan penghasilan pasangan ialah ~ MeV] [T]
 - A. I, III, IV B. I, II, III C. I, IV D. I, II, III, V E. None of A, B, C, D [Jawapan tiada dalam A, B, C, D] ANS: D
- 40. Which of the following statements is (are) true regarding Bohr's hydrogen model? [Yang manakah kenyataan(-kenyataan) berikut adalah benar mengenai model hidrogen Bohr?]
 - I. The velocity of the electron in the lower orbits is relativistic. [Halaju elektron dalam orbit rendah adalah kerelatifan.] [F]
 - II. The kinetic energy of the electron in the lower orbits is relativistic. [*Tenaga kinetik elektron dalam orbit rendah adalah kerelatifan.*] [F]

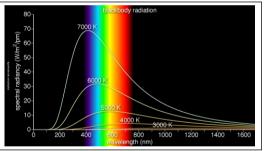
- 17 -III. The model does not take into account the effect of Heisenberg uncertainty principle. [Model tersebut tidak mengambil kira kesan prinsip ketidakpastian Heisenberg] [T]
- IV. The energy scale characterizing the transition is ~ keV. [Skala tenaga yang mencirikan peralihan ialah ~ keV] [F]

A. III Only B. I, II, IV C. I, II D. III, V E. None of A, B, C, D [Jawapan tiada dalam A, B, C, D] ANS: A

Section B: Structural questions. [*Bahagian B: Soalan-soalan strutur.*]

Instruction: [Arahan:] Answer ALL questions. Each question carries 20 marks. [Jawab semua soalan. Setiap soalan membawa 20 markah.]

1. (a) A typical spectral distribution of radiation energy of a black body for several temperatures is as shown. [*Terpapar adalah suatu taburan spektrum yang tipikal bagi tenaga pancaran suatu jasad hitam untuk beberapa suhu.*]



The shift of the peak of the curve was found to obey the empirical Wein's displacement law, $\lambda_{\rm p}T$ = constant ,

where the symbol λ_p refers to the value of the wavelength corresponding to the peak of the curve.

The *total power radiated per unit area* of a blackbody is found to be empirically related to its absolute temperature by the *the Stefan-Boltzman law*

$$I(T) = \sigma T^4$$

where σ is the Stefan constant. The radiance, $R(\lambda, T)$ and I(T) are related by the integral

$$I(T) = \int_{0}^{\infty} R(\lambda, T) \mathrm{d}\lambda.$$

Wein proposed an empirical form for the radiance $R(\lambda, T)$ by constructing a mathematical function to fit the experimental blackbody curve, known as the *Wein's law*:

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$$R(\lambda,T) = \frac{-18}{\lambda^5} - \frac{18}{\lambda^5}$$
 (Wein's law)

The quantities a and b are not derived but are simply curve-fitting parameters.

On the theoretically front, Planck derives his famous blackbody radiation law by assuming that the energies emitted from the oscillators are quantized. In his theory, the radiance is given by the theoretical expression

$$R(\lambda,T) = \frac{2\pi hc^2}{\lambda^5 \left(e^{hc/\lambda kT} - 1\right)}$$
(Planck's law)

[Anjakan puncak lengkungan didapati mematuhi hukum sesaran Wein, $\lambda_p T$ = pemalar, dengan λ_p mewakili nilai jarak gelombang pada puncak lengkungan.

Jumlah kuasa pancaran per unit permukaan suatu jasad hitam didapati berkait secara empirikal kepada suhu mutlak oleh hukum Stefan-Boltzman, $I(T) = \sigma T^4$, dengan σ pemalar

Stefan. Radians, $R(\lambda,T)$ dikaitkan dengan I(T) oleh kamiran $I(T) = \int R(\lambda,T) d\lambda$.

Wein menyarankan suatu bentuk empirikal bagi $R(\lambda,T)$ dengan membinakan suatu fungsi matematik untuk memadankan lengkungan eksperimen jasad hitam. Ia dikenali sebagai hukum Wein: $R(\lambda,T) = \frac{ae^{-b/\lambda T}}{\lambda^5}$. Kuantiti a dan b bukannya diterbitkan tapi sekadar merupakan parameter-parameter untuk memadankan lengkungan.

Dalam garis depan teori, Planck menerbitkan hukum jasad hitamnya yang masyur dengan anggapan bahawa tenaga terpancar daripada pengayun adalah terkuantumkan. Dalam teorinya, radians diberikan oleh

 $R(\lambda,T) = \frac{2\pi hc^2}{\lambda^5 \left(e^{hc/\lambda kT}-1\right)}.$

]

Using Planck's law as given above, [Dengan menggunakan hukum Planck,]

- (i) show that it reduces to Wein's law in the short wavelength limit. [tunjukkan bahawa ia terturun kepada hukum Wein dalam limit jarak gelombang pendek.]
- (*ii*) Evaluate *a* and *b* in terms of the natural constants (i.e. k, c, h, π). [*Nilaikan a dan b dalam sebutan pamalar semulajadi, iaitu k, c, h, \pi*]

(iii)Evaluate the Stefan constant. [Nilaikan pemalar Stefan.]

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If the photocurrent of a photocell is cut off by a retarding potential of 0.92 V for monochromatic radiation of 2500 Å, what is the work function of the material? [*Jika fotoarus suatu fotosel dipengal oleh keupayaan rencatan 0.92 V untuk pancaran* monokromatik 2500 Å, apakan funsi kerja bahan tersebut?]

- 19 -

[4]

(c)

(b)

- (*i*) What is the frequency of a X-rays photon with momentum 1.1×10^{-23} kg·m/s [*Apakah frekuensi suatu foton sinar-X dengan momentum* 1.1×10^{-23} kg·m/s ?]
- (ii) What is the momentum of (c)(i) in unit of eV/c? [Apakah memomtum di (c)(i) dalam unit eV/c?]

[3+3=6]

2. (a) Derive the Compton scattering formula $\lambda' - \lambda = \frac{h}{mc} (1 - \cos \theta)$, where λ and λ' are the

wavelengths of the incident and scattered photon respectively, θ the scattered angle of the photon, *m* the mass of target particle.

[Terbitkan formula serakan Compton $\lambda' - \lambda = \frac{h}{mc} (1 - \cos \theta)$.] [10]

(b) Determine the wavelength of a photon that is emitted when a atom hydrogen makes a transition from state n = 10 to the ground state.

[Tebtukan jarak gelombang foton yang dipancarkan apabila suatu atom hydrogen beralih dari keadaan n = 10 ke keadaan asas.]

[5]

(c) Given the wave function of a particle in an infinite $box \psi_n(x) = \sqrt{\frac{2}{L}} \sin \frac{n\pi x}{L}$, where *L* is the width of the box. Find the probability that the particle can be found between x = 0 and x = L/n when it is in the *n*th state. [Diberikan fungsi gelombang zarah dalam kotak infini $\psi_n(x) = \sqrt{\frac{2}{L}} \sin \frac{n\pi x}{L}$, di mana *L* ialah lebar kotak tersebut. Carikan kebarangkalian untuk mencarikan zarah di antara x=0 dan x=L/n bila ia berada dalam keadaan n.] [5]

3. (a) Consider three inertial frames that are moving along a common direction. The relative velocity of S' with respect to S is $\beta_1 c$, whereas the relative velocity of S' with respect to S' is

 $\beta_2 c$. Find the velocity of S'' with respect to S, βc , in terms of $\beta_1 c$, and $\beta_2 c$. [Pertimbangkan tiga rangka inersia yang bergerak sepanjang arah yang sama. Halaju relatif S' terhadap S ialah $\beta_1 c$, manakala halaju relatif S'' terhadap S' ialah $\beta_2 c$. Carikan halaju S'' terhadap S, βc , dalam sebutan $\beta_1 c$ dan $\beta_2 c$.] - 20 -

(b) The kinetic energy, *K*, of a fast-moving alpha particle (with rest mass M_{α}) is measured in the laboratory. [*Tenaka kinetik*, *K*, *bagi suatu zarah alfa (dengan jisim rehat* M_{α}) *diukurkan dalam makmal*.]

(i) What is its total energy E? [Apakah jumlah tenaganya?]

- (ii) What is its momentum p? [Apakah momentumnya?]
- (iii) What's the increase in its mass (as compared to its mass when at rest), ΔM_{α} ? [Apakah pertambahan dalam jisimnya (berbanding dengan jisimnya semasa ia berehat)?]
- (*iv*) Based on the answer of (*ii*) above, show that the expression of the kinetic energy K reduces to the classical one in the limit $v \rightarrow c$, where v is the velocity of the alpha particle.

[Berdasarkan jawapan dalam (ii) di atas, tunjukkan bahawa sebutan tenaga kinetik K terturun kepada sebutan tenaga kinetik klasikal dalam limit $v \rightarrow c$, dengan v halaju zarah alfa.]

[2+3+2+3]

1(A) ANS Elmer Anderson, pg49, problem 2-6.

(i) For short wavelength, the exponential term in Planck's law, $e^{hc/\lambda kT}$, becomes very large compared to the value 1, $e^{hc/\lambda kT} >> 1$, hence the term in the bracket in the denominator of the Planck's law reduces to $e^{hc/\lambda kT}$, i.e.

$$\lim_{\lambda \to 0} \frac{2\pi hc^2}{\lambda^5 \left(e^{hc/\lambda kT} - 1\right)} = \frac{2\pi hc^2}{\lambda^5} e^{-hc/\lambda kT} . \qquad \text{Eq. (1)}$$

Comparing Eq. (1) and the Wein's law, we find that both have the same form of λ -dependence,

$$\frac{2\pi hc^2}{\lambda^5}e^{-hc/\lambda kT}\equiv\frac{ae^{-b/\lambda T}}{\lambda^5}.$$

[satisfactory argument: 2 MARKS]

(*ii*) Comparing both equation, we identify the constants a and b to be

$$a \equiv 2\pi hc^2$$
 [2 MARKS]
 $b \equiv hc/k$ [2 MARKS]

(*iii*) Stafan-Boltzman law: $I(T) = \sigma T^4$

[ZCT 104E]

$$\begin{aligned} & -21 - \\ \text{Substitute Planck's law, } R(\lambda, T) = \frac{2\pi\hbar c^2}{\lambda^5 (e^{\hbar c/\lambda kT} - 1)}, \text{ into the definition of} \\ I(T) = \int_0^\infty R(\lambda, T) d\lambda, \text{ we get} \\ I(T) = \int_0^\infty R(\lambda, T) d\lambda = \int_0^\infty \frac{2\pi\hbar c^2}{\lambda^5 (e^{\hbar c/\lambda kT} - 1)} d\lambda = 2\pi\hbar c^2 \int_0^\infty \frac{1}{\lambda^5 (e^{\hbar c/\lambda kT} - 1)} d\lambda. \\ \text{Define } x = \frac{\hbar c}{\lambda kT} \Longrightarrow dx = -\frac{\hbar c}{kT} \frac{1}{\lambda^2} d\lambda \\ I(T) = 2\pi\hbar c^2 \int_0^\infty \frac{1}{\lambda^5 (e^{\hbar c/\lambda kT} - 1)} d\lambda = 2\pi\hbar c^2 \int_0^\infty \frac{1}{\lambda^3 (e^x - 1)} \frac{d\lambda}{\lambda^2} \\ = -\frac{2\pi k^4 T^4}{\hbar^3 c^2} \int_\infty^\infty \frac{x^3}{e^x - 1} dx = \frac{2\pi k^4 T^4}{\hbar^3 c^2} \int_0^\infty \frac{x^3}{e^x - 1} dx = \frac{2\pi k^4 T^4}{\hbar^3 c^2}.$$
 Hence, the Stefan constant is $\sigma = \frac{2\pi^5 k^4 T^4}{15\hbar^3 c^2}.$ [4 marks]

1(C)(i) ANS: 5×10¹⁸ Hz [3 marks] 1(C)(ii)ANS: xx eV/c [3 marks]

- 2(A) ANS Elmer E. Anderson, pg. 66 (BM version). [10 marks]
- 2(B) ANS: (Beiser, BM version, pg 161, Soalan 3) [5 marks]
- 2(C) ANS (Beiser, Ex. 19, pg. 198)
- The probability density is given by $p_{\mu}(x) = \psi_{\mu}(x)\psi_{\mu}^{*}(x)$, where the wave function of a particle in a box is

$$\psi_n(x) = \sqrt{\frac{2}{L}} \sin \frac{n\pi x}{L}; \text{ The probability to find the particle between } x_2 \text{ and } x_1 \text{ within the box is}$$

$$P_n(x_2, x_1) = \int_{x_1}^{x_2} \psi_n(x) \psi_n^*(x) dx = \frac{2}{L} \int_{x_1}^{x_2} \sin^2 \frac{n\pi x}{L} dx = \left(\frac{x}{L} - \frac{x}{2n\pi} \sin \frac{2\pi nx}{L}\right) \Big|_{x_1}^{x_2}. \text{ Here, set } x_2 = L/n, x_1 = 0,$$

$$P(L/n, 0) = \left(\frac{x}{L} - \frac{x}{2\pi} \sin \frac{2\pi x}{L}\right) \Big|_{0}^{L/n} = \left(\frac{1}{n} - \frac{L}{2\pi n} \sin 2\pi n\right) - (0 - 0) = \frac{1}{n}$$
[5 marks]

3(A) ANS Elmer E. Anderson, pg. 19 (BM version), problem 1-10.

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- 22 -Take S' to be the 'rest frame'. S'' is moving with respect to S' with a velocity of $u_x = \beta_2 c$. Take S as the "moving frame", moving at a velocity of $v = -\beta_1 c$ with respect to the frame S'. Hence, the velocity of

$$u'_{x} = \frac{u_{x} - v}{1 - \frac{u_{x}v}{c^{2}}} = \frac{\beta_{2}c - (-\beta_{1}c)}{1 - \frac{(\beta_{2}c)(-\beta_{1}c)}{c^{2}}} = \frac{(\beta_{2} + \beta_{1})c}{1 + \beta_{2}\beta_{1}}$$

Note: one can check the correctness of the above result by considering two limiting cases:

- i. When $\beta_2 \rightarrow 0$, S'' becomes S', hence, we should recover $u'_x \rightarrow \beta_1 c$.
- ii. When $\beta_1 \rightarrow 0$, S becomes S', hence, we should recover $u'_x \rightarrow \beta_2 c$.

S'' with respect to S, u'_x , is related to both u_x and v via the formula

[10 marks]

3(B) ANS (My own question)

(*i*) Total energy $E = K + M_{\alpha}c^2$ [2 marks]

- (ii) $E = K + M_{\alpha}c^2 \Rightarrow E^2 = (K + M_{\alpha}c^2)^2$ Energy-momentum invariance: $E^2 = p^2c^2 + M_{\alpha}^2c^4$ Eliminating *E* in the above equations, $p = \sqrt{(K^2/c^2 + 2KM_{\alpha})}$. [3 marks]
- (*iii*) Let *M* be the relativistic mass of the alpha particle. Its total energy is then related to this mass as per $E = Mc^2$. But $E = K + M_a c^2$, hence, the increase in mass $\times c^2$, $\Delta M_a c^2 = Mc^2 - M_a c^2 = (K + M_a c^2) - M_a c = K$ $\Rightarrow \Delta M_a c^2 = K$ [2 marks]
- (iv) In the limit of $v \to c$, the relativistic expression for the momentum reduces to classical one, i.e. $p_{SR} = \gamma M_{\alpha} v \to p_{Classical} = M_{\alpha} v$. Hence, from (ii), as $v \to c$, $\sqrt{(K^2/c^2 + 2KM_{\alpha})} = M_{\alpha} v$. Squaring, $K^2/c^2 + 2KM_{\alpha} = M_{\alpha}^2 v^2$. Solving the quadratic equation in K: $K^2 + 2KM_{\alpha}c^2 - M_{\alpha}^2 v^2 c^2 = 0$ The positive root is given by $K = [-2M_{\alpha}c^2 + \sqrt{(4M_{\alpha}^2c^4 + 4M_{\alpha}^2v^2c^2)}]/2 = -M_{\alpha}c^2 + \sqrt{(M_{\alpha}^2c^4 + M_{\alpha}^2v^2c^2)}$ $= -M_{\alpha}c^2 + M_{\alpha}c^2 (1 + v^2/c^2)^{1/2} = -M_{\alpha}c^2 + M_{\alpha}c^2 (1 + v^2/2c^2 + ...)$ (Binomial expansion) $= M_{\alpha}v^2/2$ (retaining the term up to order of v^2/c^2) [3 marks]

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- 23 -5. ANS:D 6. ANS:B. 7. ANS:A. 8. ANS: D (Only III, IV are true) 9. ANS: C [My own question.] 10. ANS: D 11. ANS: D [My own question.] Note: In the limit $v \leq c$. $\frac{K_P}{K_e} = \frac{p^2 / 2m_P}{p^2 / 2m_e} \Longrightarrow \frac{K_P}{K_e} = \frac{m_e}{m_P} \Longrightarrow K_P = \frac{m_e}{m_P} K_e < K_e$ 12. ANS: D. 13. ANS:B 14. ANS:D 15. Solution: E. only III is true 16. Solution: A 17. Solution: A 18. Solution: B 19. Solution: B $eV = \frac{p^2}{2m} = \frac{\left(h/\lambda_e\right)^2}{2m}$ $\Rightarrow \lambda_e = \frac{h}{\sqrt{2m_e eV}} = \frac{hc}{\sqrt{2m_e c^2 eV}} = \frac{hc}{\sqrt{2m_e c^2 eV}} = \frac{1240 \text{nm} \cdot \text{eV}}{\sqrt{1 \text{MeV} \cdot e \cdot 10000 \text{V}}} =$ $\frac{1240\text{nm} \cdot \text{eV}}{\sqrt{1 \times 10^{10} \text{eV}^2}} = \frac{1240\text{nm}}{\sqrt{10^{10}}} \sim \frac{10^3 \text{nm}}{10^5} = 10^{-2} \text{nm}$ $\frac{\lambda_e}{\lambda} \sim \frac{10^{-2} \mathrm{nm}}{10^2 \mathrm{nm}} = 10^{-4}$ Hence, with λ_e we can see 4 orders smaller. 20. Solution: E, Only I is true. Young and Freeman, pg. 1485, Q38 21. Solution: A 22. Solution: C Note: $E_n = -\frac{Z^2}{n^2}E_0$ 23. Solution: D. 24. Solution: D 25. ANS: B 26. ANS: C 27. ANS: A 28. ANS: B 29. ANS: A **30.** ANS: B 31. ANS: A 32. ANS: B 33. ANS: C 34. ANS: C 35. ANS: E (Only IV is true) 36. ANS: D 37. ANS: D 38. ANS: D

SESSI 06/07/Final Exam - 24 -39. (ANS: C) 40. (ANS: A) 41. (ANS: A) 42. ANS: C $\lambda = -\frac{h}{2}$ $\Delta x = 2\lambda = \frac{2h}{p_x}$ $\Delta x \Delta p_x \ge \frac{\hbar}{2} \Longrightarrow \frac{2h}{p_x} \Delta p_x \ge \frac{\hbar}{2} \Longrightarrow \frac{\Delta p_x}{p_x} \ge \frac{\hbar}{4h} = \frac{1}{8\pi}$ $\frac{\Delta p_x}{p_x} = \frac{m\Delta v_x}{mv_x} \ge \frac{1}{8\pi} \Longrightarrow \Delta v_x \ge \frac{v_x}{8\pi}$

43. ANS: D 44. ANS: A

Section B: Structural questions.

[Bahagian B: Soalan-soalan strutur.]

1(A) ANS Elmer Anderson, pg49, problem 2-6.

For short wavelength, the exponential term in Planck's law, $e^{hc/\lambda kT}$, becomes very large (iv) compared to the value 1, $e^{hc/\lambda kT} >>1$, hence the term in the bracket in the denominator of the Planck's law reduces to $e^{hc/\lambda kT}$, i.e.

$$\lim_{\lambda \to 0} \frac{2\pi hc^2}{\lambda^5 \left(e^{hc/\lambda kT} - 1\right)} = \frac{2\pi hc^2}{\lambda^5} e^{-hc/\lambda kT} . \qquad \text{Eq. (1)}$$

Comparing Eq. (1) and the Wein's law, we find that both have the same form of λ -dependence,

$$\frac{2\pi hc^2}{\lambda^5} e^{-hc/\lambda kT} \equiv \frac{a e^{-b/\lambda T}}{\lambda^5}.$$

[satisfactory argument: 2 MARKS]

- Comparing both equation, we identify the constants a and b to be (v) $a \equiv 2\pi hc^2$ [2 MARKS] $b \equiv hc/k$ [2 MARKS]
- Stafan-Boltzman law: $I(T) = \sigma T^4$ (vi) Substitute Planck's law, $R(\lambda, T) = \frac{2\pi hc^2}{\lambda^5 (e^{hc/\lambda kT} - 1)}$, into the definition of $I(T) = \int_{0}^{\infty} R(\lambda, T) d\lambda$, we get

[ZCT 104E]

$$I(T) = \int_{0}^{\infty} R(\lambda, T) d\lambda = \int_{0}^{\infty} \frac{2\pi hc^2}{\lambda^5 (e^{hc/\lambda kT} - 1)} d\lambda = 2\pi hc^2 \int_{0}^{\infty} \frac{1}{\lambda^5 (e^{hc/\lambda kT} - 1)} d\lambda.$$

Define $x = \frac{hc}{\lambda kT} \Rightarrow dx = -\frac{hc}{kT} \frac{1}{\lambda^2} d\lambda$

$$I(T) = 2\pi hc^2 \int_{0}^{\infty} \frac{1}{\lambda^5 (e^{hc/\lambda kT} - 1)} d\lambda = 2\pi hc^2 \int_{0}^{\infty} \frac{1}{\lambda^3 (e^x - 1)} \frac{d\lambda}{\lambda^2}$$

$$= -\frac{2\pi k^4 T^4}{h^3 c^2} \int_{0}^{0} \frac{x^3}{e^x - 1} dx = \frac{2\pi k^4 T^4}{h^3 c^2} \int_{0}^{\infty} \frac{x^3}{e^x - 1} dx = \frac{2\pi k^4 T^4}{h^3 c^2} \frac{\pi^4}{15} = \frac{2\pi^5 k^4 T^4}{15h^3 c^2}$$

Hence, the Stefan constant is $\sigma = \frac{2\pi^5 k^4 T^4}{15h^3 c^2}$. [4 marks]

1(B) ANS: 4.08 eV E. Anderson, pg. 57, Problem 2-16. **[4 marks]**

1(C)(i) ANS: 5×10¹⁸ Hz [3 marks] 1(C)(ii) ANS: xx eV/c [3 marks]

- 2(A) ANS Elmer E. Anderson, pg. 66 (BM version). [10 marks]
- 2(B) ANS: (Beiser, BM version, pg 161, Soalan 3) [5 marks]

2(C) ANS (Beiser, Ex. 19, pg. 198)

The probability density is given by $p_n(x) = \psi_n(x)\psi_n^*(x)$, where the wave function of a particle in a box is

$$\psi_n(x) = \sqrt{\frac{2}{L}} \sin \frac{n\pi x}{L}; \text{ The probability to find the particle between } x_2 \text{ and } x_1 \text{ within the box is}$$

$$P_n(x_2, x_1) = \int_{x_1}^{x_2} \psi_n(x) \psi_n^*(x) dx = \frac{2}{L} \int_{x_1}^{x_2} \sin^2 \frac{n\pi x}{L} dx = \left(\frac{x}{L} - \frac{x}{2n\pi} \sin \frac{2\pi nx}{L}\right) \Big|_{x_1}^{x_2}. \text{ Here, set } x_2 = L/n, x_1 = 0,$$

$$P(L/n, 0) = \left(\frac{x}{L} - \frac{x}{2\pi} \sin \frac{2\pi x}{L}\right) \Big|_{0}^{L/n} = \left(\frac{1}{n} - \frac{L}{2\pi n} \sin 2\pi n\right) - (0 - 0) = \frac{1}{n}$$

[5 marks]

3(A) ANS Elmer E. Anderson, pg. 19 (BM version), problem 1-10.

Take S' to be the 'rest frame'. S'' is moving with respect to S' with a velocity of $u_x = \beta_2 c$. Take S as the "moving frame", moving at a velocity of $v = -\beta_1 c$ with respect to the frame S'. Hence, the velocity of S'' with respect to S, u'_x , is related to both u_x and v via the formula

$$u'_{x} = \frac{u_{x} - v}{1 - \frac{u_{x}v}{c^{2}}} = \frac{\beta_{2}c - (-\beta_{1}c)}{1 - \frac{(\beta_{2}c)(-\beta_{1}c)}{c^{2}}} = \frac{(\beta_{2} + \beta_{1})c}{1 + \beta_{2}\beta_{1}}$$

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Note: one can check the correctness of the above result by considering two limiting cases:

iii. When $\beta_2 \rightarrow 0$, S'' becomes S', hence, we should recover $u'_x \rightarrow \beta_1 c$.

iv. When $\beta_1 \rightarrow 0$, S becomes S', hence, we should recover $u'_x \rightarrow \beta_2 c$.

[10 marks]

3(B) ANS (My own question)

(v) Total energy $E = K + M_{\alpha}c^2$ [2 marks]

- (vi) $E = K + M_{\alpha}c^2 \Rightarrow E^2 = (K + M_{\alpha}c^2)^2$ Energy-momentum invariance: $E^2 = p^2c^2 + M_{\alpha}^2c^4$ Eliminating *E* in the above equations, $p = \sqrt{(K^2/c^2 + 2KM_{\alpha})}$. [3 marks]
- (vii) Let *M* be the relativistic mass of the alpha particle. Its total energy is then related to this mass as per $E = Mc^2$. But $E = K + M_{\alpha}c^2$, hence, the increase in mass $\times c^2$, $\Delta M_{\alpha}c^2 = Mc^2 - M_{\alpha}c^2 = (K + M_{\alpha}c^2) - M_{\alpha}c = K$ $\Rightarrow \Delta M_{\alpha}c^2 = K$ [2 marks]
- (viii) In the limit of $v \ll c$, the relativistic expression for the momentum reduces to classical one, i.e. $p_{SR} = \gamma M_a v \rightarrow p_{Classical} = M_a v$. Hence, from (ii), as $v \ll c$, $p = M_a v = \sqrt{(K^2/c^2 + 2KM_a)}$. Squaring, $K^2/c^2 + 2KM_a = M_a^2 v^2$. Solving the quadratic equation in K: $K^2 + 2KM_ac^2 - M_a^2 v^2c^2 = 0$ The positive root is given by $K = [-2M_ac^2 + \sqrt{(4M_a^2c^4 + 4M_a^2v^2c^2)}]/2 = -M_ac^2 + \sqrt{(M_a^2c^4 + M_a^2v^2c^2)}$ $= -M_ac^2 + M_ac^2 (1 + v^2/c^2)^{1/2} = -M_ac^2 + M_ac^2 (1 + v^2/2c^2 + ...)$ (Binomial expansion) $= M_a v^2/2$ (retaining the term up to order of v^2/c^2) [3 marks]

UNIVERSITI SAINS MALAYSIA

Kursus Semasa Cuti Panjang Sessi 2006/2007

Jun 2007

ZCT 104/3 - Physics IV (Modern Physics) [Fizik IV (Fizik Moden)]

Duration: 3 hours [Masa : 3 jam]

Please ensure that this examination paper contains XXX pages before you begin the examination.

[Sila pastikan bahawa kertas peperiksaan ini mengandungi XXX muka surat yang bercetak sebelum anda memulakan peperiksaan ini.]

Instruction: Answer only FIVE questions out of six questions given.

Students are allowed to answer all questions in Bahasa Malaysia or in English.

[Arahan: Jawab LIMA soalan daripada enam solaan yang disediakan.

Sila jawab soalan-soalan objektif daripada bahagian A dalam kertas jawapan objektif yang dibekalkan. Sila serahkan kertas jawapan objektif dan jawapan kepada soalan-soalan struktur berasingan.

Pelajar dibenarkan untuk menjawab samada dalam bahasa Malaysia atau bahasa Inggeris.]

Data

Speed of light in free space, $c = 3.00 \times 10^8$ m s⁻¹ Permeability of free space, $\mu_0 = 4\pi \times 10^{-7}$ H m⁻¹ Permittivity of free space, $\varepsilon_0 = 8.85 \times 10^{-12}$ F m⁻¹ Elementary charge, $e = 1.60 \times 10^{-19}$ C Planck constant, $h = 6.63 \times 10^{-34}$ J s Unified atomic mass constant, $u = 1.66 \times 10^{-27}$ kg Rest mass of electron, $m_e = 9.11 \times 10^{-31}$ kg Rest mass of proton, $m_p = 1.67 \times 10^{-27}$ kg Molar gas constant, = 8.31 J K⁻¹ mol⁻¹ Avogadro constant, $N_A = 6.02 \times 10^{23}$ mol⁻¹ Gravitational constant, $G = 6.67 \times 10^{-11}$ N m² kg⁻² Acceleration of free fall, g = 9.81 m s⁻²

Instruction: Answer only 5 out of six questions prepared. Each question carries 20 marks.

[Arahan: Jawab hanya 5 soalan daripada 6 soalan yang disediakan. Setiap soalan membawa 20 markah.]

- 2 -

- (a) What is the de Broglie wavelength of an alpha particle (q = +2e, M_α= 6.64×10⁻²⁷ kg) accelerated from rest through a potential drop of 125 V?
 [Apakah jarak gelombang de Broglie zarah alfa (q = +2e, M_α= 6.64×10⁻²⁷ kg) yang dipecutkan daripada keadaan rehat melalui suatu kejatuhan keupayaan 125 V?]
 - (b) What is the energy of a photon that has wavelength 0.10 μm? Give your answer in unit of eV. [Apakah tenaga foton yang ber jarak gelombang 0.10 μm?Nyatakan jawapan anda dalam unit eV]

[3 marks]

(c) Show that the wavelength λ of an *relativistic* electron of kinetic energy K

and rest mass *m* is
$$\lambda = \frac{hc}{\sqrt{K(K + 2mc^2)}}$$
.

[Tunjukkan bahawa jarak gelombang λ suatu elektron kerelatifan yang tenaga kinetik K dan

berjisim rehat m diberikan oleh
$$\lambda = \frac{nc}{\sqrt{K(K+2mc^2)}}$$
.]

[8 marks]

(d) A block is attached to a massless spring. The spring is stretched from its equilibrium position and released, and the block is set into a simple harmonic motion with a total energy of 2.0 J with a frequency of oscillation 0.56 Hz. Assuming that the energy is quantised, find the quantum number *n* for the system.

[Suatu blok diikat kepada suatu spring yang jisimnya boleh dibaikan. Spring tersebut ditarik daripada kedudukan keseimbangannya dan dilepaskan. Blok tersebut melakukan gerakan harmonik mudah dengan jumlah tenaga 2.0 J dan frekuensi ayunan 0.56 Hz. Andaikan tenaga adalah terkuantumkan, cari nombor quantum n bagi sistem tersebut.]

[4 marks]

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2. (a) (*i*) The *x*-coordinate of an electron is measured with an uncertainty of 0.20 mm. What is the *x*-component of the electron's velocity, v_x , if the minimum percentage uncertainty in a simultaneous measurement of v_y is 1.0 %?

[Koordinat-x suatu elektron diukurkan dengan ketidakpastian 0.20 mm. Apakah komponen-x bagi halaju elektron, v_{xy} jika peratusan minimum ketidakpastian dalam ukuran v_x yang serentak ialah 1.0 %?]

[3 marks]

(ii) Repeat part a(i) for a proton.[Ulangi bahagian a(i) bagi kes proton]

[2 marks]

(b) The unstable W^+ particle has a rest energy of 80.41 GeV (1 GeV = 10⁹ eV) and an uncertainty in rest energy of 2.06 GeV. Estimate the lifetime of the W^+ particle. [Zarah W^+ yang tidak stabil mempunyai tenaga rehat 80.41 GeV dan ketidakpastian dalam tenaga rehat 2.06 GeV. Anggarkan jangka hayat zarah W^+]

[5 marks]

(c) The kinetic energy of a nonrelativistic particle in terms of its momentum can be writen as $K = p^2/2m$. Use the Heisenberg uncertainty principle to estimate the minimum kinetic energy of a proton confined within a nucleus having a diameter of 1 fm (1 fm = 10⁻¹⁵m) [*Tenaga kinetik suatu zarah tidak kerelatifan dalam sebutan momentumnya boleh dinyatakan sebagai* $K = p^2/2m$. Gunakan prinsip ketidakpastian Heisenberg untuk menganggarkan tenaga kinetik minimum suatu proton yang terperangkap dalam suatu nukleus yang berdiameter 1 fm.]

[10 marks]

3. (a) Electrons are ejected from a metallic surface with speeds ranging up to 4.6×10⁵ m/s when light with a wavelength of 625 nm is used in a photoelectric effect experiment. [Elektron dipancarkan daripada suatu permukaan logam dengan laju sehingga 4.6×10⁵ m/s bila cahaya berjarak gelombang 625 nm digunakan dalam suatu eksperiment kesan fotoelektrik.]

(*i*) What is the work function of the surface in unit of eV? [*Apakah fungsi kerja bagi permukaan tersebut dalam unit eV*?]

[4 marks]

(*ii*) What is the cutoff frequency for this surface?[Apakah frekuensi penggal bagi permukaan tersebut?]

[4 marks]

(b) Show that a photon cannot transfer all of its energy to a free electron. (*Hint:* Note that the system energy and momentum transfer must be conserved).

[Tunjukkan banawa suatu foton tidak boleh pindahkan kesemua tenaganya kepada suatu elektron bebas (Petunjuk: Dimaklumkan bahawa tenaga sistem dan momentum terpindahkan mest diabadikan.)]

[12 marks]

4. (a) A particle of mass *m* is confined to an impenetrable one-dimensional box between x = 0 and x = L. The wave function of the particle is $\psi(x) = A \sin\left(\frac{n\pi x}{L}\right)$.

[Suatu zarah berjisim m diperangkapkan dalam suatu kotak satu dimensi yang tidak boleh ditembusi di antara x = 0 and x = L. Fungsi gelombang zarah tersebut ialah $\psi(x) = A \sin\left(\frac{n\pi x}{L}\right)$.]

- (i) Use the normalization condition on ψ to obtain the normalization constant A.
 [Dengan menggunakan syarat normalisasi pada ψ, dapatkan pemalar normalisasi A.]
 [3 marks]
- (*ii*) Find the expectation value of the position *x* of the particle in the ground state.[Dapatkan nilai jangkaan bagi kedudukan x zarah dalam keadaan dasar.]

[6 marks]

(*iii*) Calculate the probability of finding the electron between x=0 and x = L/4 in the ground state.

[Hitungkan kebarangkalian menjumpai elektron di antara x=0 dan x=L/4 dalam keadaan dasar.]

[5 marks]

(b) Why is it impossible for the lowest-energy state of a harmonic oscillator to be zero? [Mengapakah keadaan pengayun harmonik pada tenaga paling rendah tidak boleh menjadi sifar?]

[6 marks]

5. (a) A particle has mass 5.52×10^{-27} kg. Compute the rest energy of the particle in MeV. [Suatu zarah berjisim 5.52×10^{-27} kg. Hitungkan tenaga rehat zarah tersebut dalam unit MeV.]

[5 marks]

(b) A cube of metal with sides of length a sits at rest in a frame S with one edge parallel to the x-axis. Therefore in S the cube has volume a³. Frame S' moves along the x-axis with a speed u. As measured by an observer in frame S', what is the volume of the metal cube? [Suatu kuib logam dengan sisinya a berada dalam keadaan rehat dalam rangka S. Salah satu sisi kuib adalah selari dengan paski-x rangka S. Jadi dalam rangka S isipadu kuib adalah a³. Rangka S' bergerak sepanjang paksi-x dengan laju u. Apakah isipadu kuib logam sebagaimana diukurkan oleh pemerhati dalam rangka S'?]

[5 marks]

(c) High-speed electrons are used to probe the interior structure of the atomic nucleus. For such electrons the expression $\lambda = h/p$ still holds, but we must use the relativistic expression

for momentum
$$p = \frac{mv}{\sqrt{1 - v^2/c^2}}$$
. Show that the speed of an electron that has de Broglie

wavelength
$$\lambda$$
 is $\nu = \frac{1}{\sqrt{1 + \left(\frac{mc\lambda}{h}\right)^2}}$

[Elektron berlaju tinggi biasanya digunakan untuk mempelapori struktur dalaman nukleus atom. Bagi elektron tersebut, kenyataan $\lambda = h/p$ masih benar tapi kita mesti menyatakan mv

momentumnya dalam bentuk kerelatifan, $p = \frac{mv}{\sqrt{1 - v^2/c^2}}$. Tunjukkan bahawa bagi elektron

yang jarak gelombang de Broglie-nya λ , lajunya diberikan oleh

$$v = \frac{c}{\sqrt{1 + \left(\frac{mc\lambda}{h}\right)^2}}$$

[10 marks]

6. (a) How much energy is required to ionise hydrogen? [Berapa banyakkah tenaga yang diperlukan untuk mengionkan hidrogen]

(i) in the ground state? [dalam keadaan dasar?]

[2 marks]

(ii) when it is in the state for which n=3? [bila ia berada pada keadaan n=3?]

[2 marks]

(b) Two hydrogen atoms collide head-on and end up with zero kinetic energy. Each atom then emits light with a wavelength of 121.6 nm (n=2 to n=1 transition). At what speed were the atoms moving before collision?

[Dua atom hidrogen berlanggar secara muka-sama-muka dan berakhiran dengan tenaga kinetik sifar. Setiap satu atom kemudian memancarkan cahaya berjarak gelombang 121.6 nm (perlihan n=2 kepada n=1). Apakah laju atom sebelum mereka berlanggar?] [4 marks]

(c) Based on the Bohr model, derive the expression for the Bohr radius for hydrogen atom from scratch. Express you answer in unit of $\stackrel{\circ}{A}$.

[Berdasarkan model Bohr, terbitkan ungkapan radius Bohr bagi atom hidrogen. Nyatakan jawapan anda dalam unit $\stackrel{\circ}{A}$.]

[10 marks]

SOLUTION

1. (a) What is the de Broglie wavelength of an alpha particle $(q = +2e, M_{\alpha} = 6.64 \times 10^{-27} \text{ kg})$ accelerated from rest through a potential drop of 125 V?

Solution

Young and Freedman, Chap 39, pg. 1516, Q39.43 (b)

Recall
$$\lambda = \frac{h}{p} = \frac{h}{\sqrt{2mE}} = \frac{h}{\sqrt{2mq\Delta V}}$$
. For an alpha particle:
 $\lambda = \frac{6.63 \times 10^{-34} \,\text{J} \cdot \text{s}}{\sqrt{2(6.64 \times 10^{-27} \,\text{kg})2(1.60 \times 10^{-19} \,\text{C})(125 \,\text{V})}} = 9.10 \times 10^{-13} \,\text{m}.$

(b) What is the energy of a photon that has wavelength 0.10 $\mu m?$ Give your answer in unit of eV.

Solution Young and Freedman, Chap 39, pg. 1515, Q39.37 (a)

 $E = hc/\lambda = 12.4 \text{eV}$

(c) Show that the wavelength λ of an *relativistic* electron of kinetic energy K and rest mass m is $\lambda = \frac{hc}{\sqrt{hc}}$.

$$\sqrt{K(K+2mc^2)}$$

Young and Freedman, Chap 39, pg. 1516, Q39.44 (a)

$$E^{2} = p^{2}c^{2} + m^{2}c^{4} \text{ and } E = K + mc^{2} \Rightarrow (K + mc^{2})^{2} = p^{2}c^{2} + m^{2}c^{4}$$

$$\Rightarrow p = \frac{[(K + mc^{2})^{2} - m^{2}c^{4}]^{1/2}}{c} = \frac{[K^{2} + 2Kmc^{2} + m^{2}c^{4} - m^{2}c^{4}]^{1/2}}{c}$$

$$= \frac{[K(K + 2mc^{2})]^{1/2}}{c}$$

$$\Rightarrow \lambda = \frac{h}{p} = \frac{hc}{[K(K + 2mc^{2})]^{1/2}}.$$

(d) A block is attached to a massless spring. The spring is stretched from its equilibrium position and released, and the block is set into a simple harmonic motion with a total energy of 2.0J with a frequency of oscillation 0.56 Hz. Assuming that the energy is quantised, find the quantum number *n* for the system.

Serway and Jewett, Chap 40, pg. 1291, Example 40.2

 $E_n = nhf = n(6.63 \times 10^{-34} \,\mathrm{J \cdot s})(0.56 \,\mathrm{Hz}) = 2.0 \,\mathrm{J}$

 $n = 5.4 \times 10^{33}$

2. (a) (*i*) The *x*-coordinate of an electron is measured with an uncertainty of 0.20 mm. What is the *x*-component of the electron's velocity, v_x , if the minimum percentage uncertainty in a simultaneous measurement of v_x is 1.0 %?

Young and Freedman, Chap 39, pg. 1514, Q39.20 (a)

 $(\Delta x) (m\Delta v_x) \ge h/4\pi$, and setting $\Delta v_x = (0.010)v_x$ and the product of the uncertainties equal to $h/4\pi$ (for the minimum uncertainty) gives $v_x = h/(4\pi m (0.010)\Delta x) = (57.9/2) \text{ m/s} = (29.0) \text{ m/s}.$

(*ii*) Repeat part a(*i*) for a proton.

Repeating with the proton mass gives 15.8 mm/s.

$$v_x \propto \frac{1}{m} \Rightarrow \frac{v_{x,(ii)}}{v_{x,(i)}} = \frac{m_{(i)}}{m_{(ii)}} \Rightarrow v_{x,(ii)} = v_{x,(i)} \frac{m_{(i)}}{m_{(ii)}} = v_{x,(i)} \frac{m_e}{m_p} = (5.5 \times 10^{-4}) \frac{9.1 \times 10^{-31}}{1.67 \times 10^{-27}} = 15.8 \text{ mm/s}.$$

(b) The unstable W^+ particle has a rest energy of 80.41 GeV (1 GeV = 10⁹ eV) and an uncertainty in rest energy of 2.06 GeV. Estimate the lifetime of the W^+ particle.

Young and Freedman, Chap 39, pg. 1515, Q39.22 $\Delta E \Delta t = \frac{h}{4\pi} \quad \Delta E = \Delta mc^2 \quad \Delta mc^2 = 2.06 \times 10^9 \text{ eV} = 3.30 \times 10^{-10} \text{ J}$ $\Delta t = \frac{h}{4\pi \Delta mc^2} = \frac{6.63 \times 10^{-34} \text{ J} \cdot \text{s}}{4\pi (3.3 \times 10^{-10} \text{ J})} = 1.6 \times 10^{-25} \text{ s}.$

(c) The kinetic energy of a nonrelativistic particle in terms of its momentum can be written as $K = p^2/2m$. Estimate the minimum kinetic energy of a proton confined within a nucleus having a diameter of 1 fm (1 fm = 10⁻¹⁵m)

Serway and Jewett, Chap 40, pg. 1317, Q52.

To find the minimum kinetic energy, think of the minimum momentum uncertainty, and maximum position uncertainty of 10^{-15} m = Δx . We model the proton as moving along a straight line with $\Delta p\Delta x = \frac{\hbar}{2}$, $\Delta p = \frac{\hbar}{2\Delta x}$. The average momentum is zero. The average squared momentum is equal to the squared uncertainty:

$$K = \frac{p^2}{2m} = \frac{(\Delta p)}{2m} = \frac{\hbar^2}{4(\Delta x)^2 2m} = \frac{\hbar^2}{32\pi^2 (\Delta x)^2 m} = \frac{(0.05 \times 10^{-5} \text{ s})}{32\pi^2 (10^{-15} \text{ m})^2 1.67 \times 10^{-27} \text{ kg}} = 8.33 \times 10^{-13} \text{ J}$$
$$= 5.21 \text{ MeV}$$

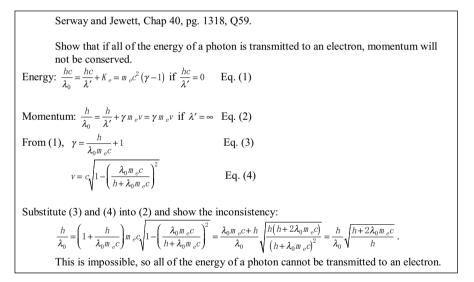
3. (a) Electrons are ejected from a metallic surface with speeds ranging up to 4.6×10^5 m/s when light with a wavelength of 625 nm is used in a photoelectric effect experiment.

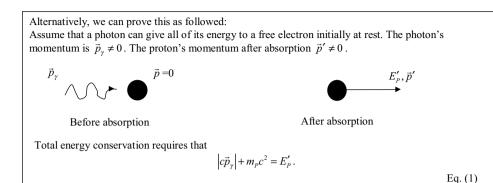
(*i*) What is the work function of the surface?(*ii*) What is the cutoff frequency for this surface?

Serway and Jewett, Chap 40, pg. 1315, Problem 14

$$K_{\text{m ax}} = \frac{1}{2} m v_{\text{m ax}}^{2} = \frac{1}{2} (9.11 \times 10^{-31}) (4.60 \times 10^{5})^{2} = 9.64 \times 10^{-20} \text{ J} = 0.602 \text{ eV}$$
(a) $\phi = E - K_{\text{m ax}} = \frac{1240 \text{ eV} \cdot \text{nm}}{625 \text{ nm}} - 0.602 \text{ nm} = \boxed{1.38 \text{ eV}}$
(b) $f_{c} = \frac{\phi}{h} = \frac{1.38 \text{ eV}}{6.626 \times 10^{-34} \text{ J} \cdot \text{s}} \left(\frac{1.60 \times 10^{-19} \text{ J}}{1 \text{ eV}} \right) = \boxed{3.34 \times 10^{14} \text{ H z}}$

(b) Show that a photon cannot transfer all of its energy to a free electron. (*Hint:* Note that the system energy and momentum transfer must be conserved).





Einstein's energy-momentum conservation formula relates the total energy of the proton after absorption, \vec{p}'_{p} , to the proton's momentum after photon absorption, \vec{p}' via

$$E_{P}^{\prime 2} = \left| \vec{p}^{\prime} \right|^{2} c^{2} + m_{P}^{2} c^{4}.$$

Squaring Eq. (1), we could relate \vec{p}' to \vec{p}_{x} by virtue of Eq. (2):

$$c^{2} \left| \vec{p}_{\gamma} \right|^{2} + m_{p}^{2} c^{4} + 2 \left| \vec{p}_{\gamma} \right| m_{p} c^{3} = E_{p}^{\prime 2} = \left| \vec{p}^{\prime} \right|^{2} c^{2} + m_{p}^{2} c^{4}$$

$$\Rightarrow \left| \vec{p}_{\gamma} \right|^{2} + 2 \left| \vec{p}_{\gamma} \right| m_{p} c = \left| \vec{p}^{\prime} \right|^{2}$$
Eq.(3)

Independently, we also require the process to observe total momentum conservation, $\vec{p}_v = \vec{p}' \Rightarrow |\vec{p}_v| = |\vec{p}'|$

Eq. (2)

Obviously, Eq. (3) and Eq. (4) are not consistent, hence, we conclude that both momentum and energy conservation does not hold simultaneously if a photon delivers all of its energy to a free electron.

4. (a) A particle of mass *m* is confined to an impenetrable one-dimensional box between x = 0 and

x = L. The wave function of the particle is $\psi(x) = A \sin\left(\frac{n\pi x}{L}\right)^{-1}$

(i) Use the normalization condition on ψ to obtain the normalization constant A.

- (ii) Find the expectation value of the position x of the particle in the ground state.
- (*iii*) Calculate the probability of finding the electron between x=0 and x = L/4 in the ground state.

or $\int_{0}^{L} A^{2} \sin^{2} \left(\frac{n\pi x}{L} \right) dx = 1$

(i) Normalization requires

$$\int_{a \text{ ll space}} |\Psi|^2 dx = 1$$
$$\int_{0}^{L} A^2 \sin^2\left(\frac{n\pi x}{L}\right) dx = A^2\left(\frac{L}{2}\right) = 1$$

(ii)

 $\langle x \rangle$

2)

Serway and Jewett, Chap 41, pg. 1346, Problem 17, 18.

$$= \int_{0}^{L} x \frac{2}{L} \sin^{2}\left(\frac{\pi x}{L}\right) dx = \frac{2}{L} \int_{0}^{L} x \left(\frac{1}{2} - \frac{1}{2} \cos\frac{2\pi x}{L}\right) dx = \frac{1}{L} \frac{x^{2}}{2} \Big|_{0}^{L} - \frac{1}{L} \frac{L^{2}}{16\pi^{2}} \left[\frac{4\pi x}{L} \sin\frac{4\pi x}{L} + \cos\frac{4\pi x}{L}\right]_{0}^{L} = \boxed{\frac{L}{2}}$$

or

(iii) The desired probability is

$$P = \int_{0}^{L/4} |\Psi|^2 dx = \frac{2}{L} \int_{0}^{L/4} \sin^2 \left(\frac{\pi x}{L}\right) dx = \frac{2}{L} \left(\frac{x}{2} - \frac{1}{4\pi} \sin \frac{2\pi x}{L}\right)_{0}^{L/4} = \frac{2}{L} \left(\frac{L}{8} - 0 - 0 + 0\right) = \boxed{0.250}$$

(b) Why is it impossible for the lowest-energy state of a harmonic oscillator to be zero?

Serway and Jewett, Chap 41, pg. 1345, Question 8.

Quantum mechanically, the lowest kinetic energy possible for any bound particle is greater than zero. The following is a proof: If its minimum energy were zero, then the particle could have zero momentum and zero uncertainty in its momentum. At the same time, the uncertainty in its position would not be infinite, but equal to the width of the region in which it is restricted to stay. In such a case, the uncertainty product $\Delta x \Delta p_x$ would be zero, violating the uncertainty principle. This contradiction proves that the minimum energy of the particle is not zero. Any harmonic oscillator can be modeled as a particle or collection of particles in motion; thus it cannot have zero energy.

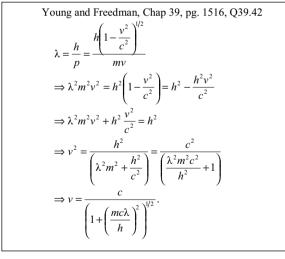
5. (a) A ψ particle has mass 5.52×10^{-27} kg. Compute the rest energy of the particle in MeV.

Young and Freedman, Chap 37, pg. 1440, Q37.42 $(5.52 \times 10^{-27} \text{ kg})(3.00 \times 10^8 \text{ m/s})^2 = 4.97 \times 10^{-10} \text{ J} = 3105 \text{ MeV}.$

(b) A cube of metal with sides of length a sits at rest in a frame S with one edge parallel to the x-axis. Therefore in S the cube has volume a³. Frame S' moves along the x-axis with a speed u. As measured by an observer in frame S', what is the volume of the metal cube?

Young and Freedman, Chap 37, pg. 1441, Q37.50 One dimension of the cube appears contracted by a factor of $\frac{1}{\gamma}$, so the volume in S' is $a^3/\gamma = a^3\sqrt{1-(u/c)^2}$.

(c) High-speed electrons are used to probe the interior structure of the atomic nucleus. For such electrons the expression $\lambda = h/p$ still holds, but we must use the relativistic expression for momentum $p = \frac{mv}{\sqrt{1 - v^2/c^2}}$. Show that the speed of an electron that has de Broglie wavelength λ is $v = \frac{c}{\sqrt{1 + \left(\frac{mc\lambda}{h}\right)^2}}$



6. (a) How much energy is required to ionize hydrogen? (*i*) in the ground state?

(*ii*) when it is in the state for which *n*=3?

Serway and Jewett, Chap 42, pg. 1392, Problem 8.

(a) We use
$$E_n = \frac{-13.6 \text{ eV}}{2}$$

To ionize the atom when the electron is in the n^{th} level, it is necessary to add an amount of energy given by $E = -E_n = \frac{13.6 \text{ eV}}{2}$.

(i) Thus, in the ground state where n = 1, we have E = 13.6 eV

(ii) In the
$$n = 3$$
 level, $E = \frac{13.6 \text{ eV}}{9} = \boxed{1.51 \text{ eV}}$.

(b) Two hydrogen atoms collide head-on and end up with zero kinetic energy. Each atom then emits light with a wavelength of 121.6 nm (n=2 to n=1 transition). At what speed were the atoms moving before collision?

Serway and Jewett, Chap 42, pg. 1392, Problem 11.

Each atom gives up its kinetic energy in emitting a photon,

so
$$\frac{1}{2}mv^2 = \frac{hc}{\lambda} = \frac{(6.626 \times 10^{-34} \text{ J} \cdot \text{s})(3.00 \times 10^8 \text{ m/s})}{(1.216 \times 10^{-7} \text{ m})} = 1.63 \times 10^{-18} \text{ J}$$

 $v = 4.42 \times 10^4 \text{ m/s}$. Note: the mass of a hydrogen is taken to be the same as the mass of a proton, $1.67 \times 10^{-27} \text{kg} = 938 \text{MeV}$

- (c) Based on the Bohr model, derive the expression for the Bohr radius for hydrogen atom from scratch. Express you answer in unit of Å.

Serway and Jewett, Chap 42, pg. 1392, Problem 11.

Quantisation of angular momentum:

$$L = mvr = n\hbar \Rightarrow v = \frac{nn}{mr} \qquad \text{Eq. (1)}$$
Mechanical stability:

$$\frac{mv^2}{r} = \frac{Ze^2}{4\pi\varepsilon_0 r^2} \qquad \text{Eq. (2)}$$
Substitute v from Eq. (1) into Eq. (2), we have $\frac{m\left(\frac{n\hbar}{mr}\right)^2}{r} = \frac{Ze^2}{4\varepsilon_0\pi r^2} \Rightarrow r = \frac{n^2}{Z}\frac{4\pi\varepsilon_0\hbar^2}{me^2} \equiv \frac{n^2}{Z}a_0$

$$a_0 = \frac{4\pi\varepsilon_0\hbar^2}{me^2} = 0.53 \text{ Å}$$